Coulomb dissociation of $^{20,21}\text{N}$


(R3B Collaboration)
1Helmholtz-Zentrum Dresden-Rossendorf, Dresden, Germany
2Technische Universität Dresden, Dresden, Germany
3KVI-CART, University of Groningen, Groningen, The Netherlands
4GSI Helmholtzzentrum für Schwerionenforschung Darmstadt, Darmstadt, Germany
5University of Santiago de Compostela, Santiago de Compostela, Galicia, Spain
6Goethe University Frankfurt, Frankfurt, Germany
7School of Physics and Astronomy, University of Birmingham, Birmingham, United Kingdom
8Technische Universität Darmstadt, Darmstadt, Germany
9Lund University, Lund, Sweden
10Texas A&M University-Commerce, Commerce, Texas, USA
11IEM CSIC, Madrid, Spain
12GANIL, Caen, France
13Universidad de Vigo, Vigo, Galicia, Spain
14University of Surrey, Guildford, Surrey, United Kingdom
15SINP, Kolkata, India
16University of Liverpool, Liverpool, United Kingdom
17NRC Kurchatov Institute, Moscow, Russia
18Instituto Superior Técnico, University of Lisbon, Lisboa, 1049-001 Lisboa, Portugal
19MTA Atomki, Debrecen, Hungary
20Saint Mary’s University, Halifax, Nova Scotia, Canada
21Universidad Complutense de Madrid, Madrid, Spain
22University of Aarhus, Aarhus, Denmark
23Centro de Física Nuclear da Universidade de Lisboa, Lisboa, Portugal
24Technische Universität München, München, Germany
25Chalmers University of Technology, Gothenburg, Sweden
26Saint Mary University, Halifax, Nova Scotia, Canada
27STFC Daresbury Laboratory, Daresbury, United Kingdom
28Beihang University, Beijing, China
29University of Notre Dame, Notre Dame, Indiana, USA
Neutron-rich light nuclei and their reactions play an important role in the creation of chemical elements. Here, data from a Coulomb dissociation experiment on $^{20,21}$N are reported. Relativistic $^{20,21}$N ions impinging on a lead target and the Coulomb dissociation cross section was determined in a kinematically complete experiment. Using the detailed balance theorem, the $^{20}(n,\gamma)^{21}$N and $^{20}(n,\gamma)^{21}$N excitation functions and thermonuclear reaction rates have been determined. The $^{19}(n,\gamma)^{20}$N rate is up to a factor of 5 higher at $T < 1$ GK with respect to previous theoretical calculations, leading to a 10% decrease in the predicted fluorine abundance.

DOI: 10.1103/PhysRevC.93.065807

I. INTRODUCTION

The astrophysical $r$ process (rapid neutron capture process) is an important process for the synthesis of heavy elements [1]. The path of the $r$ process involves many neutron-rich nuclei. One possible astrophysical site for the $r$ process is supernovae with a neutrino-driven wind scenario [2] where the neutrino wind dissociates all previously formed nuclei into protons, neutrons, and alpha particles [3,4]. Nuclear reaction network calculations have shown that also light neutron-rich nuclei have an important impact on the final elemental abundance of the $r$-process nucleosynthesis [3,5]. As the half-lives of nuclei close to the neutron drip line are very short, no target material can be fabricated. Therefore, these nuclei have to be studied in beam, e.g. by exploiting the virtual gamma field of a lead target. The astrophysically important neutron capture reaction may, then, be studied by time inversion applying the principle of detailed balance [6].

In the S393 experiment at the LAND/R3B setup (Large Area Neutron Detector; Reactions with Relativistic Radioactive Beams) at GSI Darmstadt, Germany, many neutron-rich nuclei were provided in a cocktail beam. In this article, experimental results on the Coulomb dissociation cross sections of $^{20}$N and $^{21}$N are discussed. Data on neutron-rich boron, carbon, and oxygen isotopes from the S393 experiment have been presented elsewhere [7–10].

II. EXPERIMENTAL SETUP

A primary $^{40}$Ar beam with 490 MeV/u kinetic energy is guided onto a 4 g/cm$^2$ thick Be target placed at the entrance of the FRS (Fragment Separator) [11] producing a large variety of secondary ions in a cocktail beam. Thereafter, the secondary ions pass a separation stage consisting of bending magnets and a fixed beam line. As their beam trajectory is fixed by the magnetic rigidity $B\rho$, the secondary ions are separated with respect to their velocity according to their mass-to-charge ratio.

At the end of the FRS the secondary ions traverse a 3 mm thick plastic scintillator (called S8) at a distance of 55 m from the reaction target (mentioned later in detail). Additionally, the POS detector, a 1 mm thick plastic scintillator at the entrance of the LAND/R3B cave, is placed 1.45 m in front of the reaction target. Together, these detectors are used for time-of-flight measurements to identify the mass-to-charge ratio $A/Z$ of the secondary ions.

Besides that, a PSP detector (position-sensitive silicon PIN diode), placed 105 cm upstream of the reaction target, is used to determine the charge of the secondary ions by an energy loss measurement $dE/dx$, which completes the identification of the particles impinging onto the LAND/R3B setup. After a rough selection of the ion of interest, a Gaussian fit is applied to $A/Z$ and $dE/dx$ separately for each nucleus under study ($^{20}$N and $^{21}$N). All events within $3\sigma$ of the Gaussian fit are selected for further analysis (Fig. 1). Contamination due to detector resolutions and cuts are studied in Sec. III F.

