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1 **Fluid-Structure Interaction Assessment of Blood Flow Hemodynamics and**
2 **Leaflet Stress During Mitral Regurgitation**

3
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11
12 **Abstract**

13 The aim of this study is to simulate the Mitral Regurgitation (MR) disease
14 progression from mild to severe intensity. A Fluid Structure Interaction (FSI)
15 model was developed to extract the hemodynamic parameters of blood flow in
16 mitral regurgitation (MR) during systole. A two-dimensional (2D) geometry of the
17 mitral valve was built based on the data resulting from Magnetic Resonance
18 Imaging (MRI) dimensional measurements. The leaflets were assumed to be
19 elastic. Using COMSOL software, the hemodynamic parameters of blood flow
20 including velocity, pressure, and Von Mises stress contours were obtained by
21 moving arbitrary Lagrange-Euler mesh. The results were obtained for normal and
22 MR cases. They showed the effects of the abnormal distance between the leaflets
23 on the amount of returned flow. Furthermore, the deformation of the leaflets was
24 measured during systole. The results were found to be consistent with the relevant
25 literature.

26 **Keywords:** Fluid-Structure Interaction, hemodynamics, mitral, regurgitation,
27 systole

1 **Introduction**

2 Mitral valve regurgitation is a condition in which the valve does not close tightly
3 and there is an abnormal reversal of blood flow from the left ventricle to the left
4 atrium. This increases the pressure in the left atrium and may lead to complications
5 such as dyspnea, fatigue, orthopnea, and pulmonary edema. Mitral valve
6 regurgitation is an important health issue. More than three millions people in the
7 USA suffer from moderate or severe regurgitation [1]. In spite of the fact that
8 measuring hemodynamic parameters in left ventricle and mitral valve stress
9 patterns are significantly challenging, numerical analyses can be used to develop
10 new models to further understand this issue [2]. Coincident with developments in
11 non-invasive blood flow imaging (echo-doppler and Magnetic Resonance Imaging,
12 MRI), in recent years significant studies have combined such imaging with
13 numerical simulation [3]; with applications to human mitral valves, including
14 prediction of disease progression and treatment.

15 One of the first attempts for modeling of mitral regurgitation (MR) was by Dent et
16 al. [4] who introduced a mathematical model for the quantification of MR using
17 experimental data. In parallel, Doppler echocardiography, color Doppler
18 assessment, and color Doppler mapping were used to study the degree of MR
19 [5,6,7]. More recently, Wenk et al. [8] have studied a finite element model of the
20 left ventricle with mitral valve. Their model was based on magnetic resonance
21 imaging data from a sheep that had developed moderate ischemic MR after
22 postero-basal myocardial infarction. A three-dimensional (3D) FSI model of MR
23 flow was presented by Mao et al. [9] that showed the FSI method could simulate
24 the coupled valves structure response and the intraventricular hemodynamics in
25 left ventricle. Little et al [10] introduced a 3D ultrasound imaging model of MR.
26 Einstein [11] studied MR by using a Fluid-Structure Interaction (FSI) model.

1 Together these studies have presented a comprehensive strategy for analyzing MR.
2 Development by This et al. [12] presented a one-way FSI model to simulate three
3 different mitral valve defects, including blood-flow in patients. While numerical
4 techniques, including FSI, have been applied for the development of a ‘healthy’
5 mitral valve model [13-15], Su et al. [16] studied the intraventricular flow in a
6 patient-specific mitral and aortic valves integrated model including left ventricle
7 using a Two-dimensional methodology. Their results confirmed the ability of
8 estimating the patient-specific intraventricular flow by means of numerical method
9 together with FSI approach. While models of MR are developing, there has been
10 limited assessment of the effect of ventricular and annular dimensions on MR.
11 Particularly valuable is intraventricular flow during the early diastolic phase, when
12 the hemodynamic parameters including vortices may be important in filling [17],
13 closure and regurgitation of the mitral valve.

14 The aim of this study is the development of a computational model for the
15 assessment of MR, including its progression from mild to severe. To assess the
16 feasibility of developing such an FSI model, a 2D model is assessed, which may
17 also be more likely to undergo clinical translation due to the model solution times
18 [3]. This initial model has focused on assessing MR during three main cases: mild,
19 moderate, and severe conditions.

20

21 **Methods**

22 A 2D simplified parametric model of the mitral valve was built using Comsol
23 Multiphysics software (Figure 1). This model was based on certain dimensions of
24 left ventricle that was measured through an MRI image. The model included two
25 leaflets and a semi elliptical left ventricle. Both leaflets have the same geometry

1 and considered as symmetrical. The tips of the leaflets were set as touching in a
2 'normal' position [15] whereas the distance between the leaflets is 1 mm (mild
3 MR), 3 mm (moderate MR), and 5 mm (severe MR) inspired from a physical
4 model [18]. Blood is a virtually incompressible fluid and non-Newtonian [19-21];
5 however, it can be considered as Newtonian in large arteries and the heart. In the
6 present study, we assumed blood to be a Newtonian fluid [22-23]. The leaflets
7 were considered as isotropic and linear elastic material with Poisson's ratio of 0.33
8 [24] and Young's modulus of 1 MPa [25]. The viscosity of blood was set to 2.7
9 mPa.s and density of 1060 kg/m³ [17]. Because the model was solved during the
10 systolic phase, the ventricular pressure as well as the atrial pressure were
11 considered as inputs.

