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Design of Modified 4×6 Filtering Butler Matrix Based on All-Resonator Structures

Qiang Shao, Fu-Chang Chen, Member, IEEE, Yi Wang, Senior Member, IEEE, Qing-Xin Chu, Fellow, IEEE and Michael J. Lancaster, Senior Member, IEEE

Abstract—In this paper, two novel 4×6 filtering Butler matrices with uniform and non-uniform power distribution are proposed. The matrices, consisting of a network of coupled resonators and two phase shifters, provide power division and phase shift together with a bandpass transfer function. The analytical synthesis procedures for the 4×6 filtering Butler matrices is presented. To verify the concept experimentally, two 4×6 filtering Butler matrices, operating at 2.4 GHz, with uniform and non-uniform power distribution are designed, fabricated, and measured. Simulated and measured results are found to be in good agreement with each other. Multibeam antenna arrays are realized by using the Butler matrix and the theoretical analysis has been confirmed by measurements of multibeam antenna arrays, which show reduced sidelobe level.

Index Terms—Bandpass filter, Butler matrix, microstrip, switched-beam antenna.

I. INTRODUCTION

In recent years, the switched-beam antenna has become of great interest as it can achieve higher spectral efficiency and enhance the capacity of wireless communication systems. The standard switched-beam antenna array generally consists of three parts: switches, a beam-forming network (BFN), and an antenna array [1]. The switches determine which port the signal will be input from. The signal is then split in the BFN with incremental phases generated at its outputs. Finally, the output signal feed into the antenna array. The BFN is the core part of the switched-beam antenna array as the main beam will point at different directions based on the signals generated by it. Except for the Blass matrix [2], which is a lossy one, there are other two kinds of popular BFNs. One such a BFN is the Nolen matrix [3] and several Nolen matrices have been demonstrated for narrow band applications [4]-[6]. Another popular BFN is the Butler matrix [7], which is the subject of this paper. Several Butler matrices have been proposed for switched-beam antenna arrays [8]-[11]. In practical use, additional bandpass filters may be cascaded before the switches, to suppress spurious modes of the resonators, as well as reducing the intermodulation products generated by the amplifiers. In this paper, to reduce the size and volume of such a system, the BFN and bandpass filter are replaced by a new Butler matrix with an inherent bandpass filter function. Conventionally the Butler matrix consists of several hybrid couplers and phase shifters and [12]-[14] present detailed systematic design methods. Introducing filtering functions to the hybrid couplers provides frequency selectivity into the Butler matrix. In [15]-[20], work has been done to introduce filtering functions to the hybrid coupler. A novel class of waveguide Butler matrices with inherent bandpass filter transfer functions was presented in [21]: the application here was in multi-port distributed power amplifiers. For antenna arrays, a low sidelobe level (SLL) is highly desired and one of the most effective methods to reduce the SLL is to apply non-uniform power tapering [22]-[24]. Several Butler matrices and Nolen matrices with reduced SLL have been proposed in [25]-[30], however these do not contain implicit filtering.

Recently, the authors have presented a 2×4 filtering Butler matrix using coupled resonators [31]. As the electric and magnetic coupling only generate ±90° phase shift, the resultant Butler matrix only provided two phase increments...
To extend the number of ports and generate more switched beams is a significant design challenge. In this paper, prototypes of a 4 × 6 filtering Butler matrix with a new modified topology and both uniform and non-uniform power distribution are presented. The analytical synthesis procedures for the Butler matrices are detailed, and example 4 × 6 filtering microstrip Butler matrices are designed, fabricated, and measured.

The paper is organized as follows. The design procedure of the modified 4 × 6 filtering Butler matrix with uniform power distribution is given in Section II. In Section III, a novel 180° filtering hybrid coupler with non-uniform power distribution is proposed. By utilizing this coupler, a modified 4 × 6 filtering Butler matrix with non-uniform power distribution is designed, fabricated and measured. Lastly, Section IV concludes this paper.