Furthermore, an active slit detector (called ROLU) consisting of four movable plastic scintillator sheets (5 mm thickness), defining an empty rectangular window in the center, is utilized to define the accepted beam spot size. Ions that do not traverse through the central window of ROLU but hit the active part of the detector are not recorded.

Moreover, four DSSSDs (double sided silicon strip detectors) [12] were placed in the beam line, two in front of and two behind the reaction target, to measure the track of the impinging particles and of the charged reaction products leaving the target. A valid signal in all four DSSSDs is required for further analysis (see Sec. III A). Four additional DSSSDs placed in a box around the target to enable the detection of low energetic charged particles are not used for the present analysis.

Reaction targets with an area of $3 \times 3 \text{ cm}^2$ and a specific thickness $d$ [$d_{\text{Fe}} = (0.176 \pm 0.004) \text{ mm}, d_{\text{C}} = (5.08 \pm 0.10) \text{ mm}$] are mounted in a remotely controllable target wheel. The lead target is used to study the Coulomb dissociation, while the data measured with the carbon target are used to subtract the nuclear contribution. Measurements with no target are used to quantify the background contribution of the material in the beamline.

Around the reaction target, the Crystal Ball detector [13], consisting of 162 sodium iodine crystals arranged in a shell, is placed to detect $\gamma$ rays stemming from the deexcitation of excited states of the outgoing ions. The proton detection capability of the Crystal Ball was not needed for the present analysis.

Downstream at 260 cm from the reaction target, ALADIN (A Large Dipole Magnet) deflects charged particles according to their magnetic rigidity. At an angle of $15^\circ$ from the nominal beam axis, two GFI (Great Fibre) detectors [14,15] with an active area of $50 \times 50 \text{ cm}^2$ measure the $x$ position of

---

1d.bennmer@hzdr.de

1Present address: LIP-Lisboa, 1000-149 Lisboa, Portugal.

3Present address: Department of Physics, University of York, YO10 5DD York, United Kingdom.
FIG. 1. Incoming particle identification for the FRS setting used in this work. The charge number $Z$ is derived by energy loss measurements in the PSP and the $A/Z$ ratio by time-of-flight measurements between S8 and POS (55 m distance). The red rectangles indicate a $3\sigma$ cut for $^{20}\text{N}$ (left) and $^{21}\text{N}$ (right). For further details, see text.

The neutrons originating from Coulomb breakup reactions are unaffected by the magnetic field of ALADIN and impinge onto LAND (Large Area Neutron Detector) [16], a 2 m long, 2 m wide and 1 m thick device for detecting neutrons with kinetic energies between $T_n = 100$ and 1000 MeV, placed at a distance of 12.6 m from the reaction target. LAND consists of 10 crossing planes of 20 paddles each. Each paddle (10 cm thick) consists of consecutively 5 mm iron converter (to convert the neutrons into detectable charged particles) and 5 mm plastic scintillator sheets. Further details can be found elsewhere [16,17].

A sketch of the LAND/R3B setup as it was used for the S393 experiment is shown in Fig. 2. Although not needed for the present analysis, the proton detection capabilities are shown for completeness.

III. DATA ANALYSIS

In this section, the analysis of the recorded events is discussed. The identification of the incoming beam was already described in the previous section.

A. Selection of the reaction channel

After selecting the nuclei of interest during the incoming particle identification, we fix the charge number $Z$ of the outgoing heavy reaction fragment for the specific reaction channel ($Z = 7$) by a cut on the energy loss in the TFW. Then the deflection of the fragments in the magnetic field depends only on their mass number $A$ and their velocity.

In addition, the horizontal position measurement at the GFIs, used to identify the mass number of the fragment, is additionally correlated with the angle of emission and the interaction position at the target. In order to convert the horizontal position measurements of the charged fragments at

FIG. 2. Sketch (top view) of the detector setup at the LAND/R3B cave. Indicated are plastic scintillators (orange), the neutron flight path (blue line), the flight path of heavy ions (magenta line), and that of protons (red line). Distances of the detectors are to scale, while the thicknesses of the thin detectors are not to scale. See text for details.
FIG. 3. Doppler corrected gamma sum spectra for outgoing nuclei (red solid line) after Coulomb breakup and a background estimation (blue dashed line). Left panel for outgoing $^{19}$N and right panel for $^{20}$N. The black arrows indicate known excited states [18].

the GFIIs into mass numbers, a mass reconstruction algorithm using the trajectories and time-of-flight information is used.

A valid reaction event is defined for further analysis when each of the following conditions are fulfilled. Exactly one neutron is registered in LAND. Late neutron events, i.e., from scattered neutrons, are rejected by a cut on the neutron velocity $v_n > 20$ cm/ns as this reflects the velocity of the incoming ion. Exactly one outgoing $^{19}$N is detected in the fragment branch (both GFIIs, and TFW). In order to ensure the tracking of the incoming and outgoing particle, at least one hit in both planes of each of the four in-beam DSSSDs is required for data analysis.

