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Forecasting carbon price using empirical mode decomposition and

evolutionary least squares support vector regression

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7 Abstract: Conventional methods are less robust in terms of accurately forecasting non-stationary and nonlineary 8 carbon prices. In this study, we propose an empirical mode decomposition-based evolutionary least squares support 9 vector regression multiscale ensemble forecasting model for carbon price forecasting. Firstly, each carbon price is 10 disassembled into several simple modes with high stability and high regularity via empirical mode decomposition. 11 Secondly, particle swarm optimization-based evolutionary least squares support vector regression is used to forecast each mode. Thirdly, the forecasted values of all the modes are composed into the ones of the original carbon price. 12 13 Finally, using four different-matured carbon futures prices under the European Union Emissions Trading Scheme as 14 samples, the empirical results show that the proposed model is more robust than the other popular forecasting methods 15 in terms of statistical measures and trading performances.

Keywords: carbon price forecasting; empirical mode decomposition; least squares support vector regression; particleswarm optimization

18 **1. Introduction**

19 Global climate change, as a grand challenge faced by the human society, is attracting more and more attention 20 around the world in the recent few decades. To address this challenge, the Kyoto Protocol, signed in 1997, came into 21 effect on February 16, 2005. The protocol established the quantitative greenhouse gas emission reduction targets for the 22 developed and industrialized countries. To achieve these targets effectively, the European Union Emissions Trading 23 System (EU ETS) was initiated in January 2005. The EU ETS has been the biggest carbon trading market so far. It also 24 provides an important demonstration of carbon market construction for other countries or regions, as well as a new 25 investment choice for investors [1]. In light of this, it is important to improve the accuracy of carbon price forecasting. 26 On the one hand, accurately forecasting carbon prices can contribute to a deep understanding on the characteristics of 27 carbon prices so as to establish an effective and stable carbon pricing mechanism. On the other hand, it can provide a 28 practical guidance for production operations and investment decisions, helping to avoid carbon price risks and 29 maximize carbon assets. Therefore, carbon price prediction has become one of the most popular topics in energy 30 research.

As we know, prediction technology generally can be classified into two categories: (i) time series forecasting, and 31 32 (ii) multi-factor forecasting. Although multi-factor forecasting can consider the influences of exogenous variables, it is 33 used to forecast the carbon price in the premise of forecasting the exogenous variables, which will inevitably lead to the 34 problem of error accumulation so as to make the failure of carbon price prediction. Time series prediction can predict 35 the future trend of carbon price by establishing a mathematical model to extend the trend of its own historical 36 changeable law without the influences of exogenous variables, which can obtain a good prediction accuracy. Many 37 studies have proven that time series prediction is applicable for energy and carbon price forecasting. Thereby, 38 multi-factor forecasting is excluded, and time series forecasting is utilized to predict carbon price in this study. Recently, 39 carbon price forecasting has attracted more and more research attentions [2-11]. The time series forecasting approaches

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used so far can be roughly divided into two broad categories: statistical and econometric models, and artificial
intelligence (AI) models. The former includes the multiple linear regression [2], GARCH [3], MS-AR-GARCH [4],
FIAPGARCH [5], HAR-RV [6], and nonparametric models [7]. The latter includes artificial neural networks (ANNs)
[8,9] and least squares support vector regression (LSSVR) [10,11]. Although the existing methods can obtain good
results when they are applied for stationary time series forecasting, they are not robust for forecasting accurately carbon
price due to its highly non-stationary and nonlinear characteristics [12].

7 Empirical mode decomposition (EMD), proposed by Huang and his co-authors in 1998, is an effective approach for handling the nonlinear and non-stationary time series [13,14,15]. EMD can disassemble any carbon price into 8 9 several intrinsic mode functions (IMFs) plus a residue with high stability and high regularity. When the IMFs and 10 residue are used as the inputs of ANN or LSSVR, it can improve learning efficiency and forecasting accuracy by 11 providing better understanding and feature-capturing [11,16]. Thereby, the accuracy of carbon price forecasting can be 12 enhanced through EMD. During the past few years, the EMD-based ANN and/or LSSVR models have been applied for 13 time series forecasting [17-26], including carbon price forecasting [11,16]. However, the traditional back-propagation ANNs, used as the predictors, can lead to the overfitting problems. Although LSSVR, built on the structural risk 14 15 minimization, can effectively solve the overfitting problem [27], the performance of a LSSVR predictor is sensitive to 16 its own model selection. Yet the hybrid EMD and LSSVR models have rarely been employed for carbon price 17 forecasting. Thus, this study seeks to address this gap in carbon price forecasting methodology.

18 The aim of this study is to develop an EMD-based evolutionary LSSVR model to forecast carbon prices with high 19 accuracy. The contributions of the study are two-fold. On the one hand, an EMD-based evolutionary LSSVR model 20 (EMD-LSSVR-ADD) is constructed to forecast carbon prices: (1) each carbon price is decomposed into several IMFs plus a residue with high stability and high regularity via EMD; (2) all the IMFs and residues are respectively predicted 21 22 via LSSVR trained by particle swarm optimization (PSO); (3) the forecasted values of all the IMFs and residues are 23 aggregated into the ones of the original carbon price. On the other hand, using the empirical data from four 24 different-matured carbon futures under the EU ETS, the study compares the forecasted results of the proposed model 25 with the single ARIMA and LSSVR models, the hybrid ARIMA+LSSVR model, and a variation of the forecasting 26 model (EMD-ARIMA-ADD) to demonstrate its robustness. Guo et al. (2012)[28] argued that it may be more suitable to 27 integrate all IMFs without IMF_1 when forecasting wind speed. Thus the study adds two models by removing the IMF_1 28 from EMD-ARIMA-ADD and EMD-LSSVR-ADD to test whether this approach is feasible in the prediction of 29 carbon prices, denoted as EMD-ARIMA-IMF₁-ADD and EMD-LSSVM-IMF₁-ADD models respectively. The study 30 adopts the well-established evaluation criteria, including level forecasting, directional prediction, the Diebold-Mariano 31 (DM) test, the Rate test, and trading performances including the Annualized return, Annualized volatility and 32 Information ratio, to assess the robustness of the proposed EMD-LSSVR-ADD model.