II. DESIGN OF MODIFIED 4 × 6 FILTERING WITH UNIFORM POWER DISTRIBUTION

A. Analysis

In our previous paper [29], a 180° filtering hybrid coupler, as shown in Fig. 1(a), was proposed. It is used in this paper as the building block of the new filtering Butler matrix. To realize the embedded filtering characteristic, the connecting network is formed of coupled resonators. However, this presents a problem with the implementation of the phase shifter in the connecting network. To overcome this, a modified configuration of Butler matrix is shown in Fig. 1(b). Compared with the traditional topology of Butler matrix, an additional 180° hybrid coupler is introduced, and the phase shifter is moved from within the connecting network to the terminals. This facilitates the circuit implementation using resonators. However, in this case, there are six output ports but effectively only four are used. When using this matrix to feed a 4-element linear array as illustrated later in this paper, combining devices may be required in the final antenna system implementation, possibly with some impact on the RF performance. Fig. 2(a) and (b) show the coupling scheme of the modified 4 × 6 filtering Butler matrix and its microstrip layout on a substrate with a dielectric constant εr = 2.55, a loss tangent δ = 0.0029, and a thickness h = 0.8 mm. There are twenty-four resonators in the microstrip layout, each of which is a half-wavelength uniform impedance resonator and resonates at the central frequency of the bandpass filter (f0). A 180° filtering hybrid coupler is composed of four resonators with an appropriate coupling scheme. The couplers are connected by direct coupling between resonators and the -90° phase shifters are realized by quarter-wavelength uniform impedance microstrip lines.

When port P1 or port P2 is the input port, based on the analysis in [29], the output ports P5, P6, P7, and P8 have equal amplitude and 0° or 180° phase shift. In this case the other ports are isolated. When port P3 is used as the input port, the

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Fig. 2. (a) Coupling scheme of the modified 4 × 6 filtering Butler matrix. (b) Layout of the modified 4 × 6 filtering Butler matrix. (L1 = 10.89, L4 = 7.00, L2 = 10.00, L3 = 13.54, L7 = 12.47, L8 = 13.08, L9 = 18.36, L10 = 10.00, L11 = 14.83, L12 = 11.48, L13 = 25.48, L14 = 21.45, L15 = 5.00, S1 = 0.2, S6 = 0.2, W1 = 0.4, W2 = 1.0, W3 = 2.2, all in millimeters.)
phases of the output ports P6, P9, P8 and P10 can be calculated as

\[ \angle S_{o3} - \angle S_{o3} = (\angle S_{c3} + \angle S_{dc} + \angle S_{9d}) \]
\[ - (\angle S_{a3} + \angle S_{ba} + \angle S_{ab}) \]
\[ = (\angle S_{c3} - \angle S_{a3}) + (\angle S_{dc} - \angle S_{ba}) \]
\[ + (\angle S_{9d} - \angle S_{ab}) \] (1)

\[ \angle S_{h3} - \angle S_{h3} = (\angle S_{a3} + \angle S_{ba} + \angle S_{ab}) \]
\[ - (\angle S_{c3} + \angle S_{dc} + \angle S_{9d}) \]
\[ = (\angle S_{a3} - \angle S_{c3}) + (\angle S_{ba} - \angle S_{dc}) \]
\[ + (\angle S_{ab} - \angle S_{9d}) \] (2)

\[ \angle S_{10,3} - \angle S_{10,3} = (\angle S_{c3} + \angle S_{dc} + \angle S_{10d}) \]
\[ - (\angle S_{a3} + \angle S_{ba} + \angle S_{ab}) \]
\[ = (\angle S_{c3} - \angle S_{a3}) + (\angle S_{dc} - \angle S_{ba}) \]
\[ + (\angle S_{10d} - \angle S_{ab}) \] (3)

where \( \angle S_{ba} \) represents the phase response between the ports and the nodes A, B, C, D are defined in Fig. 1(b). Based on the properties of the 180° hybrid coupler, and taking the phase shift into account, the phase response across the output ports is

\[ \angle S_{c3} = \angle S_{a3} \] (4)

\[ \angle S_{10d} - \angle S_{10d} = \angle S_{9d} - \angle S_{9d} = \angle S_{ba} - \angle S_{ab} = 90° \] (5)

The modified 4 × 6 filtering matrix is realized by connecting the couplers together via AB and CD. These connections are simply made by coupling the resonators to the adjacent couplers as seen in Fig 2(a). The couplings are electrical, so the phase response of the connecting network is

\[ \angle S_{dc} = \angle S_{9d} \] (6)

Considering (1) to (6), when port P3 is used as the input port, the output phase increment can be calculated as

\[ \angle S_{o3} - \angle S_{o3} = \angle S_{o3} - \angle S_{o3} = \angle S_{10,3} - \angle S_{a3} = 90° \] (7)