12 **Boundary conditions**

13 The total time of systolic phase was 0.3 s which was considered for the simulation.
14 The fluid applied a force on the leaflets leading to closure; further described
15 elsewhere [13]. The functions of the ventricular pressure and atrial pressure were
16 defined in the software as time-dependent inlet boundary conditions (Figure 2a,
17 2b) [16]. For the systolic phase, an aortic velocity function was defined at the
18 boundary of a simplified aorta (Figure 2c, 2d). All other boundaries, including
19 ventricle walls were considered as a non-slip condition. It should be noted that
20 mitral leaflets and related edges were restricted from moving.

21 Triangular normal elements were used, with a finer meshing was set for leaflet
22 areas in order to get more precise numerical solution (Figure 3; Table 1). A moving
23 Arbitrary-Lagrange-Euler (ALE) mesh was applied to the leaflets and the blood
24 flow, however, the other areas had a fixed mesh. COMSOL Multiphysics (Comsol
25 Multiphysics, Stockholm, Sweden) was used to solve the model using a transient
26 FSI method; described in further detail elsewhere [26-28].

1

2

3 Table.1: Specifications of mesh parameters

Number of vertex elements	13
Number of boundary elements	245
Number of elements	2781
Minimum element quality	0.505

4

5 **Results**

6 The performed numerical simulation was used to predict the pressure, velocity, and
7 Von Mises stress contours, for blood-flow and the valve leaflets, respectively,
8 during mild, moderate, and severe MR. The extracted hemodynamic parameters
9 are presented and compared as below.

10 1-Pressure:

11 Figure 4a-4c provides the pressure contours in three different time steps for severe
12 MR. In severe MR, the leaflets were not attached to each other completely and
13 there is an approximately 5 mm distance between the leaflets. The contours
14 showed a pressure drop in the left ventricle. At a time of 0.3 s, the ventricle
15 pressure variation was between 0.9 to 14.5 kPa with much back flow to the atrium.

16 Figure 5a-5c shows the pressure contours at three different time steps for
17 moderate MR. The pressure drop within the left ventricle was lower than for severe
18 MR but was still between 10-15 kPa. This drop was still considerable and due to a
19 3 mm distance between the leaflets.

20 Figure 6a-6c presents the pressure contours for mild MR. The ventricular
21 pressure reached to 16 kPa which was near to that for a 'healthy' valve. The

1 distance of 1 mm, between leaflets, was not effective in reducing the ventricle
2 pressure as compared to severe MR. The backflow of blood towards the atrium
3 was much lower than for moderate and severe MR.

4 Therefore, the severity of MR could be quantified from the pressure contours and
5 decreasing of ventricle pressure. For severe MR, a decrease in ventricle pressure is
6 predicted, down to 0.9 kPa (at 0.3 s). Furthermore, the backflow of blood was
7 much greater toward the atrium during severe MR. Wenk et al [8] reported the left
8 ventricle pressure between 0.8 kPa to 12.19 kPa during MR. These values are
9 consistent with our results during moderate and severe MR, which ranged from
10 was 0.9 kPa to 14 kPa.

11

12 2-Velocity:

13 The velocity streamlines of severe, moderate and mild MR are shown in Figures 7-
14 9, respectively. Moreover, Figure 10 shows the maximum velocity at the tip of the
15 leaflets area for three time steps during systole in three MR modes. According to
16 these results, it can be concluded that the velocity increases up to 6 and 4.8 m/s at
17 the leaflet tips area in severe and moderate MR, respectively, resulting to the
18 formation of a velocity jet. However, there appeared to be a slight increase in the
19 velocity (about 1.6 m/s) for mild condition resulting no velocity jet. The velocity
20 changing trend is generally consistent with all MR conditions including some
21 vortices evident in the center of ventricle. Vermeulen [29] reported the range of jet
22 velocities between 2.6 m/s to 4 m/s during mitral valve leakage. However, Lassila
23 [30], Thomas [31], and Grayburn [32] concluded that the jet velocity is increased
24 to the highest value during severe MR.