The paper is organized as follows. Section 2 describes the EMD, LSSVR, and the proposed models. Section 3
 reports the empirical analysis, and Section 4 concludes the study.

35 **2. Methodology**

36 2.1 EMD

37 EMD can decompose a carbon price into several IMFs and one residue by its local feature scales, as follows:

38 Step 1: Find out the local extreme points of carbon price x(t);

- 39 Step 2: Shape the upper and lower envelopes, $e_{max}(t)$ and $e_{min}(t)$, respectively;
- 40 Step 3: Obtain the mean of $e_{\max}(t)$ and $e_{\min}(t)$:
- 41

$$a(t) = \left[e_{\max}(t) + e_{\min}(t)\right] / 2$$

Step 4: Get the difference between x(t) and a(t):

$$d(t) = x(t) - a(t)$$

3 Step 5: Check d(t). When d(t) cannot meet the two conditions of IMF, let x(t) = d(t), return to the step 1, 4 and cannot repeat unless d(t) meets the two conditions. Otherwise, d(t) is defined as an IMF, and let the residue 5 r(t) = x(t) - d(t);

6 Step 6: Perform the steps 1-5 only when the termination criterion is met. EMD cannot stop unless σ(t) < θ₁
7 for a prescribed fraction (1-α) and σ(t) < θ₂ for the remaining fraction, where θ₁ and θ₂ are two thresholds
8 aimed to ensure mean globally small changes while locally big excursions.

9 In this study, we use the termination criterion by Rilling *et al.* [29], in which $\alpha = 0.05$, $\theta_1 = 0.05$, and $\theta_2 = 0.5$

10 Finally, we can obtain: $X(t) = \sum_{i=1}^{m} IMF_i(t) + R_m(t)$, where *m* is the number of IMFs, and $R_m(t)$ is the final residue.

11 2.2 LSSVR

12 For data $\{x_i, y_i\}, i = 1, 2, \dots, n$, LSSVR is defined as [27]:

13
$$\min\left\{\frac{1}{2}\|\omega\|^2 + \frac{1}{2}C\sum_{i=1}^n \xi_i^2\right\}$$

15 in which ω : the weight vector, C: the penalty parameter, ξ_i : the error, φ : mapping function, and b : the bias.

s.t. $y_i = \omega \cdot \varphi(x_i) + b + e_i, i = 1, 2, \dots, n$

16 The Lagrange function is used to find out the solutions for ω and ξ_i :

17
$$L(\omega, b, \xi, \alpha) = \frac{1}{2} \|\omega\|^2 + \frac{1}{2} C \sum_{i=1}^n \xi_i^2 - \sum_{i=1}^n \alpha_i \{\omega \cdot \varphi(x_i) + b + \xi_i - y_i\}$$

18 in which $\{\alpha_i, i = 1, 2, \dots, n\}$ are a set of Lagrange multipliers. The optimal solutions are obtained from:

19
$$\begin{cases} \frac{\partial L}{\partial \omega} = 0 \rightarrow \omega = \sum_{i=1}^{n} \alpha_{i} \varphi(x_{i}) \\ \frac{\partial L}{\partial \omega} = 0 \rightarrow \sum_{i=1}^{n} \alpha_{i} = 0 \\ \frac{\partial L}{\partial e_{i}} = 0 \rightarrow \alpha_{i} = Ce_{i} \\ \frac{\partial L}{\partial \alpha_{i}} = 0 \rightarrow \omega \cdot \varphi(x_{i}) + b + e_{i} - y_{i} = 0 \end{cases}$$

20

Using the least squares method to resolve the linear equations, LSSVR can be obtained as: $y(x) = \sum_{i=1}^{n} \alpha_i K(x, x_i) + b$,

21 in which the kernel function, $K(x, x_i) = \varphi(x) \cdot \varphi(x_i)$, fulfills the Mercer's principle.

22 2.3 Hybriding LSSVR and PSO for carbon price forecasting

The model selection of LSSVR is concerned with two key issues [29,30]: how to select an appropriate kernel function, and how to determine the optimal parameters of LSSVR. For the former, radial basis function (RBF), $K(x, y) = \exp(-||x - y||^2 / 2\sigma^2)$, is selected to build the LSSVR model, because RBF can yield good results in general [31]. For the latter, we use the PSO algorithm [32] to seek the optimal parameters (*C* and σ) of LSSVR. In the modeling of PSO, $x_i = (x_{i1}, x_{i2}, \dots, x_{iM})$ and $v_i = (v_{i1}, v_{i2}, \dots, v_{iM})$ are respectively defined as the position and velocity of particle *i*, *i* = 1,2, ..., *m*. $p_{best} = (p_{i1}, p_{i2}, \dots, p_{iM})$ and $g_{best} = (p_{g1}, p_{g2}, \dots, p_{gM})$ are respectively 1 defined as the optimum positions of particle *i* and *m* particles at the current iteration. x_i and v_i of each particle are 2 updated as:

3

$$x_{ii}(t+1) = \begin{cases} -p_{\max}, & x_{ii} < -p_{\max} \\ x_{ii}(t) + v_{ii}(t+1), & -p_{\max} \le x_{ii} \le p_{\max} \\ p_{\max}, & x_{ii} > p_{\max} \end{cases}$$
(1)

4
$$v_{id}(t+1) = \begin{cases} -v_{max}, & v_{id} < -v_{max} \\ w(t) \cdot v_{id}(t) + c_1 \cdot r_1 \cdot [p_{id}(t) - x_{id}(t)] + c_2 \cdot r_2 \cdot [p_{gd}(t) - x_{id}(t)], & -v_{max} \le v_{id} \le v_{max} \\ v_{max}, & v_{id} > v_{max} \end{cases}$$
(2)

5 where $1 \le i \le m$, $1 \le d \le M$, $x_{ii}(t)$ and $v_{id}(t)$ are respectively the position and velocity of particle *i* at iteration *t*, 6 p_{id} is the optimal position of particle *i* at iteration *t*, p_{gd} is the global optimal position, and *w* is the inertia weight, 7 defined as:

8
$$w(t) = w_{\max} - \frac{w_{\max} - w_{\min}}{t_{\max}} \times t$$
(3)

9 where, w_{max} and w_{nin} are respectively the maximal and minimal inertia weights.