In the same way, when port P4 is the input port, the output port phases can be calculated as

\[ \angle S_{9d} - \angle S_{9d} = \angle S_{9d} - \angle S_{9d} = \angle S_{10} - \angle S_{a4} = 90° \] (8)

As in [29], the +90° admittance inverters \( J \) are used to model the input and output coupling. In Fig. 2(a) the +90° and -90° admittance inverters are used to represent the coupling dominated by electric fields and magnetic fields, respectively. Each path from an input port to an output port is equivalent to a fifth-order bandpass filter, as shown in Fig. 3; here the resonators are represented by parallel LC circuits. So the design can now follow that of a basic bandpass filter. Once the design requirements, such as the center frequency \( (f_0) \), fractional bandwidth (FBW) and ripple level are given, the element values \( (g_1, g_2, g_3, g_4, g_5) \) for the lowpass prototype
filter can be obtained, and then the bandpass coupling matrix design parameters can be calculated as follows [32]:

\[
Q_{c1} = \frac{g_1 g_5}{FBW}, \quad Q_{c2} = \frac{g_3 g_6}{FBW} \quad (9)
\]

\[
M_{12} = \pm \frac{\sqrt{2}FBW}{2g_1 g_2}, \quad M_{23} = \frac{FBW}{\sqrt{g_2 g_3}}
\]

\[
M_{34} = \frac{FBW}{\sqrt{g_3 g_4}}, \quad M_{45} = \pm \frac{\sqrt{2}FBW}{2\sqrt{g_4 g_5}} \quad (10)
\]

here \(Q_{c1}\) and \(Q_{c2}\) are the external quality factors of the resonators at the input and output, and \(M_{12}, M_{23}, M_{34}, M_{45}\) are the coupling coefficients between the adjacent resonators (“+” denotes a coupling that is dominated by electric coupling, and “-” denotes one dominated by magnetic coupling).

**B. Synthesis example**

In order to verify the design concept, the new filtering Butler matrix has been designed, fabricated and measured. The center frequency of the filter is taken to be 2.4 GHz with a fractional bandwidth of 8%. The ripple level is 0.04321 corresponding to a 20 dB return loss. Therefore, the element values for the lowpass prototype filter are \(g_1 = 0.9714, g_2 = 1.3721, g_3 = 1.8014, g_4 = 1.3721\) and \(g_5 = 0.9714\). Based on (9) and (10), the external quality factors can be calculated as \(Q_{c1} = Q_{c2} = 12.14\) and the coupling coefficients between adjacent resonators are calculated as \(M_{12} = M_{45} = \pm 0.049\) and \(M_{23} = M_{34} = 0.050\).

Fig. 4 shows the extracted input and output resonators external quality factor with respect to the length of the feedlines (\(L_1\) and \(L_2\)). These are obtained following the technique described in [32]. From the graph, the length of the feeding lines, for the required \(Q_o\), can be obtained as \(L_1 = 12.20\) mm and \(L_2 = 13.80\) mm. These lengths are good initial values, but further optimization is required as described below. Similarly, the extracted coupling coefficients with respect to the gaps \(S_2, S_3, S_4\) and \(S_5\) are shown in Fig. 5 [32]. The initial values of the gaps between adjacent resonators can now be obtained as \(S_2 = 0.54\) mm, \(S_3 = 0.8\) mm, \(S_4 = 0.72\) mm and \(S_5 = 1.22\) mm. To improve the overall response, the initial dimensions of the gaps are optimized using IE3D software to be \(L_1 = 12.20\) mm, \(L_2 = 13.45\) mm, \(S_2 = 0.56\) mm, \(S_3 = 0.82\) mm, \(S_4 = 0.71\) mm and \(S_5 = 1.16\) mm. The small differences between the initial and optimized values show the excellent accuracy of the extraction technique.

