

# First-principles modeling of the temperature dependence for the superlattice intrinsic stacking fault energies in $L_{12}$ $Ni_{75-x}X_xAl_{25}$ alloys

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1 **First-principles modeling of the temperature dependence for the**  
2 **superlattice intrinsic stacking fault energies in  $L1_2$   $Ni_{75-x}X_xAl_{25}$**   
3 **alloys**

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10 **Abstract**

11 Stronger and more resistant alloys are required in order to increase the performance and efficiency  
12 of jet engines and gas turbines. This will eventually require planar faults engineering, or a complete  
13 understanding of the effects of composition and temperature on the various planar faults that  
14 arise as a result of shearing of the  $\gamma'$  precipitates. In this work, a combined scheme consisting  
15 of the density functional theory, the quasi-harmonic Debye model, and the axial Ising model, in  
16 conjunction with a quasistatic approach are used to assess the effect of composition and temperature  
17 of a series of pseudo-binary alloys based on the  $(Ni_{75-x}X_x)Al_{25}$  system using distinct relaxation  
18 schemes to assess observed differences. Our calculations reveal that the (111) superlattice intrinsic  
19 stacking fault energies in these systems decline modestly with temperature between 0 K and 1000 K.

## 20 I. INTRODUCTION

21 In precipitation-strengthened alloys, the shearing of particles is often one of the active  
22 deformation mechanisms. Superalloys are no exception to this, and their complex shearing  
23 mechanisms are indeed partly responsible for their superior mechanical properties at high  
24 temperatures. Over the last few decades, increasing focus has been spent on understanding  
25 these shearing mechanisms, which change with composition and temperature. The crystal  
26 structure of the matrix ( $\gamma$ , fcc) and precipitate ( $\gamma'$ ,  $L1_2$ ) phase is such that a full dislocation  
27 in the matrix results in the introduction of an anti-phase boundary (APB) in the precipitate  
28 phase. Other partial dislocations can also shear these precipitates, leading to a diverse range  
29 of faults: superlattice intrinsic stacking faults (SISFs), superlattice extrinsic stacking faults  
30 (SESFs), complex stacking faults (CSFs), which can themselves be intrinsic or extrinsic,  
31 twin structures and more complicated planar defects.

32 The energies of these planar faults are extremely important as they determine the nature  
33 of the complex dislocation structures shearing the precipitates, as well as the segregation of  
34 solute elements to the fault energies, which in turns can affect the motion of dislocations  
35 through the precipitates. As a result, a number of mechanical properties, such as minimum  
36 grain size due to milling, strain hardening and yield stress depend on planar fault ener-  
37 gies. Creep resistance is also affected by the planar fault energies<sup>1</sup>. As microstructure and  
38 processing methods are refined further, it may be possible to achieve even higher strengths  
39 and high-temperature properties through planar faults engineering. Therefore, a complete  
40 understanding of the effect of composition and temperature on planar fault energies must  
41 be developed in order to exploit these opportunities.

42 Planar fault energies can be measured experimentally, by determining the separation  
43 between partials using transmission electron microscopes. However, the thin-film effects  
44 and uncertainty about how to apply relevant corrections make this type of experimental  
45 work very difficult<sup>2-4</sup>. These issues also make it very difficult to systematically study the  
46 effect of composition and temperature on these planar fault energies.

47 On the other hand, recent experimental work has shown robust evidence of solute seg-  
48regation to these planar faults in the superalloys, often referred to as Suzuki segregation<sup>5</sup>.  
49 Several studies have successfully employed scanning transmission electron microscopy, often  
50 coupled with energy dispersive spectroscopy, to map solute concentration at SISFs, SESFs

51 and twin structures in both Ni- and Co-based superalloys<sup>6,7</sup>. At the same time, the density  
 52 functional theory (DFT) has been employed to compute relevant planar fault energies, and  
 53 to assess the effect of composition on these values. Two main approaches exist for calculating  
 54 planar fault energies using the DFT. A more traditional approach involves calculating the  
 55 energy differences between a perfect and a faulted supercell, thereby simulating the planar  
 56 fault explicitly<sup>8,9</sup>. An alternative approach is to employ the Ising model to describe the  
 57 energy of a large supercell as a sum of contributions arising from the interactions of pairs  
 58 of planes<sup>10</sup>. Both methods have been used to compute various planar fault energies and the  
 59 effect of composition on planar fault energies for  $\gamma'$ - Ni<sub>3</sub>Al-based alloys<sup>8,9,11</sup>.