10 The study introduces the PSO algorithm to seek the optimal parameters (C and σ) of LSSVR, in order to 11 improve searching efficiency and prediction accuracy [10], as presented in Fig. 1.

12 13

Insert Figure 1

14

Step 1: set up the training and test sets. The carbon price data is divided into a training set and a test set. The former is used for establishing the model, and the latter is used to test the forecasting performance of the proposed model.

18 Step 2: initialization. Randomly generating *m* particles with coding *C* and σ by real values, and setting the 19 parameters of PSO: maximal iterations t_{\max} , maximal position p_{\max} , maximal velocity v_{\max} , $w \in [w_{\min}, w_{\max}]$, 20 acceleration coefficients c_1 and c_2 , $C \in [C_{\min}, C_{\max}]$, $\sigma \in [\sigma_{\min}, \sigma_{\max}]$. Let t = 0, and training begins.

21 Step 3: selecting the root mean square error (RMSE) as the fitness function:

22
$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \hat{x}_i)^2}$$
(4)

23 in which *n* is the number of training sample, x_i and \hat{x}_i are the real and predicted values.

Step 4: evaluating the fitness. Calculating the fitness value of each particle by Eq. (4), and obtain p_{best} and g_{best} at the current generation.

26 Step 5: updating the position and velocity of each particle by Eqs. (1)–(3).

Step 6: Checking the end condition. When the end condition, the maximum iterations here, is satisfied, the
optimization process ends, and the optimal parameters are obtained to build the LSSVR. If not, move to step 7.

29 Step 7: Let t = t+1, and return to the step 4.

30 2.4 The proposed EMD-based LSSVR model for carbon price forecasting

For the carbon price x_t $(t = 1, 2, \dots, T)$, a *h*-step forecasting in advance, \hat{x}_{t+h} , can be expressed as

32
$$\hat{x}_{t+h} = f(x_t, x_{t-1}, \dots, x_{t-m+1})$$

1	where x_t , \hat{x}_t and <i>m</i> are the real, predicted values, and lag order respectively.
2	As shown in Fig. 2, we propose an EMD-based LSSVR model (EMD-LSSVR-ADD) for carbon price forecasting,
3	generally comprised of the subsequent three key steps:
4	Step 1: Each carbon price is decomposed into a batch of IMFs and one residue with high stability and regularity
5	via EMD.
6	Step2: LSSVR is employed in forecasting the IMFs and residue respectively, so as to obtain their forecasted
7	values.
8	Step 3: The forecasted values of all the IMFs and residues are aggregated into the final predicted values of the
9	original carbon price.
10	In short, the proposed EMD-LSSVR-ADD is in essence an EMD (multiscale decomposition)-LSSVR (component
11	forecast)-ADD (multiscale ensemble forecast) model, which is a utilization of "decomposition and ensemble" tactics
12	[11,34]. In the next section, four carbon futures prices are used for testing the robustness of the proposed multiscale
13	prediction approach.
14	Insert Figure 2
15	
16	
17	3. Empirical analysis
18	3.1 Data
19	As the biggest carbon trading market in the EU ETS, the European Climate Exchange (ECX) is an indicator of the
20	global carbon markets. Four futures prices matured in Decembers of 2013, 2014, 2015 and 2016 (denoted as DEC13,
21	DEC14, DEC15 and DEC16 respectively) are selected as empirical samples. The daily data has been collected in
22	Euros/ton (excluding public holidays from April 2008 to October 2016). For the convenience of modeling, the samples
23	are divided into two subsets: the training set and the testing set. The training set is used to establish prediction models,
24	and the testing set is employed to test the robustness of the established models. The divided samples of carbon prices
25	are reported in Table 1. The data used are obtained from the website of ECX (http://www.theice.com).
26	
27	Insert Table 1
28	
29	3.2 Evaluation criteria
30	Forecasting performance is measured by two main criteria: level forecasting and directional prediction. Level
31	forecasting is measured via the root mean squared error (RMSE):
32	$RMSE = \sqrt{\frac{1}{n} \sum_{t=1}^{n} [\hat{x}(t) - x(t)]^2}$
33	On the other hand, directional prediction is measured with the directional prediction statistic (D_{stat}) [10, 36]:
34	$D_{stat} = \frac{1}{n} \sum_{t=1}^{n} a_t \times 100\%$
35	$a_{t} = \begin{cases} 1, & if[x(t+1) - x(t)][(\hat{x}(t+1) - x(t)] \ge 0\\ 0, & otherwise \end{cases}$

36 where $\hat{x}(t)$ and x(t) are the real and predicted values respectively, and *n* is the number of test samples.

37 The DM test is further used to statistically contrast the predicted performances of various predictive models [37].

1 In this study, mean square prediction error (MSPE) is chosen as the loss function. Thus, the DM statistic is defined as

$$DM = \frac{d}{\sqrt{\hat{V}_{\bar{d}} / T}} \sim N(0, 1), \quad T \to \infty$$

3 where
$$\overline{d} = \frac{1}{T} \sum_{t=1}^{T} \left[g(e_{te,t}) - g(e_{re,t}) \right]$$
, $g(e_{te,t}) = \sum_{t=1}^{T} e_{te,t}^2$, $g(e_{re,t}) = \sum_{t=1}^{T} e_{re,t}^2$, $e_{te,t} = x_t - \hat{x}_{te,t}$, $e_{re,t} = x_t - \hat{x}_{re,t}$,

4 $\hat{V}_{d} = \gamma_0 + 2\sum_{j=1}^{\infty} \gamma_j$, and $\gamma_j = \operatorname{cov}(d_t, d_{t-j})$. $\hat{x}_{te,t}$ and $\hat{x}_{re,t}$ denote the forecasted values of x_t calculated using the test 5 model (*te*) and reference model (*re*) at time *t*, respectively. A one-tailed test is generally employed in evaluating the DM 6 statistic. In the DM test, the null hypothesis, i.e. the tested model is not worse than the reference model, is tested.