B. Study of emitted $\gamma$ rays

Transitions of the impinging nucleus into an excited state of the outgoing nucleus are identified by measuring the gamma energy released during the deexcitation of the state. As the particles are strongly forward boosted ($\beta_{^{20}N} = 0.742$ and $\beta_{^{21}N} = 0.726$, where $\beta$ is the velocity divided by the speed of light $c$), a correction for the Doppler shift is applied. Furthermore, the segmentation of the Crystal Ball makes it necessary to take care of hits in several crystals by using an add-back algorithm which works as follows. Single crystals with an energy $E_{\gamma,\text{crystal}} > 0.3$ MeV (to suppress background due to Bremsstrahlung) are grouped to clusters which are used to calculate the entire emitted gamma-energy during the reaction of one impinging particle.

In the left panel of Fig. 3 (red, solid line) the summed gamma energy (sum of all clusters) for incoming $^{20}$N and outgoing $^{19}$N is shown. A clear peak at $E_{\gamma,\text{sum}} = 1.15$ MeV is visible, corresponding to the first excited state of the outgoing $^{19}$N nuclei as previously measured by Sohler et al. [18]. The blue dashed line indicates a background estimation by gating on unreacted outgoing $^{20}$N (otherwise equal cuts as discussed in Sec. III A). This shows that the peak at 1.15 MeV is not caused by background events. Furthermore, there is a high-energy tail with count rates half as large as that of the signal peak. These might correspond to higher lying states of $^{19}$N. But due to the limited statistics and energy resolution, they cannot be unambiguously identified.

The gamma sum spectrum originating from deexcitations of $^{20}$N is shown in the right panel of Fig. 3. A dominant peak is visible at $E_{\gamma,\text{sum}} = 0.85$ MeV, again corresponding to the first excited state [18]. Only a small additional structure arises at 1.3 MeV and no significant structures are detected at $E_{\gamma,\text{sum}} \geq 1.5$ MeV. As Sohler et al. [18] reported several peaks in the close vicinity of 850 keV, and due to the limited energy resolution of our gamma spectra, the observed peak cannot unambiguously be used to gate on the first excited state. Therefore, a gate on transitions into the first plus the second excited state is given in the presented analysis.

C. Coulomb dissociation cross section

After applying the cuts for selecting the reaction channel, the reaction probabilities are obtained by dividing the number of reaction events (see Sec. III A) by the effective number of nuclei impinging onto the target. The latter value is derived by counting all outgoing nitrogen isotopes that are detected at the fragment arm, including the unreacted $^{20}$N (resp. $^{21}$N) ions. This automatically takes into account losses due to particles scattered out of the beamline, detector inefficiencies in the fragment arm, and applied cuts which together amount to 33%.

The Coulomb dissociation cross section follows as

$$\sigma_{\text{CD}} = p_{\text{pb}}^{\text{react}} F_{\text{pb}} - p_{\text{c}}^{\text{react}} \alpha F_{\text{c}} - p_{\text{empty}}^{\text{react}} (F_{\text{pb}} - \alpha F_{\text{c}})$$  (1)

with

$$F_{\text{target}} = \frac{M_{\text{target}}}{d_{\text{target}} N_A}$$
where the indices Pb, C, and empty denote the specific targets (lead, carbon, and no target). $p_\text{target}^{\text{react}}$ is the probability of the impinging particle to react with the target, $M_\text{target}$ is the molar mass of the material of the target, $d_\text{target}$ is the areal density of the target (measured by weighing), $N_A$ is Avogadro’s number, $\alpha$ is the nuclear scaling factor derived in the following paragraph.

The factor $\alpha$ is necessary to scale the nuclear contribution measured with the carbon target to the much larger lead nuclei. The black disk model is used to estimate

$$\alpha_{\text{PB}} = \frac{A_{\text{FB}}^{1/3} + A_{\text{Pb}}^{1/3}}{A_{\text{FB}}^{1/3} + A_{\text{C}}^{1/3}} = 1.7.$$  \hspace{1cm} (2)

As $p_\text{C}^{\text{react}} < 0.1 p_\text{Pb}^{\text{react}}$, the choice of $\alpha$ has only a limited influence on $\sigma_{\text{CD}}$.

D. Excitation energy

The excitation energy $E^*$ of the reaction is extracted by the invariant mass method via

$$E^* = c^2 \sqrt{m_{\text{frag}}^2 + E_X^2 - m_{\text{proj}}^2 c^2 + E_{\gamma, \text{sum}}}$$  \hspace{1cm} (3)

with

$$E_X = 2 \gamma_{\text{frag}} \gamma_{\text{n}} m_{\text{frag}} m_{\text{n}} (1 - \beta_{\text{frag}} \beta_{\text{n}} \cos \theta_{\text{frag},n}),$$

where $m_{\text{proj}}$ is the rest mass of the incoming nucleus, $m_{\text{frag}}$ is the rest mass of the outgoing heavy reaction fragment, $m_{\text{n}}$ is the rest mass of the outgoing neutron, $\beta_{\text{frag}}$ is the velocity of the outgoing heavy reaction fragment, $\beta_{\text{n}}$ is the velocity of the outgoing neutron, $\gamma_{\text{frag}} = (1 - \beta_{\text{frag}}^2)^{-1/2}$, $\gamma_{\text{n}} = (1 - \beta_{\text{n}}^2)^{-1/2}$, $\theta_{\text{frag},n}$ is the angle between the outgoing heavy reaction fragment and the neutron, while $E_{\gamma, \text{sum}}$ is the energy of all gamma quanta emitted during the reaction. Here, due to the high photopeak efficiency ($\sim 70\%$) of the crystal ball at the relatively low $\gamma$-ray energies ($\sim 1$ MeV), $E_{\gamma, \text{sum}}$ is simply taken as the sum of the detected $\gamma$-ray energies. This approximation entails a slight downward shift of the excitation function for Coulomb dissociation into excited states of the product nucleus, which is not significant here, because those states contribute only negligibly to the reaction rate at the effective astrophysical temperatures.; see below.