25

26 3- Stress:

1 The stress distribution varied significantly over the leaflets in our
2 results. Stress in Severe MR case Figure 11 (a,b,c) presents the Von Mises
3 stress distribution in severe MR case in three time steps. The stress varied
4 between 100-500 kPa. Stress in Moderate and mild MR case Figure 12 (a,b)
5 shows the stress distribution in moderate and mild MR case at $t=0.3$ s. The
6 average of Von Mises stress on leaflets at mid systole (0.2 sec) for severe,
7 moderate and mild MR are 275, 214 and 74 kPa, respectively. Lee et al.
8 predicted the *in vivo* stresses of a region of interest using a numerical
9 analysis method for the anterior leaflet of a healthy mitral valve. The total
10 range of region of interest (ROI) stresses that they estimated were between
11 80.9 to 593.2 kPa, consistent with our results [33]. The stresses varied
12 between 100 to 500 kPa over the leaflets based on our numerical results for
13 moderate and severe MR. For instance, Wenk et al. [8] reported the
14 effective stress in the center of the anterior leaflet to 119 kPa. Prot et al [34]
15 results showed the leaflet stress to be 130-220 kPa. In another study, Salgo
16 [35] reported higher stresses up to 400 kPa. The difference between the
17 reported values comes back to different type of leaflet material models
18 including linear isotropic, orthotropic, etc.

20 **Discussions:**

21 In this study, an FSI model was developed to simulate the progression of
22 MR disease from mild to severe. Using this model, the blood hemodynamic
23 parameters can be extracted within the progression process and compared
24 between different intensities of MR. There are some limitations to
25 understanding the exact physiology of MV function in healthy and diseased
26 states due to the influence of elastic leaflets and the role of left ventricle in
27 fluid dynamics [36-38]. Therefore, the elastic material properties were also

1 incorporated into simulation in addition to non-Newtonian fluid properties.
2 FSI was used because of the forces that fluid had applied on the leaflets in
3 interaction with the structure which leads to large structural deformations.

4 A comparison of the results obtained between the different severities of MR has
5 led to the following findings:

- 6 • Increasing severity of disease leads to decrease of intraventricular
7 pressure.
- 8 • As the distance between the leaflets increases, the Von Mises stress
9 on the leaflets increases and the return flow to the atrium increases.
- 10 • The increased velocity near the tip of the leaflets in severe MR
11 causes the vortex in the atrium area. This vortex is due to the
12 interaction of the back flow from the ventricle to the fluid flow in the
13 atrium.
- 14 • Another developed vortex, inside the left ventricle, was increased
15 during the early to the end of the systolic phase.
- 16 • It was also shown that a pair of vortices, which were developed
17 under the leaflets, led to valve closure.

18
19 It was shown that this method can measure the stress patterns on the
20 leaflets as the disease progresses. We tried to develop a model to study the
21 hemodynamic parameters of blood flow in mitral regurgitation case. It was
22 found that the pressure throughout the ventricle is decreased and also the
23 velocity jet increased as the distance between leaflets is increased.

24 Moreover, it was shown that an increase in the distance between the leaflets
25 increases the average of Von Mises stress on leaflets at mid systole.

1 On the other hand, considering the same input boundary conditions for
2 different MR states, the contraction of ventricle muscle is not effective, so
3 the leakage plays an important role on decreasing the pressure. When the
4 leakage occurs in one of the components, the pump will not be able to
5 create ideal pressure. In a similar way, for severe disorder mitral function,
6 severe leakage of blood from left ventricle to the atrium (flow back) during
7 systole is observed and leads to decrease of the pressure in the ventricle.
8 There are simplifications in this study, particularly around the use of a 2D
9 model which limits assessment of mitral annular motion. In future, this may
10 be overcome by use of a 3D model. However, in current solution times are
11 prohibitory as regards real-time translation into clinical practice; unlike 2D
12 models which solve over a time-frame which is compatible with clinical
13 practice, as discussed elsewhere [39]. The model presented in this study
14 along with the obtained results was able to capture the mitral regurgitation
15 in different cases based on the gap size between the leaflets. It is important
16 to consider multiple parameters for evaluating MR severity and one single
17 measurement is not sufficient. Thus, we calculated different hemodynamic
18 parameters of MR including pressure and velocity contours as well as
19 leaflets' stress. These predicted results show that a regurgitant jet flow is
20 always present in different MR cases due to an open way from left ventricle
21 to atrium. The severity of MR was studied quantitatively as the area of the
22 jet by above mentioned hemodynamic parameters. We believe that our
23 model was able to demonstrate the function of MR and it can be very
24 helpful for surgeons to use surgical plans based on predicted results of
25 blood flow hemodynamics and leaflet stress during mitral regurgitation.

26

27

1 **Conclusion**

2 In this study, we have modelled the left ventricle with symmetric mitral
3 valves integrated in 2D. In addition to the mitral valve prescribed according
4 progression of MR disease, the FSI approach was applied to the leaflets of
5 valves to simulate the interaction between the blood flow and elastic leaflet.
6 We have successfully demonstrated important parameters (such as pressure
7 and velocity) and development in the mitral regurgitation.

9 **Compliance with Ethical Standards**

10 All procedures performed in studies involving human participants were in accordance with the
11 ethical standards of the institutional and/or national research committee and with the 1964 Helsinki
12 declaration and its later amendments or comparable ethical standards.

13 **Funding:** None.

14 **Conflict of Interest:** Authors declare that they have no conflict of interests.

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