Therefore, only if p is lower than a frequently-used level of significance 0.05, we should reject it; otherwise, we should accept it.

The statistics of RT test is expressed as

2

9

10

$$Z_{RT} = \frac{p_A - p_B}{\sqrt{\frac{p_A(1 - p_A)}{n} + \frac{p_B(1 - p_B)}{n}}} \sim N(0, 1), \ n \to \infty$$

where p_A and p_B are respectively the accuracies of directional prediction of models A and B. The null hypothesis of RT test is that the accuracies of directional prediction of models A and B are the same. Using the two-sided test, when the absolute value of z_{RT} exceeds 1.96, the null hypothesis is rejected at the significance level of 5%.

A good statistical accuracy does not always mean a good trading performance. For investors, they usually care more about a model's practicability in trading. In this section, inspired by Sermpinis et al.(2016) [37], we design a pseudo trading strategy to test the trading performance as an investor chooses to buy or sell (or stay watching) carbon assets when the forecasted return is above or below (or equal) zero at the current carbon price respectively in real market. This can illustrate our model's application value of making production and investment more profit. We use the Annualized return, Annualized volatility and Information ratio to evaluate the trading performance. They defined as:

21 Daily return:
$$R_t = \frac{P_t - P_{t-1}}{P_{t-1}}$$

22 Annualized return:
$$R^A = 252 * \frac{1}{k} * \sum_{t=1}^n R_t$$

23
Annualized volatility:
$$\sigma^{A} = \sqrt{252} * \sqrt{\frac{1}{k-1} * \sum_{t}^{k} (R^{t} - R^{m})}$$

24
Information ratio: $IR = \frac{R^{A}}{\sigma^{A}}$

where, P_t is daily price of carbon future; k is the number of test set and R^m is mean value of R^t .

In order to evaluate the predictive performance of proposed EMD–LSSVR–ADD model with other popular forecasting models, the study compares its outputs with the outputs of the single ARIMA and LSSVR models, a hybrid ARIMA+LSSVR model, variants of the EMD–ARIMA–ADD model, EMD–ARIMA–IMF₁–ADD and EMD–LSSVM– IMF₁–ADD models. In the variant of the EMD–ARIMA–ADD model, all the IMFs and residues extracted by EMD are independently forecasted by the ARIMA model, and the predicted values are summed into the final predicted ones of the original carbon price.

32 3.3 Results and discussions

Forecasting experiments are carried out in terms of the steps outlined in the previous section. We set the thresholds and tolerance as $[\theta_1, \theta_2, \alpha] = [0.05, 0.5, 0.05]$ [29], and the decomposition results via EMD are reported in Fig.3. It is evident that DEC13, DEC14, DEC15 and DEC16 tend to be non-stationary and nonlinear due to the fact that their means change over time. DEC13, DEC14 and DEC15 are respectively disassembled into seven IMFs and one residue, while DEC16 is disassembled into six IMFs and one residue. At the same time, all the IMFs and residues have a higher stability and stronger regularity compared with the original series.

Insert Figure 3

a
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10 We apply the one shot testing method [38], in which one single model applies over all test period. Thus, we apply 11 the fixed time window to train the models by the training set, and forecast the testing set by the trained models. 12 Meantime, we perform the one-step-ahead forecasting for DEC13 to DEC16. - EViews developed by Quantitative 13 Micro Software is used for ARIMA modeling. The optimum model is found via the Akaike information criterion. By 14 trial and error, both the best models derived from DEC14 to DEC16 are ARIMA (2,1,0) models, while the best models 15 for DEC13 is ARIMA (1,1,1) model. Moreover, as previously mentioned, ARIMA is also used to model each IMF and 16 residue decomposed by EMD. The predicted values of all IMFs and residues are then aggregated into the predicted 17 values of EMD-ARIMA-ADD model.

All the LSSVR models are built by the LSSVMlab by Suykens and his colleagues on the platform of MATLAB 2016b. The input of each LSSVR model is determined using a partial autocorrelation function method [16]. The optimal parameters are searched with 100 particles and 5 generations. $C \in [1,1000], \sigma \in (0,50], c_1 = c_2 = 2, w_{max} = 0.9,$ $w_{min} = 0.1, p_{max} = 0.05$, and $v_{max} = 50$. Moreover, as mentioned above, LSSVR is also used to forecast each IMF and residue decomposed via EMD, and the predicted values of all IMFs and residues are aggregated into the forecasted values of EMD-LSSVR-ADD model.

24 The hybrid ARIMA+LSSVR model is built as discussed above, the predicted values of the original carbon price by 25 ARIMA and LSSVR models are equally weighted sum of the final predicted ones of carbon prices. Consequently, 26 Inspired by Tang et al. (2012)[18], Guo et al. (2012)[28], Zhu and Wei,(2013)[10] and Yu et al. (2015)[39], two single models (LSSVR and ARIMA), a hybrid ARIMA+LSSVR model, and four multiscale forecasting models (EMD-27 28 ARIMA-IMF1-ADD, EMD-ARIMA-ADD, EMD-LSSVR-IMF1-ADD and EMD-LSSVR-ADD) are applied to 29 forecast carbon prices. The results of RMSE and D_{stat} for the different models are shown in Table 2. The DM and RT 30 test results are listed in Tables 3 and 4. Furthermore, the comparison of the trading performances is concluded in Table 31 5. The out-of-sample forecasted results for DEC13, DEC14, DEC15 and DEC16 by the proposed 32 EMD-LSSVR-ADD are presented in Fig.4.