The mass of the incoming $^{20}$N (resp. $^{21}$N) and the outgoing $^{19}$N (resp. $^{20}$N) were taken from the AME2003 mass evaluation [19]. Differences to the updated mass evaluation AME2012 [20] amount to only 10 keV, much less than the experimental resolution.

An energy-dependent correction for the neutron detection efficiency must be applied to the Coulomb dissociation cross section. The total neutron efficiency of LAND is based on a simulation which includes the acceptance due to the kinematics of the specific reaction, the acceptance due to deactivated/broken paddles and the nominal energy-dependent neutron efficiency of the detector measured in an earlier experiment [17].

For kinetic energies in the center of mass of $T_{n\text{m}}^\text{c} < 5$ MeV, the neutrons are strongly forward boosted, so that all neutrons hit the active area of LAND. The efficiency drops dramatically for $T_{n\text{m}}^\text{c} > 5$ MeV as the transverse momentum component becomes more dominant and, thus, many neutrons miss the active area of LAND.

The kinetic energy of the neutrons in the center-of-mass system for the $^{20}$N($\gamma$, $n$)$^{19}$N reaction is depicted in Fig. 4.

E. Differential Coulomb dissociation cross section

The differential reaction cross section of $^{20}$N impinging onto the lead target as a function of the excitation energy $E^*$ is extracted from the yield formula

$$\frac{d\sigma_{\text{Pb}}}{dE^*} = \left( \int_{E^*} ^{E^*+dE^*} d\sigma_{\text{Pb}}(\tilde{E}) \frac{d\tilde{E}}{dE^*} \right) \frac{1}{\Delta E^*},$$

where $N(\text{Pb})$ is the number of outgoing $^{19}$N nuclei, $N(\text{Pb})$ is the number of incoming $^{20}$N nuclei, and $n_{\text{LAND}}$ is the one-neutron detection efficiency of LAND.

The differential Coulomb dissociation cross section as a function of the excitation energy [Eq. (3)], then, is given by

$$\frac{d\sigma_{\text{CD}}}{dE^*} = [P_{\text{Pb}}(E^*) F_{\text{Pb}} - P_{\text{C}}(E^*) \alpha F_{\text{C}} - P_{\text{empty}}(E^*) F_{\text{empty}}] \frac{1}{\Delta E^*}.$$

The total differential Coulomb dissociation cross section (including transitions into the ground state and any excited state) as a function of the excitation energy for impinging $^{20}$N is depicted in Fig. 5 (black line).

In order to separate transitions of $^{20}$N($\gamma^*$, $n$) into the first excited state of $^{19}$N at 1141 keV, a cut on $0.70 < E_{\gamma, \text{sum}} < 1.40$ MeV is performed. Furthermore, the resulting
\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig5.png}
\caption{Coulomb dissociation cross section of $^{20}$N as a function of the excitation energy for the total reaction (black line) and transitions into the first excited state of $^{19}$N at 1141 keV (red line). The error bars reflect statistical uncertainties only.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig6.png}
\caption{Coulomb dissociation cross section of $^{21}$N as a function of the excitation energy for the total reaction (black line) and transitions into the ground state of $^{20}$N (magenta line). The error bars reflect statistical uncertainties only. For the ground state transitions, the error bars were omitted for reasons of clarity as they are comparable to the ones of the total reaction.}
\end{figure}

$E^*$ spectrum is corrected for the photopeak efficiency of the Crystal Ball $\epsilon(E_{\gamma,\text{sum}} = 1.15 \text{ MeV}) = 0.67$ which is based on simulations taking into account the kinematic boost. The result is shown in Fig. 5 (red line).

Transitions into the ground state of $^{19}$N are explored by subtracting transitions into any excited state (with a gate on $E_{\gamma,\text{sum}} > 0.7 \text{ MeV}$) from the total excitation energy spectrum (see Fig. 5). Here, the excited state data are corrected for the total $\gamma$ efficiency of 0.85, which is constant within 3\% for $E_{\gamma,\text{sum}} = 1-5 \text{ MeV}$.

The total differential Coulomb dissociation cross section as a function of the excitation energy for impinging $^{21}$N is shown in Fig. 6 (black line). Transitions of $^{21}$N($^{\gamma^*,n}$) into the first plus second excited state of $^{20}$N are deduced by gating on $0.40 < E_{\gamma,\text{sum}} < 1.00 \text{ MeV}$ and correcting for the photopeak efficiency of $\epsilon(E_{\gamma,\text{sum}} = 0.90 \text{ MeV})$.