**C. Measurement results**

Fig. 6 shows a photograph of the fabricated filtering Butler matrix. Fig. 7(a) and (b) show the simulated and measured S-
parameters when the signal is input at port $P_1$ and port $P_3$. The measured results are in good agreement with the simulated results. The measured minimum insertion loss for the bandpass filter is 8.9 dB, including the 6 dB power division and 2.9 dB filter loss. The return losses are higher than 15 dB. This deviation from 20 dB is likely caused by small errors in the structure dimensions. The measured isolation between port $P_1$ and port $P_2$ and between port $P_3$ and port $P_4$ is larger than 22 dB in both cases. The measured output phases of the Butler matrix are shown in Fig. 7(c) and (d). As expected, $\angle S_{51}$, $\angle S_{61}$, $\angle S_{71}$ and $\angle S_{81}$ have equal phase and $\angle S_{65}$, $\angle S_{93}$, $\angle S_{85}$ and $\angle S_{10,3}$ have -90° phase shift. Over the 3-dB fractional bandwidth (2.3-2.5 GHz) of the filter, the measured phase imbalances are within ±10°.
D. Switched-beam antenna array

A switched-beam antenna array has been used to further test the filtering Butler matrix. The radiation element should have a broadband characteristic to cover the bandwidth of the bandpass filter, so a Vivaldi antenna is chosen. This is shown in Fig. 8(a). Four antenna elements have been equally spaced at a distance of 62.5 mm, which corresponds to 0.5 λ at 2.4 GHz. The Butler matrix is connected to the antenna array via coaxial cables of equal-length, as shown in Fig. 8(b). It is worth mentioning that coaxial cables will need to be reconnected to the adequate antenna array elements when the input ports change from ports 1 and 2 to ports 3 and 4. The simulated and measured radiation patterns of the array obtained at 2.4 GHz are shown in Fig. 9. The directions of the main beams point at 0°, as shown in Fig. 9(a), when port P1 is used as the input port, whereas endfire performance is obtained when port P2 is the input port, as shown in Fig. 9(b). When port P3 and port P4 are used as the input port, the directions of the main beams point at -30° and +30°, as shown in Fig. 9(c) and (d) respectively. It can be seen that the measured results closely match the simulated results.

III. DESIGN OF 4 × 6 FILTERING BUTLER MATRIX WITH NON-UNIFORM POWER DISTRIBUTION

A. Analysis

In a practical application a low sidelobe level is important for the antenna array to select the desired signals. This can be achieved by a non-uniform power distribution of signals across the array. This section describes the design of a new 4 × 6 filtering Butler Matrix with non-uniform power distribution to achieve the desired level. A novel 180° filtering
hybrid coupler with unequal power distribution based on microstrip resonators is shown in Fig. 10(a). All the four microstrip resonators are half-wavelength uniform impedance resonators, which resonate at the central frequency of the filter. The input ports P1 and P2 are coupled to the resonators 1 and 4. The output ports P3 and P4 are coupled to the resonators 2 and 3. The coupling level between resonators 2 and 4 as well as between resonators 1 and 3 are equal in magnitude. So are the coupling level between resonators 1 and 2 and between resonators 3 and 4. However, the couplings between resonators 1 and 2, 1 and 3, 3 and 4 are dominated by the electric field, whereas the coupling between resonators 2 and 4 is dominated by the magnetic field. Different from the hybrid in [29], the coupling level between the resonators 1 and 2, and between resonators 1 and 3 are not identical. They control the power ratio of the output ports. This also applies to the coupling strengths between resonators 2 and 4 and between resonators 4 and 3.

Fig. 10(b) shows the equivalent circuit of the hybrid coupler. The coupling scheme of the coupler is the same as the 180° filtering hybrid coupler in [29], and therefore the output phase shifts remain unchanged. When the input signal is from port P1, the equivalent circuit is reduced to Fig. 11(a) because port P2 is isolated. The input admittance \( Y_{inA} \) from node A can be expressed as

\[
Y_{inA} = \frac{J_{12(1)}}{Y_{inB}} + \frac{J_{12(2)}}{Y_{inC}} Y_{inA} = \frac{J_{12(1)}}{Y_{inB}} + \frac{J_{12(2)}}{Y_{inC}}
\]

(11)

where \( Y_{inB} \) and \( Y_{inC} \) are the input admittance seen from node B and C. They can be expressed in turn as

\[
Y_{inB} = Y_{inC} = \frac{J_{23}}{Y_0} + j\omega L + \frac{1}{j\omega L}
\]

(12)

Hence the input admittance \( Y_{inA} \) becomes

\[
Y_{inA} = \frac{J_{12(1)}}{Y_{inB}} + \frac{J_{12(2)}}{Y_{inC}} = \frac{J_{12(1)}}{Y_{inB}} + \frac{J_{12(2)}}{Y_{inC}}
\]

(13)

It can be seen that the equivalent circuit in Fig. 11(a) is a second-order bandpass filter as shown in Fig. 11(b), this then gives

\[
J_{12(1)}^2 + J_{12(2)}^2 = J_{12}^2
\]

(14)

where \( J_{12} \) is the inverter in the standard filter.