33	Insert Table 2
34	Insert Table 3
35	Insert Table4
36	Insert Table 5

- 37
- 38

From the perspective of level forecasting measured by RMSE, it can be found that, firstly, the prediction accuracy

of LSSVR model is superior to that of ARIMA model for its strong nonlinear approximation ability and excellent 1 2 self-learning ability. Meanwhile, the optimization of PSO improves the learning and prediction abilities of LSSVM. The hybrid process of ARIMA and LSSVR models only improves the predication accuracy slightly here. Secondly, all the 3 multiscale ensemble prediction models including EMD-ARIMA-IMF1-ADD, EMD-ARIMA-ADD, EMD-LSSVR-4 5 IMF₁-ADD and EMD-LSSVR-ADD obviously outperform each single prediction models such as ARIMA, LSSVR 6 and their hybrid model. The main reason is that after EMD decomposition, both LSSVR and ARIMA can effectively 7 forecast the simple and stable components so as to significantly improve the prediction accuracy. Thirdly, among the multiscale ensemble prediction models, the EMD-LSSVR-ADD and EMD-ARIMA-ADD show better results than 8 9 EMD-LSSVR-IMF₁-ADD and EMD-ARIMA-IMF₁-ADD, which differs from the conclusion of Guo et al.(2012) and 10 shows the necessity to take all the IMFs into consideration when forecasting carbon prices. Last but not least, the result 11 of EMD-LSSVR-ADD is superior to that of EMD-ARIMA-ADD, which shows the strong predictive power of the proposed EMD-LSSVR-ADD model. Comparing all models here, the highest level of accuracy achieved by the 12 13 proposed EMD-LSSVR-ADD model implies the advantage of "decomposition and ensemble" principle.

In terms of the level of directional prediction, the results of D_{stat} are similar in terms of RMSE. The models established via EMD decomposition and LSSVR show higher accuracy in directional prediction. Therefore, the proposed EMD–LSSVR–ADD model achieves the highest value of D_{stat} (or at least as high as) compared with other models in the contracts from DEC13, DEC14, DEC15 and DEC16. Concerning the improvement level of directional prediction, EMD makes the largest contribution. Due to the significant advantages of EMD, LSSVR just produces a less progress than ARIMA here.

20 Two findings are derived from the DM test results. Firstly, all the multiscale ensemble prediction models 21 remarkably outperform than single scale models at the significance level of 5%. There is no obvious difference between 22 ARIMA, LSSVM and hybrid models in level prediction. This confirms the power of EMD for capturing different 23 characteristics of carbon prices. Secondly, in general, the proposed EMD-LSSVR-ADD model is significantly superior 24 to EMD-ARIMA-IMF₁-ADD and EMD-LSSVR-IMF₁-ADD models, but it has no obvious advantage compared with 25 EMD-ARIMA-ADD model except for DEC15. Furthermore, the RT test reveals the similar results as the DM test, i.e. 26 the multiscale ensemble models can obtain high accuracy of directional prediction at the confidence level of 5% for all 27 carbon prices. Although the proposed EMD-LSSVR-ADD model has the highest accuracy from D_{stat}, it does not show 28 significant differences from other multiscale ensemble models in accuracy for direction.

In terms of the trading performance, the proposed EMD–LSSVR–ADD model produces the best trading performances in all the carbon prices for its highest Annualized return and smallest Annualized volatility. This implies that our proposed EMD–LSSVR–ADD model is capable of achieving good trading gains, and also suggests the advantages of EMD over single scale models.

33 To sum up, we can draw a few conclusions from the empirical analysis results: (1) in terms of level prediction, 34 directional forecasting, the DM test, and the RT test, compared with ARIMA, LSSVR, ARIMA+LSSVR, EMD-ARIMA-IMF1-ADD, EMD-ARIMA-ADD and EMD-LSSVR-IMF1-ADD models, our proposed EMD-LSSVR-35 36 ADD model can obtain better statistical and trading performances; (2), four multiscale ensemble models can achieve 37 more precise prediction results than ARIMA, LSSVR, and ARIMA+LSSVR models, implying that "decomposition and 38 ensemble" tactics can significantly enhance predictive capability; (3) the nonlinear approach (LSSVR) is more 39 appropriate to forecast carbon prices than the linear model (ARIMA). Therefore, the proposed EMD-based LSSVR 40 model is a promising approach for carbon price forecasting.

41 42

Insert Figure 4

4. Conclusions and future work

3 In this study, we propose a new empirical mode decomposition-based evolutionary least squares support vector 4 regression for carbon price forecasting. This model use empirical mode decomposition to disassemble each carbon price 5 into a batch of more stationary and more regular components, which can be easily forecasted by the particle swarm optimization-based evolutionary least squares support vector regression. The final forecasted values of carbon prices are 6 7 obtained via aggregating the forecasted values of all the components. Finally, using four carbon futures prices from the 8 European Union Emissions Trading Scheme as samples, the proposed empirical mode decomposition-based 9 evolutionary least squares support vector regression has been empirically tested, and its predictive performance has been 10 compared with the predictive performance of single, hybrid and variational multiscale forecasting models, in terms of 11 statistical measures and trading performances. The empirical results suggest that the proposed model can yield the 12 optimal statistical measures. Moreover, the proposed model shows great trading performance as well, which indicates 13 its value in practice. Our main future work is (1) to improve the accuracy of empirical mode decomposition, (2) to build 14 the best forecasting for each component in terms of their own characteristics, and (3) to explore the nonlinear ensemble 15 of all the components. Through these efforts, the accuracy of high non-stationary and nonlinear carbon price forecasting 16 is expected to be further improved. Furthermore, Based on the proposed model, how to develop an intelligent 17 forecasting and trading decision support system for carbon market so as to make production and investment a maximum 18 profit is also our another next work.