In order to derive the transitions into the ground state of $^{20}$N (Fig. 6, magenta line), the $E^*$ spectrum of the transitions of $^{21}$N($^{\gamma^*,n}$) into any excited state of $^{20}$N with $E_{\gamma,\text{sum}} > 0.40 \text{ MeV}$ is corrected with the total $\gamma$ efficiency and subtracted from the total reaction.

\subsection{F. Error budget}

Systematic uncertainties from the identification of the incoming particles are derived by varying the cuts on $A/Z$ and $dE/dx$ of the incoming particle from $2\sigma$ to $3\sigma$ and calculating the difference. As these uncertainties are very small (3\%) in contrast to the statistical uncertainties, these will be neglected in the further analysis.

Moreover, the single neutron detection efficiency of LAND is known with an uncertainty of 6\%. The Crystal Ball efficiency is determined with an uncertainty of 6\%.

\begin{table}[h]
\centering
\begin{tabular}{lcc}
\hline
 & $^{20}$N (total) & $^{21}$N (total) \\
\hline
$\sigma_{\text{CD}}$ (mb) & $(90 \pm 12)_{\text{stat}}$ & $(75 \pm 13)_{\text{stat}}$ \\
\hline
\end{tabular}
\end{table}

The uncertainty of the measurement of the areal density of the target amounts to 2\% and, thus, will be neglected in the further analysis.

The results of the Coulomb dissociation cross sections and the corresponding uncertainties are summarized in Table I.

\section{IV. RESULTS}

Most of the Coulomb dissociating $^{20}$N nuclei populate excited states of $^{19}$N (Table I): 40\% of the total Coulomb dissociation cross section is caused by transitions into the first excited state of $^{19}$N at 1141 keV, 44\% to higher excited states.
states. Only 17% of the reactions are caused by transitions into the ground state, which is compatible with zero within the statistical uncertainties.

The total excitation energy spectrum of the Coulomb dissociation of $^{20}$N is shown in Fig. 5 (black line). While there are no entries for energies from 0 to 2 MeV, the spectrum notably increases at 2 MeV. The one-neutron separation threshold of $^{20}$Ni is 2.16 MeV.

Some structures appear at 5.5, 7.0, 9.0, 10.2, and 11.5 MeV. For $E^* > 17$ MeV, the spectrum drops to values consistent with zero within the statistical errors as the number of virtual photons at 18 MeV drops to 15% of that at 3 MeV.

Transitions of $^{20}$N into the first excited state of $^{19}$Na at 1143 keV are depicted in Fig. 5 (red line). Here, the spectrum rises significantly above zero for energies $E^* = 3.5$ MeV which reflects the sum of $S_{\text{in}}(20N)$ and the energy of the first excited state. Some structure is visible for energies between 3.5 and 14 MeV.

A summary of the cross sections for the Coulomb dissociation of $^{21}$N is presented in Table I. Here, 59% of the Coulomb dissociation $^{21}$N into excited states of $^{20}$N [less than for the $^{20}$N($\gamma^*,n$)$^{19}$N reaction]. 41% of the reactions pass into the ground state of $^{20}$N [higher than for $^{20}$N($\gamma^*,n$)$^{19}$N].

The total energy-dependent Coulomb dissociation cross section of $^{21}$N is shown in Fig. 6 (black line). The spectrum does not show any entry between 0 and 4.5 MeV. The one-neutron separation threshold of $^{21}$N is $S_{\text{in}}(21N) = 4.60$ MeV. The spectrum rises significantly above zero at $E^* = 5.25$ MeV. Subsequently, there is a structure between 5 and 14 MeV. Beyond 14 MeV the spectrum drops to values consistent with zero.

The energy-dependent Coulomb dissociation cross section of $^{21}$N, passing into the ground state of $^{20}$N, is depicted in Fig. 6 (magenta line). The spectrum rises significantly above zero for energies between 5 and 9 MeV with a plateau-like structure. No significant peaks can be identified due to the large statistical uncertainties.

V. PHOTOOBSORPTION AND NEUTRON CAPTURE CROSS SECTION

The differential photoabsorption cross section is calculated via the virtual photon theorem [6]

$$\frac{d\sigma_{\text{CD}}}{dE_{\gamma}} = \frac{1}{E_{\gamma}} n_{E_1}(E_{\gamma}) \sigma_{\text{photo}}.$$  \hspace{1cm} (6)

Here, $d\sigma_{\text{CD}}/dE_{\gamma}$ is the differential Coulomb dissociation cross section as a function of the excitation energy (where $E_{\gamma} \equiv E^*$), calculated as in the previous section, $n_{E_1}(E_{\gamma})$ is the number of virtual photons and $\sigma_{\text{photo}}$ is the photoabsorption cross section for multipolarity $E1$ as a function of the excitation energy.

As the cross sections of higher multiplicities are found to be three orders of magnitude lower than for $E1$ [21], higher multiplicities are neglected.