60 One of the main limitations of the available theoretical studies is that all values are  
 61 computed at 0 K. This may be a problem since the superalloys are usually operating at  
 62 appreciable temperatures. Thus, it becomes necessary to assess how these energies may  
 63 change as temperature is increased. In our recent major work<sup>11</sup>, we have established the  
 64 effect of composition on the SISF energies in all  $\gamma'$ - Ni<sub>3</sub>Al-based alloys at 0 K. We have  
 65 as well addressed the temperature effect on the SISF energies for several Ni<sub>3</sub>Al-based sys-  
 66 tems, specifically:  $(Ni_{75-x}Co_x)Al_{25}$ ,  $(Ni_{75-x}Cu_x)Al_{25}$ ,  $(Ni_{75-x}Pd_x)Al_{25}$ ,  $(Ni_{75-x}Pt_x)Al_{25}$ .  
 67 However, our temperature-dependence results (section IV.B.3<sup>11</sup>) are preliminary, since they  
 68 did not involve local atomic relaxations of the D0<sub>19</sub> structure. Thereby, the SISF energies  
 69 temperature-dependence presented earlier<sup>11</sup> was tentative. In this work, we try to establish  
 70 the SISF energies variation as a function of temperature. The investigated alloys are those  
 71 recently<sup>11</sup> addressed:  $(Ni_{75-x}X_x)Al_{25}$  pseudo-binary system, where  $X = \text{Co, Cu, Pd or Pt}$ ,  
 72 and  $x = 4.62975, 9.2595, 13.88925$  and  $18.51825$  at. % X. We employ a combined scheme con-  
 73 sisting of DFT, the quasi-harmonic Debye (QHD) model, and the axial Ising model (AIM),  
 74 in conjunction with a quasistatic approach. Furthermore, we assess the effect of relaxations  
 75 on the overall results by applying two distinct schemes: full internal relaxation where atoms  
 76 within the structure are allowed to relax to their lowest energy position, and internally static  
 77 whereby the positions of atoms are kept fixed within the structures.

## 78 II. COMPUTATIONAL METHOD

79 We combine DFT calculations with the AIM and the QHD model in order determine  
 80 the temperature dependence of SISF energies in L1<sub>2</sub> Ni<sub>3</sub>Al-based alloys. This paper does

81 not focus on the methodology behind both models, nor on their advantages/disadvantages  
 82 relative to other approaches (Supercell method and phonon calculations). However, we will  
 83 adequately introduce the main formalisms of both AIM and QHD models that helped us to  
 84 have direct access into SISF energies and their thermal dependence. For more details, the  
 85 reader is referred to Refs. 11 and 12 and references therein.

## 86 A. AIM model

87 We employ the axial nearest-neighbor Ising model (ANNI) which is the first-order ap-  
 88 proximation of the AIM model. The (111) SISF formation energy of L1<sub>2</sub> alloys using the  
 89 ANNI model is given by:

$$90 \quad \gamma_{\text{ANNI}}^{L1_2} = \frac{8(E_{D0_{19}} - E_{L1_2})}{V_{L1_2}^{2/3} \cdot \sqrt{3}}, \quad (1)$$

91 where  $V_{L1_2}$  is the volume of 4-atoms L1<sub>2</sub> unit cell and  $V_{L1_2}^{2/3} \cdot \sqrt{3}$  is the area of 4-atoms in the  
 92 L1<sub>2</sub> (111) plane over which the stacking fault extends.  $E_{L1_2}$  and  $E_{D0_{19}}$  are the energies per  
 93 atom of the L1<sub>2</sub> and D0<sub>19</sub> structures.

## 94 B. QHD model

95 The QHD model is able to establish the equation of state of a solid, *i.e.*, the volume  
 96 temperature-dependence  $V=f(T)$  where  $V$  is the equilibrium volume at a given temperature  
 97  $T$ . This is achieved through minimizing the non-equilibrium Gibbs function as:

$$98 \quad \left( \frac{\partial G^*}{\partial V} \right)_{T,P} = 0, \quad (2)$$

99 where

$$100 \quad G^*(T, P, V) = E_e(V) + PV + A_{vib}(T, V). \quad (3)$$

101  $E_e$  is the total energy of the system at a given volume  $V$ , calculated using the DFT.  $P$  is  
 102 the ambient pressure,  $A_{vib}(T, V)$  is the Helmholtz vibrational energy term. This term is the  
 103 core-element of the model as it consists of an approximation of the vibrational density of  
 104 states (DOS) known as Debye's phonon DOS. The minimization of  $G^*$  is implemented in  
 105 the **gibbs** code<sup>13</sup>.

106 Let's mention here that the computational method presented here was used recently<sup>11</sup> to

107 calculate a preliminary temperature-dependence of SISF energies in L1<sub>2</sub> Ni<sub>3</sub>Al-based alloys,  
 108 with the exception that in this study we take into account the local atomic relaxations  
 109 of the D0<sub>19</sub> phase, which makes the approach more robust and complete in establishing  
 110 qualitatively and quantitatively the desired thermal dependence.

### 111 C. Supercell modeling and first-principles techniques

112 The Ni<sub>75-x</sub>X<sub>x</sub>Al<sub>25</sub> alloy was modeled using 108-atom L1<sub>2</sub>-based 3×3×3(×4-atoms) and  
 113 216-atom D0<sub>19</sub>-based 3×3×3(×8-atoms) supercells. The transition metal ternary element X  
 114 (Co,Cu,Pd,Pt) occupy exclusively the Ni-sites as the latter manifest strong site-preference  
 115 to the Ni-sublattice<sup>14-17</sup>. In our study, the alloy compositions fall within the experimen-  
 116 tal solubility of X in Ni<sub>3</sub>Al alloys<sup>14</sup>. The used supercells were generated to satisfy the  
 117 chemical disorder on the Ni-sublattice where the Warren-Cowley short-range order (SRO)  
 118 parameters<sup>18,19</sup> were minimized at several nearest neighbor coordination shells.