19 20

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- 25 26

Appendix A

Abbreviations: EMD, empirical mode decomposition; LSSVR, least squares support vector regression; IMF,
 intrinsic mode function; PSO, particle swarm optimization; EU ETS, European Union Emissions Trading System;
 GARCH, generalized autoregressive conditional heteroscedasticity; ANN, artificial neural networks; ARIMA,
 autoregressive integrated moving average; RBF, radial basis function; ECX, European Climate Exchange; RMSE, root

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- 31 mean squared error; D_{stat} directional prediction statistic; DM, Diebold–Mariano; RT, Rate test.
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1 Figures

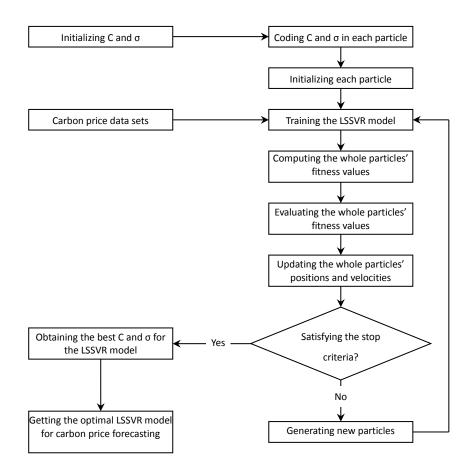
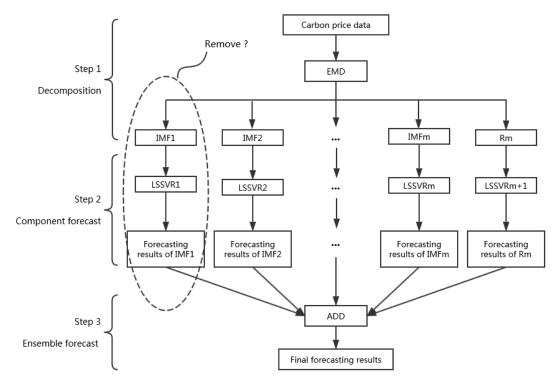


Fig. 1. The process of model selection for LSSVR using PSO.



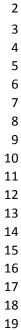
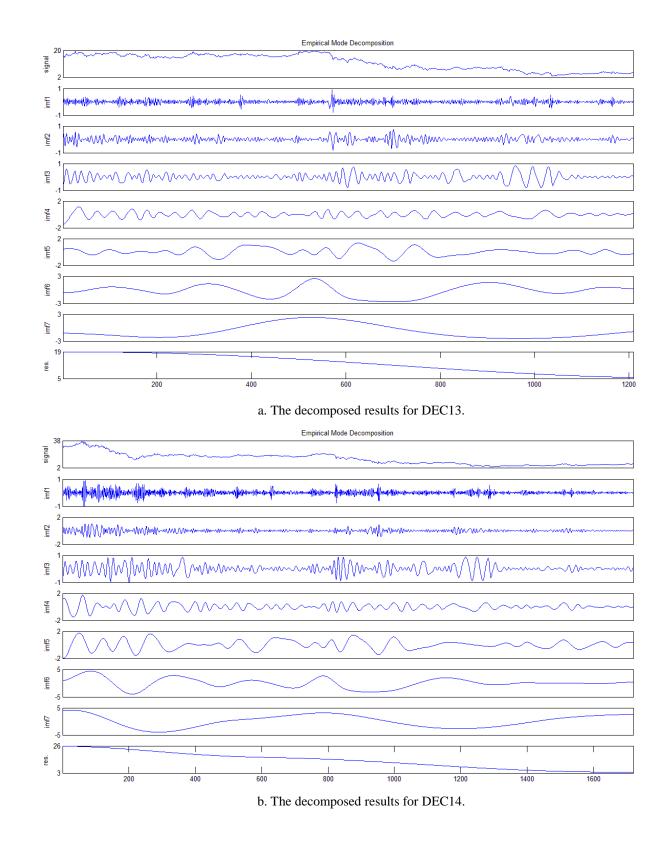
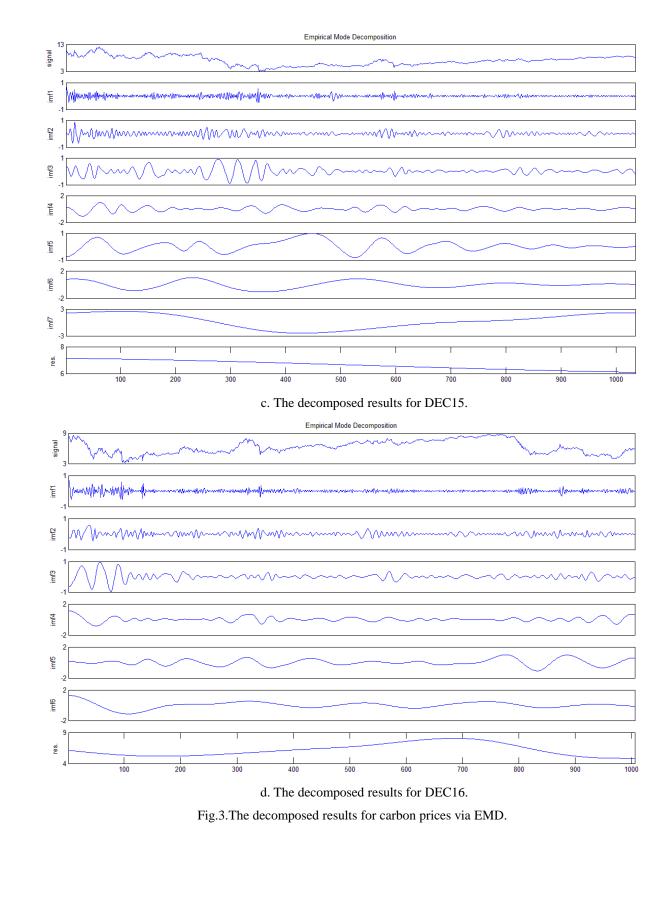
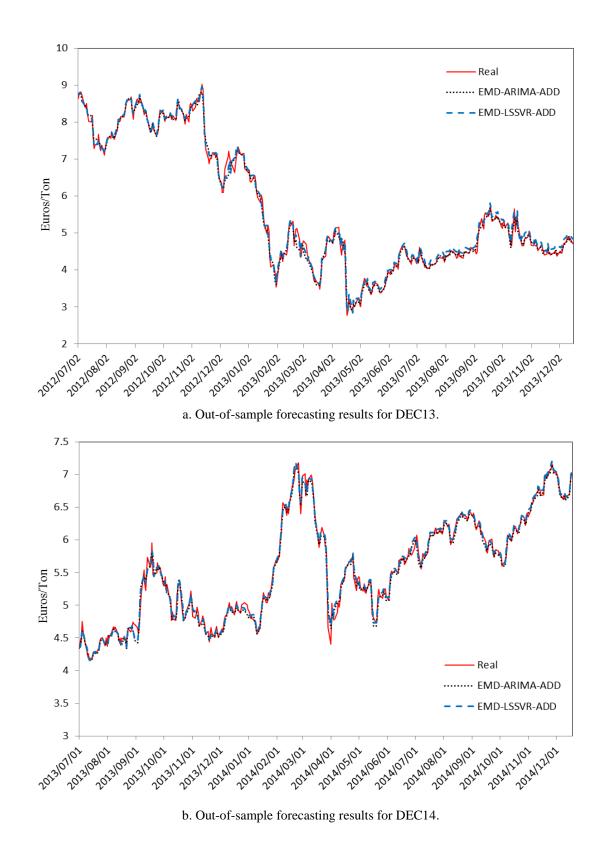