Then, the photoabsorption cross section is derived from

$$\sigma_{\gamma,n} \equiv \sigma_{E1}^{\text{photo}} = \frac{1}{E_{\gamma} n_{E1}(E_{\gamma})} \frac{d\sigma_{\text{CD}}}{dE^*} E^*.$$  \hspace{1cm} (7)

The virtual photon spectrum for the $E1$ multipolarity is derived as described in detail in Ref. [6]:

$$n_{E1}(E^*) = \frac{2}{\pi} Z^2_{\text{eff}} a^2 \left(\frac{e}{\pi}\right)^2 \left[\xi K_0(\xi) K_1(\xi) - L(\xi)\right]$$ \hspace{1cm} (8)

with

$$L(\xi) = \frac{\mu^2}{2\xi^2} \left[K_1^2(\xi) - K_0^2(\xi)\right],$$

where $K_i$ are the modified Bessel functions of order $i$, $\alpha$ is the fine-structure constant, and $\xi$ is the adiabaticity parameter which reads $\xi = E^*/b((h\gamma/\beta)c)$ with $b$ as the impact parameter.

Utilizing the fact that nuclear reactions are invariant under time reversal, the neutron capture cross section is determined via the theorem of detailed balance [6]:

$$\sigma_{n,\gamma} = \frac{2(2I_A + 1)}{(2I_B + 1)(2I_\text{cm} + 1)} k^2_{\text{cm}} \sigma_{\gamma,n}.$$ \hspace{1cm} (9)

where $\sigma_{\gamma,n}$ is the photoabsorption cross section [see Eq. (7)], $k_{\text{cm}} = E^*/(\hbar c)$, $k^2_{\text{cm}} = 2\mu(E^* - Q)/\hbar^2$ with $Q = S_{\text{in}} + S_{\gamma,\text{sum}}$, and $\mu$ is the reduced mass of the system of the outgoing fragment plus neutron [e.g., for the system $^{19}$N+n, $\mu = (M_{\gamma}\gamma M_n)/M_{\gamma} (M_{\gamma} + M_n)$]. $I_{A,B}$ are the spins of the incoming and outgoing particle. With $^{20}$N as the incoming nucleus, index A denotes $^{20}$N with $I_A = 2$ for the ground state, index B represents the outgoing $^{19}$N with $I_B = 1/2$ for the ground state and $I_B = 3/2$ for the first excited state, and index $n$ indicates the neutron with $I_n = 1/2$. With $^{21}$N as the incoming beam, $I_A = 2$ for the ground state, index B represents the outgoing $^{20}$N with $I_B = 2$ for the ground state and $I_B = 3$ for the first excited state.

Integrating over energies $E_{\text{c.m.}} \in [0,15]$ MeV (where $E_{\text{c.m.}} = E^* - Q$), the neutron capture cross section of the ground state of $^{19}$N amounts to $\sigma_{n,\gamma}(^{19}$N, g.s.) = (0.003 ± 0.010stat) mb. As the statistical uncertainty is large, only an upper limit with 90% confidence level is given: $\sigma_{n,\gamma}(^{19}$N, g.s.) ≤ 0.016 mb. The neutron capture cross section of the first excited state of $^{19}$N amounts to $\sigma_{n,\gamma}(^{19}$N, 1st) = (0.0057 ± 0.0014th) mb. Similarly, the neutron capture cross section of the ground state of $^{20}$N amounts to $\sigma_{n,\gamma}(^{20}$N, g.s.) ≤ 0.0091 mb.

The first and the second excited states of $^{20}$N cannot be clearly separated due to the low resolution of our gamma spectra. For further analysis of the stellar reaction rate and its implementation into a reaction network we provide the neutron capture cross section of the first and second excited state of $^{20}$N $\sigma_{n,\gamma}(^{20}$N, 1st + 2nd) = (0.0041 ± 0.0010th) mb.

A summary of the derived photoabsorption and neutron capture cross sections is given in Table II.

VI. ASTROPYHICAL REACTION RATE

From the derived neutron capture cross section, the Maxwellian averaged reaction rate [22] is calculated,

$$N_A(\sigma v) = N_A \left(\frac{8\pi}{\mu^2} k_B T \right)^{1/2} \int_0^\infty \sigma_{n,\gamma} E \exp \left(-\frac{E}{k_B T}\right) dE,$$  \hspace{1cm} (10)
TABLE II. Photoabsorption and neutron capture cross section of the nitrogen isotopes under study. The errors reflect statistical uncertainties only. Upper limits are given with 90% confidence level.

<table>
<thead>
<tr>
<th>$\sigma_{\gamma,n}$($^{20}$N), total</th>
<th>(1.15 ± 0.27) mb</th>
</tr>
</thead>
<tbody>
<tr>
<td>ground state</td>
<td>0.62 mb</td>
</tr>
<tr>
<td>1st excited state</td>
<td>(0.51 ± 0.12) mb</td>
</tr>
<tr>
<td>$\sigma_{\gamma,n}$($^{21}$N), total</td>
<td>(0.93 ± 0.30) mb</td>
</tr>
<tr>
<td>ground state</td>
<td>0.74 mb</td>
</tr>
<tr>
<td>1st + 2nd exc. state</td>
<td>(0.69 ± 0.16) mb</td>
</tr>
<tr>
<td>$\sigma_{\gamma,n}$($^{19}$N), ground state</td>
<td>0.016 mb</td>
</tr>
<tr>
<td>1st excited state</td>
<td>(0.0057 ± 0.0014) mb</td>
</tr>
<tr>
<td>$\sigma_{\gamma,n}$($^{20}$N), ground state</td>
<td>0.0091 mb</td>
</tr>
<tr>
<td>1st + 2nd exc. state</td>
<td>(0.0041 ± 0.0010) mb</td>
</tr>
</tbody>
</table>

where $N_A$ is Avogadro’s number, $\mu$ the reduced mass of the system under study (e.g., $^{19}$N + n), $k_B$ the Boltzmann constant, and $T$ the temperature of the stellar environment (assumed to be in thermal equilibrium with the nuclei under study).