Now define \( K \) as the power ratio between the output port P3 and P4 when the input is at port P1. \( K \) can be expressed as [23]
From (14) and (15), it can be found that
\[ J_{12(1)} = \frac{K}{K+1} J_{12(2)} \]
\[ J_{12(2)} = \frac{1}{K+1} J_{12(2)} \]
Therefore, the equivalent circuit of the 180° hybrid coupler from input port P1 to output ports P3 and P4 can be further reduced to the circuits in Fig. 11(c) and (d), respectively. The filter design parameters can be calculated as follows [32]
\[ Q_c = \frac{g_6 g_{11}}{FBW}, \quad Q_e = \frac{g_6 g_{11}}{FBW} \]
\[ M_{12(1)} = \frac{K}{1+K} \frac{FBW}{\sqrt{g_1 g_2}}, \quad M_{12(2)} = \pm \frac{1}{1+K} \frac{FBW}{\sqrt{g_1 g_2}}. \]
Here, \( Q_c \) and \( Q_e \) are the external quality factors of the resonators at the input and output, and \( M_{12(1)} \) and \( M_{12(2)} \) are the coupling coefficients between the adjacent resonators. By symmetry, when the signal is input from port P2, the power ratio of the output port P3 and port P4 is \( 1/K \).

To realize a 4 × 6 Butler matrix with non-uniform power distribution, the 180° filtering hybrid couplers connected to the output ports in Fig. 1(c) are replaced by the new couplers with unequal power ratio, as shown in Fig. 12. Fig. 13 shows the microstrip layout of the Butler matrix with non-uniform power distribution. Similar to the analysis in Section II, each path from an input to an output port can be equivalent to a fourth order bandpass filter as shown in Fig. 14. The bandpass design parameters can thus be calculated as [32]
\[ Q_c = \frac{g_6 g_{11}}{FBW}, \quad Q_e = \frac{g_6 g_{11}}{FBW} \]
\[ M_{12(1)} = \pm \frac{\sqrt{2FBW}}{2\sqrt{g_1 g_2}}, \quad M_{12(2)} = \frac{FBW}{\sqrt{g_1 g_3}} \]
\[ M_{34(1)} = \frac{K}{1+K} \frac{FBW}{\sqrt{g_1 g_2}} M_{34(2)} = \pm \frac{1}{1+K} \frac{FBW}{\sqrt{g_1 g_2}} \]

**B. Synthesis example**

In order to verify the design concept, a modified 4 × 6 filtering Butler matrix with output ports P5, P6, P7, P8 (or ports P6, P9, P8, P10) and power ratio of 1:3:3:1 is designed, fabricated and measured. The center frequency of the filter is taken to be 2.4 GHz with a fractional bandwidth of 4.5%. The
ripple level is 0.04321. The element values can be obtained as $g_1 = 0.9314, g_2 = 1.2920, g_3 = 1.5775, g_4 = 0.7628$ and $g_5 = 1.2210$. Based on (19) and (20), the external quality factors can be easily calculated as $Q_{e1} = Q_{e2} = 20.7$ and the coupling coefficients between adjacent resonators are calculated as $M_{12} = \pm 0.033$ and $M_{23} = 0.033$. For coupler 3 in Fig 12, the power ratio $K_1$ is required to be 1/3, so $M_{341} = 0.021$ and $M_{342} = 0.036$. For coupler 4, the power ratio is $K_4 = 1/3$, so $M_{451} = 0.021$ and $M_{452} = 0.036$ and for coupler 5 the power ratio should be $K_5 = 3$, so $M_{561} = 0.036$ and $M_{562} = 0.021$.

Using an extraction procedure similar to that in Section II, the initial values of the length of the feeding lines, for the required $Q_e$, can be obtained as $L_1 = 13.20$ mm and $L_2 = 13.80$ mm. The gaps between the adjacent resonators are $S_2 = 0.81$ mm, $S_3 = 1.15$ mm, $S_4 = 1.85$ mm, $S_5 = 1.20$ mm, $S_6 = 0.75$ mm, $S_7 = 1.59$ mm, $S_8 = 1.74$, $S_9 = 1.12$ mm, $S_{10} = 1.10$ mm and $S_{11} = 2.38$ mm according to the design curves in Fig. 5. The final dimensions of the gaps in Fig. 13 are optimized using IES3D software to be $L_1 = 13.28$ mm, $L_2 = 13.78$ mm, $S_2 = 0.91$ mm, $S_3 = 1.23$ mm, $S_4 = 1.67$ mm, $S_5 = 1.23$ mm, $S_6 = 0.75$ mm, $S_7 = 1.65$ mm, $S_8 = 1.67$, $S_{10} = 1.27$ mm, $S_{11} = 1.06$ mm and $S_{12} = 2.35$ mm. Again, the small difference in the values after optimization indicate the accuracy of the technique.