Fig. 2. The framework for the proposed multiscale prediction methodology.

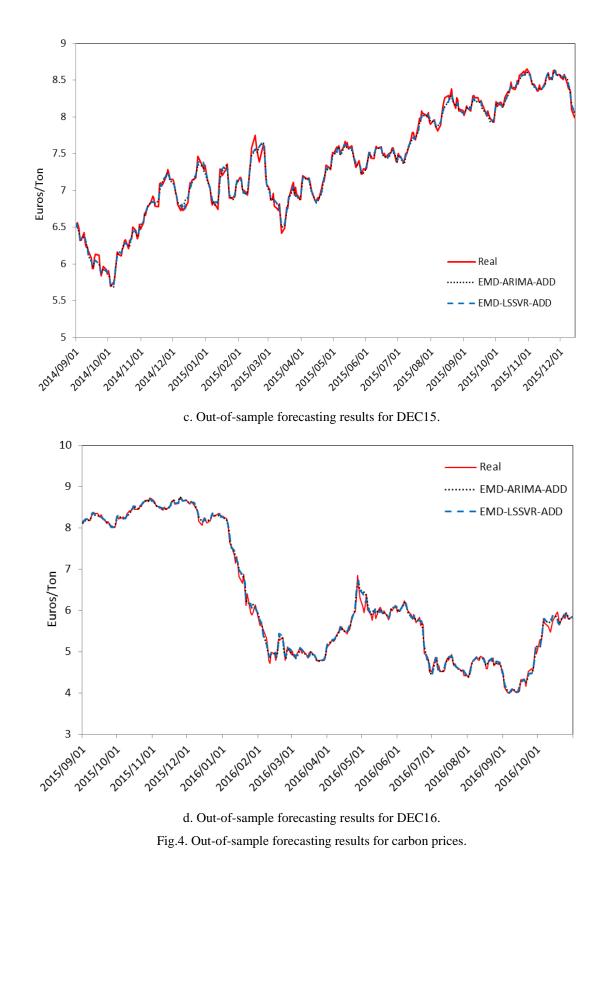












2 Tables

Table 1. Samples of carbon prices

Carbon price		Size	ze Date		
	Sample set	1209	1 April 2009 - 16 December 2013		
DEC13	Training set	833	1 April 2009 - 29 June 2012		
	Testing set	376	2 July 2012 - 16 December 2013		
	Sample set	1719	8 April 2008 - 18 December 2014		
DEC14	Training set	1340	8 April 2008 - 28 June 2013		
	Testing set	379	1 July 2013 - 18 December 2014		
	Sample set	1035	29 November 2011 - 14 December 2015		
DEC15	Training set	704	29 November 2011 - 29 August 2014		
	Testing set	331	1 September 2014 - 14 December 2015		
	Sample set	1006	27 November 2012 - 31 October 2016		
DEC16	Training set	705	27 November 2012 - 31 August 2015		
	Testing set	301	1 September 2015 - 31 October 2016		

Table 2 Out-of –sample comparisons of the RMSE and the D_{stat} of each prediction model

Ма	dala	ARIMA	LSSVM	II. haid	EMD-ARIMA-	EMD-ARIMA-	EMD-LSSVR-	EMD-LSSVR-
Models		AKIMA	LSSVM	Hybrid	IMF ₁ -ADD	ADD	IMF ₁ -ADD	ADD
	DEC13	0.211	0.209	0.206	0.127	0.126	0.139	0.125
RMSE	DEC14	0.142	0.141	0.141	0.080	0.073	0.081	0.072
KINISE	DEC15	0.091	0.091	0.090	0.055	0.050	0.053	0.047
	DEC16	0.142	0.142	0.141	0.082	0.079	0.085	0.077
	DEC13	66.22	62.50	57.71	79.52	80.05	72.87	79.79
D	DEC14	55.41	61.48	59.10	83.91	86.02	83.91	87.34
D _{stat}	DEC15	74.62	69.49	72.21	80.36	83.69	84.29	84.89
	DEC16	68.44	60.80	69.10	83.06	87.38	83.06	86.71