Due to the large, predominantly statistical uncertainty of the neutron capture cross section of the ground state of $^{19}$N and $^{20}$N, we applied a randomization technique. For each energy bin in the measured neutron capture histogram, a random Gaussian distribution is built where the bin content acts as mean value and the statistical uncertainty of the bin acts as sigma of the Gaussian distribution. Then, the randomly distributed neutron capture cross section is used to calculate the Maxwellian averaged reaction rate for each temperature [see Eq. (10)], forcing the Maxwellian averaged reaction rates to be positive definite. This procedure is repeated 1000 times; thus, for each temperature we generate 1000 values of the resulting distribution is used as a value in the Maxwellian averaged reaction rate. Then, the mean is calculated to calculate the Maxwellian averaged reaction rate for each temperature. The red dotted line denotes contributions from the ground state of $^{19}$N and the blue dotted-dashed line denotes contributions from the first excited state of $^{19}$N. The black dashed line denotes a theoretical curve given by [25].

The red dotted line denotes contributions from the neutron capture of the ground state of $^{19}$N and the blue dotted-dashed line denotes contributions from the neutron capture of the first excited state of $^{19}$N. The black dashed line denotes a theoretical curve given by [25].

As a result, the contribution of low-energy first excited states, which are located at 843 and 1177 keV for $^{20,21}$N respectively [18], to the total ($n,\gamma$) reaction rate is not constrained by the present measurement. In previous studies, the inclusion of the capture to thermally populated excited states has led to significant enhancement of the total cross section [9].

Then, the $^{19}$N($n,\gamma$)$^{20}$N reaction rates as a function of the temperature are compared with reaction rates included in reaction network codes which are mainly based on one theoretical work [25] considering just direct capture and giving a linear approximation $N_A(\nu)^{\text{theory}} = (1.54 \times 10^3)T_9$.

In Fig. 7, the stellar reaction rate [see Eq. (12)] of $^{19}$N($n,\gamma$)$^{20}$N is plotted as a function of the temperature. The red dotted line denotes contributions from the ground state of $^{19}$N (generated with the randomization technique) and the blue dotted-dashed line denotes contributions from the first excited state of $^{19}$N while considering the population probability [compare Eqs. (11) and (12)]. The black solid line denotes the stellar reaction rate which is obtained by summing the ground-state and first excited-state contributions, while the black dashed line denotes theoretical estimates [25]. It is clear that the excited state only plays a role for $T > 3$ GK.

At temperatures between 0.1 and 1.0 GK, our measured data exceed the theoretical ones by up to a factor of 3 before the ratio drops below 1 and finally levels out at 0.1 of the theoretical predictions.

In Fig. 8, the stellar neutron capture reaction rate of $^{20}$N is shown in a fashion analogous to that of Fig. 7. Again, we note that due to the limited resolution of the theoretical work only constrain the contribution of the ground state. As a result, the contribution of low-energy first excited states, which are located at 843 and 1177 keV for $^{20,21}$N respectively [18], to the total ($n,\gamma$) reaction rate is not constrained by the present measurement. In previous studies, the inclusion of the capture to thermally populated excited states has led to significant enhancement of the total cross section [9].
As basic input, we downloaded the reaction network from the JINA Reaclib Database [27]. As several reactions on neutron-rich light nuclei were not included, we included the reaction rates of $^{14}\text{B}(n,\gamma)^{15}\text{B}$, $^{17}\text{C}(n,\gamma)^{18}\text{C}$, $^{18}\text{C}(n,\gamma)^{19}\text{C}$, $^{19}\text{C}(n,\gamma)^{20}\text{C}$, and $^{18}\text{C}(\alpha,n)^{21}\text{O}$ from Sasaqui et al. [3]. The remaining reaction rates in Ref. [3] were of references predating our reference network. In Ref. [3], Hauser-Feshbach models were used to obtain estimates of the reaction rates for light neutron-rich nuclei. As the network calculation presented here is not supposed to explain the entire $r$-process nucleosynthesis, but only to give a rough impression of the impact of our measured reaction rates on the $r$ process, we omitted the derivation of new theoretical reaction rates.

Furthermore, we included the measured stellar reaction rate of $^{20}\text{Ni}(n,\gamma)^{21}\text{Ni}$ (see previous section) and updated the rate of $^{19}\text{Ni}(n,\gamma)^{20}\text{Ni}$ (referred to as “our network”) which included the reaction rate of $^{19}\text{Ni}(n,\gamma)^{20}\text{Ni}$ derived by Rauscher et al. [25] but included our rate of $^{20}\text{Ni}(n,\gamma)^{21}\text{Ni}$, as no previous reference for the latter reaction was available in the literature.