C. Measurement results

Fig. 15 shows a photograph of the fabricated Butler matrix. Measurements have been done taking the input ports P1 and P3 as an example. The simulated and measured S-parameters of the fabricated Butler matrix are shown in Fig. 16(a) and (b). For the low power path, the measured minimum insertion loss is 11.8 dB, including the 9 dB power division and 2.8 dB filter loss. For the high power path, the measured minimum insertion loss is 7.2 dB, including the 4.3 dB power division and 2.9 dB filter loss. The measured return losses are higher than 14 dB and the isolation between port P1 and port P2 (or port P3 and port P4) is larger than 25 dB. The measured output phases of the fabricated non-uniform filtering Butler matrix are shown in Fig. 16(c) and (d). When the input signal is from port P1, the phases $\angle S_{51}, \angle S_{61}, \angle S_{13}$ and $\angle S_{14}$ are almost equal. When the input signal is from port P3, the phases $\angle S_{53}, \angle S_{63}, \angle S_{83}$ and $\angle S_{93}$ are around -90°. Over the 3-dB fractional bandwidth (2.34-2.46 GHz) of the bandpass filter, all the measured phase imbalances are within ±9°.

Again, a Vivaldi antenna array has been used to further test the filtering Butler matrix. The simulated and measured radiation patterns of the Vivaldi antenna array obtained at 2.4 GHz are shown in Fig. 17. This is a linear plot for clearer comparison. As expected, the main beams angles are 0°, 180°, -30°, +30° when the input is at port P1, P2, P3, P4 respectively. More importantly, Fig 17 shows that with the non-uniform power excitation, the measured sidelobe levels have been reduced from -10 dB to -15 dB. Good agreement has been obtained between the simulated and measured results.

IV. CONCLUSION

A systematic design procedure of two modified 4 × 6 filtering Butler matrices with uniform and non-uniform power distribution have been presented in this paper. The Butler matrix is composed of coupled resonators and phase shifters, providing power division, phase shift and a bandpass response. By controlling the coupling between resonators in the couplers, a 4 × 6 filtering Butler matrix with non-uniform power distribution has been designed to suppress side lobe levels. For validation, two 4 × 6 filtering Butler matrices with uniform and non-uniform power distribution have been designed, fabricated and measured. In addition, a Vivaldi antenna array was used to examine the radiation performance of the new Butler matrix design. Close correlation between the simulated and measured results confirms the effectiveness of the design method. It is worth mentioning that in this paper a single layer substrate is used, this leads to output ports locations in the same plane. A conventional Butler matrix has another crossing layer before the output ports which may lead to more flexibility in port location.

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Qiang Shao was born in Xianning, Hubei Province, China, in January 1993. He received the B.S. degree in information engineering from Shantou University, Shantou, Guangdong, China in 2015. He is currently working towards the Ph.D. degree at South China University of Technology. His research interests include microwave filters and associated RF circuits for microwave and millimeter-wave applications.

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He is the foundation chair of IEEE Guangzhou AP/MMT Chapter, the senior members of IEEE and the China Electronic Institute (CEI). He has published over 300 papers in journals and conferences, which were indexed in SCI more than 1500 times. One of his papers published in IEEE Transactions on Antennas and Propagations in 2008 becomes the top ESI (Essential Science Indicators) paper within 10 years in the field of antenna (SCI indexed self-excluded in the antenna field). He is currently serving as the highly cited scholar by Elsevier in the field of Electrical and Electronic Engineering. He has authorized more than 30 invention patents of China.

He was the recipient of the Science Award by Guangdong Province in 2013, the Science Awards by the Education Ministry of China in 2008 and 2002, the Fellowship Award by Japan Society for Promotion of Science (JSPS) in 2004, the Singapore Tan Chian Tuan Exchange Fellowship Award in 2003, the Educational Award by Shaanxi Province in 2003.
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