					Reference model				
	Test model	ARIMA	LOOVA		EMD-ARIMA-	EMD-ARIMA-	EMD-LSSVR		
			LSSVM	Hybrid	IMF ₁ -ADD	ADD	IMF ₁ -ADD		
	LSSVM	0.8276							
	Hybrid	0.2558	0.2250						
DEC13	EMD-ARIMA-IMF1-ADD	0.0000 *	0.0000*	0.0000 *					
DEC15	EMD-ARIMA-ADD	* 0.0000	0.0000 *	0.0000 *	0.7428				
	EMD-LSSVR-IMF ₁ -ADD	0.0000 *	0.0000 *	0.0001 *	0.0069*	0.0222*			
	EMD-LSSVR-ADD	0.0000 *	0.0000 *	0.0000 *	0.6718	0.8389	0.0004 *		
	LSSVM	0.5796							
	Hybrid	0.4803	0.7311						
	EMD-ARIMA-IMF1-ADD	0.0000 *	0.0000*	0.0000 *					
DEC14	EMD-ARIMA-ADD	0.0000 *	0.0000 *	0.0000 *	0.0128 *				
	EMD-LSSVR-IMF ₁ -ADD	0.0000 *	0.0000 *	0.0000 *	0.4789	0.0119 *			
	EMD-LSSVR-ADD	0.0000 *	0.0000 *	0.0000 *	0.0079 *	0.4791	0.0005 *		
	LSSVM	0.7598							
	Hybrid	0.2193	0.1131						
	EMD-ARIMA-IMF1-ADD	0.0000 *	0.0000 *	0.0000 *					
DEC15	EMD-ARIMA-ADD	* 0.0000	0.0000 *	0.0000 *	0.0000 *				
	EMD-LSSVR-IMF ₁ -ADD	0.0000 *	0.0000 *	0.0000 *	0.0443 *	0.0164 *			
	EMD-LSSVR-ADD	0.0000 *	0.0000 *	0.0000 *	0.0000 *	0.0137 *	0.0000 *		
	LSSVM	0.8957							
	Hybrid	0.2819	0.4421						
DECL	EMD-ARIMA-IMF1-ADD	0.0000 *	0.0000 *	0.0000 *					
DEC16	EMD-ARIMA-ADD	* 0.0000	0.0000 *	0.0000 *	0.5032				
	EMD-LSSVR-IMF ₁ -ADD	* 0.0000	0.0000 *	0.0000 *	0.0225 *	0.2506			
	EMD-LSSVR-ADD	0.0000 *	0.0000 *	0.0000 *	0.0865	0.4930	0.0175 *		
	s table reports the P-values of	of DM test.	* denotes	that the nu	ull hypothesis is	rejected at the s	ignificant lev		
5%.									

Table 3 Out-of -sample comparisons of DM test of each prediction model

Reference model Test model EMD-ARIMA-EMD-ARIMA-EMD-LSSVR-ARIMA LSSVM Hybrid IMF₁-ADD ADD IMF₁-ADD LSSVM 0.2872 0.0163 * Hybrid 0.1801 EMD-ARIMA-IMF₁-ADD * 00000 * 0.0000 0.0000 * DEC13 EMD-ARIMA-ADD * 00000 0.0000 * * 0.0000 0.8565 EMD-LSSVR-IMF1-ADD 0.0477 * 0.0024 * 0.0000 * 0.0324 * 0.0204 * EMD-LSSVR-ADD * 0000.0 0.9291 0.0000 * * 0.0000 0.9268 0.0257 * LSSVM 0.0902 Hybrid 0.3048 0.5034 EMD-ARIMA-IMF1-ADD * 0000.0 * 0.0000 0.0000 * DEC14 EMD-ARIMA-ADD * 0000.0 0.0000 * * 0.0000 0.4167 EMD-LSSVR-IMF1-ADD * 00000 0.0000 * 1.0000 * 0.4167 0.0000 * EMD-LSSVR-ADD * 00000 0.0000 * * 00000 0.1786 0.5931 0.1786 LSSVM 0.1417 Hybrid 0.4831 0.4417 EMD-ARIMA-IMF1-ADD 0.0773 0.0013 * 0.0138 * DEC15 0.0041 * * 0.0000 EMD-ARIMA-ADD 0.0004 * 0.2649 EMD-LSSVR-IMF1-ADD 0.0021 * 0.0000 * 0.0002 * 0.1854 0.8334 EMD-LSSVR-ADD 0.0010 * 0.0000 * 0.0001 * 0.6716 0.8308 0.1243 LSSVM 0.0502 Hybrid 0.8614 0.0330 * * 00000 * 0.0000 EMD-ARIMA-IMF1-ADD 0.0001 * DEC16 EMD-ARIMA-ADD * 0.0000 * 0.0000 * 0.0000 0.1357 EMD-LSSVR-IMF₁-ADD * 0.0000 * 0.0000 0.0001 * 1.0000 0.1357 EMD-LSSVR-ADD * 0.0000 * 0.0000 * 0.0000 0.2116 0.8068 0.2116 Note: This table reports the P-values of Rate test. * denotes that the null hypothesis is rejected at the significant level of 5%.

Table 4 Out-of –sample	comparisons of Rate	test of each prediction mode	1

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Table 5 Out-of -sample comparisons of trading performances of each prediction model

			1	•	01			
Trading performances		ARIMA	LSSVM	Hybrid	EMD-ARIMA- IMF ₁ -ADD	EMD-ARIMA- ADD	EMD-LSSVR- IMF ₁ -ADD	EMD-LSSVR- ADD
	Annualized return(%)	-15.25	50.59	69.44	584.38	587.51	573.73	593.99
DEC13	Annualized volatility(%)	57.11	63.99	64.7	55.04	55.16	55.87	54.9
	Information ratio	-0.27	0.79	1.07	10.62	10.65	10.27	10.82
	Annualized return(%)	4.39	21.73	10.3	385.71	402.26	385.06	417.63
DEC14	Annualized volatility(%)	39.24	37.3	36.17	33.8	32.92	33.84	32.42
	Information ratio	0.11	0.58	0.28	11.41	12.22	11.38	12.88
	Annualized return(%)	56.28	40.15	51.99	194.27	206.55	203.93	211.6
DEC15	Annualized volatility(%)	17.48	17.11	17.51	16.64	16.05	15.85	15.75
	Information ratio	3.22	2.35	2.97	11.67	12.87	12.87	13.43
	Annualized return(%)	71	52.14	83.35	368.31	385.38	363.39	395
DEC16	Annualized volatility(%)	36.6	35.12	37.37	32.81	32.28	33.27	31.95
	Information ratio	1.94	1.48	2.23	11.23	11.94	10.92	12.36