In order to simulate an $r$-process environment, we used the following trajectory for the evolution of density in time consisting of an exponential decay, reflecting the expanding medium of the supernova, and an additional slower decaying term, reflecting the neutrino wind [28]:

$$
\rho(t) = \rho_0 \exp(-t/\tau_0) + \rho_1 \left(1 + t/\tau_1\right)^{-1},
$$

(13)

where $\rho_0 = 1.7995 \times 10^6 \text{ g/cm}^3$ is the initial density (at $t = 0$ s) of the exponential term, $\rho_1 = 540 \text{ g/cm}^3$ is the constant density of the second term, and $\tau_0 = 0.0051 \text{ s}$ is the decay constant of the exponential term.

The temperature $T$ is parametrized as

$$
T(t) \propto \rho(t)^{1/3},
$$

(14)

with $T(t = 0 \text{ s}) = 9.0 \text{ GK}$. These input parameters were chosen to match Terasawa et al. [5]. The initial neutron-to-proton ratio was set to 65/35 (which corresponds to set 2 in Table 4 of Sasaqui et al. [3]).

Then, the network was run to calculate the reaction flow until $10^6 \text{ s}$ after the supernova exploded. In Fig. 9, we extracted the abundance as a function of nucleon number at that time (red line) where the three main $r$-process peaks are visible at $A = 79$, $A = 130$, and $A = 195$. For comparison we added the solar abundances of $r$-process elements as derived by K"appeler et al. (1989) [29] (black symbols) and rescaled our data to match the height of the peak at $A = 195$.

Our efforts on network calculations are not to understand the entire $r$ process in detail but to estimate the impact of our measured reaction rates on the $r$-process abundances. Therefore, we use the abundances derived with our network for comparison with abundances computed when using the reference network (see previous passage).

We find a decrease of 10% for fluorine ($A = 19$), but the abundances of nuclei with higher mass are unaffected by our data.

In Fig. 10, we show the reaction flow which is the contribution per nucleon per second to the abundance of...
measured the reaction rate exactly in the important temperature range. Corrections due to neutron capture of excited states of the target nucleus play no role in this temperature range (Figs. 7 and 8).

In order to gauge the possible impact of an increase in the reaction rate due to neutron capture into excited states of the product nucleus, which is not constrained by the present data (see Sec. VI), the network calculations have been repeated with tenfold increased \((n,\gamma)\) reaction rates. The resulting fluorine abundance is 50% lower than in the reference case, and again no measurable impact is seen on any other nucleus.

VIII. SUMMARY AND OUTLOOK

Summary. We measured the Coulomb dissociation cross section of \(^{20,21}N\) and discriminated between transitions into the ground state and the first excited state of the outgoing nuclei. In the case of \(^{21}N\), we could not separate the first from the second excited state due to the limited resolution of our gamma calorimeter. Therefore, we presented only transitions into any excited state of the outgoing \(^{20}N\) ions.

Furthermore, we calculated the photo absorption cross sections via the virtual photon theory and the neutron capture cross section by using the principle of detailed balance for each individual reaction, discriminating for the excitation level of the outgoing particle. In these cases, the ground state contributions had such a low statistical uncertainty that only an upper limit could be presented.

Moreover, the thermonuclear and the stellar reaction rates were computed even for ground state transitions due to the use of a Monte Carlo method. Additionally, the reaction rates were compared to theoretical predictions.

Finally, network calculations were performed to estimate the impact of our measured reaction rates on the possible \(r\)-process scenario of a supernova with a neutrino driven wind.

A decrease of 10% in the fluorine \((A = 19)\) abundance was found relative to the abundances when using the reference rates \([25]\). The abundances of nuclei with higher mass were unaffected.

Outlook. In the future, our measured reaction rates may be implemented in reaction networks which include even more light neutron-rich nuclei. Other possible \(r\)-process scenarios could be used to study the impact of these reaction rates on the final \(r\)-process elemental abundance in more detail.

A repetition of our measurements with more statistics could reduce the statistical uncertainties already in the excitation energy spectra and the photoabsorption and neutron capture cross sections.

Additionally, the low resolution of our gamma spectra prevented the separation of the first from the second excited state of outgoing \(^{20}N\). Thus, a repetition with a gamma spectrometer with higher granularity and intrinsic energy resolution would improve the separation on the one hand and the resolution of the excitation energy spectra on the other hand.

Both experimental improvements will be provided in the future FAIR (Facility for Antiproton and Ion Research) which is presently under construction at GSI in Darmstadt, Germany \([30]\).
ACKNOWLEDGMENTS

This work was supported in part by GSI (F&E, DRLZUBE), Bundesministerium für Bildung und Forschung (BMBF) (06DR1341, 05P09CRFN5, 05P12RDFN8, and 05P15RDFN1), the Helmholtz Association Germany through the Nuclear Astrophysics Virtual Institute (NAVI, Grant No. VH-VI-417), the Helmholtz Association Detector Technology and Systems Platform, the Spanish Research funding agency under projects FPA2012-32443, FPA2013-41267-P, and FPA2013-47831-C2-1-P, the Swedish Research Council, HIC for FAIR and the TU Darmstadt-GSI cooperation contract, the Portuguese FCT project PTDC/FIS/103902/2008, UK STFC under grants ST/E500651/1 and ST/F011989/1, US NSF Grant No. 1415656, and US DOE Grant No. DE-FG02-08ER41533.