119 The first-principles calculations were performed using the Density-functional theory DFT<sup>20,21</sup>  
 120 as implemented in the Vienna Ab initio Simulation Package (VASP)<sup>22-24</sup>, which employs  
 121 the Projector Augmented Wave PAW method to determine the total energies and forces.  
 122 The exchange-correlation (XC) energy of electrons is described in the generalized gradient  
 123 approximation (GGA) using the functional parameterization of Perdew-Burke-Ernzerhof<sup>25</sup>.  
 124 The energy cut-off was set to 400 eV. A mesh of a 112 and 63 special **k**-points for 108-  
 125 Atom L1<sub>2</sub> and 216-Atom D0<sub>19</sub> phases, respectively, were taken in the irreducible wedge of  
 126 the Brillouin zone for the total energy calculations. These input parameters stabilized the  
 127 energy differences between L1<sub>2</sub> and D0<sub>19</sub> phases and guaranteed the uncertainty in SISF  
 128 energy to be less than 2 mJ/m<sup>2</sup>.

129 During relaxation of the L1<sub>2</sub> phase, the supercell shape was kept fixed. Only volume and  
 130 atomic positions were allowed to change in order to fully minimize the total energy. This  
 131 technique prevents the L1<sub>2</sub> supercell from deviating to a low symmetric phase.

132 Concerning the D0<sub>19</sub> phase, only local atomic relaxations were allowed. The D0<sub>19</sub> volume-  
 133 per-atom was intentionally set to the corresponding L1<sub>2</sub> equilibrium value, while the *c/a*  
 134 ratio was kept constant at the D0<sub>19</sub> ideal value. This insured that  $a_{D0_{19}}$  and  $c_{D0_{19}}$  corre-  
 135 spond to the underlying L1<sub>2</sub> lattice, *i.e.*,  $a_{D0_{19}}/a_{L1_2} = \sqrt{2}$  and  $c_{D0_{19}}/a_{L1_2} = \sqrt{4/3}$ . For  
 136 both phases, the local atomic relaxations were carried out using the conjugate gradient

137 algorithm<sup>26</sup>, a powerful scheme commonly used to relax the atoms into their instantaneous  
138 ground state.

### 139 III. RESULTS

140 The (111) SISF energy temperature dependence in L1<sub>2</sub> Ni<sub>3</sub>Al-based alloys is calculated  
141 through a combined DFT-AIM-QHD approach. Let us mention here that this approach  
142 is quasistatic since the temperature-dependence of the SISF energy is obtained through a  
143 DFT calculation of the of L1<sub>2</sub> and D0<sub>19</sub> energies at a volume  $V$  corresponding to a sought-  
144 after temperature  $T$ . Hence, it becomes clear now that this approach assumes that the  
145 temperature-dependence of SISF energies is attributed only to thermal expansion *i.e.*, other  
146 thermal effects, namely, electronic, vibrational and magnetic thermal excitations are not  
147 accounted for.

148 The SISF energy temperature-dependence is realized by firstly feeding the **gibbs** code<sup>13</sup>  
149 a set of L1<sub>2</sub> Energy-Volume values being determined with VASP code as demonstrated  
150 above. **gibbs** will search for an equilibrium volume that minimizes the non-equilibrium  
151 Gibbs energy at a given temperature, hence volume temperature-dependence of lattice L1<sub>2</sub>  
152 is established. Then, upon selecting a desired temperature  $T$ , we simulate the D0<sub>19</sub> energy  
153 with VASP at the corresponding equilibrium volume. Finally, the SISF energy corresponding  
154 to a temperature  $T$  is evaluated using the AIM model as expressed by Eq. 1  
155 Several experimental reports<sup>27-29</sup> back this quasistatic approach. It has been shown to  
156 be effective in calculating the elastic constants of Ni<sub>3</sub>Al<sup>30,31</sup>. It has been as well shown  
157 to be successful when calculating the elastic constants of Ta<sup>32</sup> where thermal expansivity  
158 was the dominant temperature contribution, while other thermal effects such as phonon  
159 and electronic excitation contributions were found to be quite minor at constant volume.  
160 Of particular importance to this study is the recent success in applying this approach to  
161 calculate the SISF energies in unaries<sup>33</sup>, pure compounds<sup>12</sup> and alloys<sup>34</sup> characterized by  
162 complex magnetic structures.

166 Figs. 1, 2, 3 and 4 present the SISF energy temperature dependence of the L1<sub>2</sub> Ni<sub>75-x</sub>Co<sub>x</sub>Al<sub>25</sub>,  
167 Ni<sub>75-x</sub>Cu<sub>x</sub>Al<sub>25</sub>, Ni<sub>75-x</sub>Pd<sub>x</sub>Al<sub>25</sub> and Ni<sub>75-x</sub>Pt<sub>x</sub>Al<sub>25</sub> alloys, respectively. Some of the compo-  
168 sitions studied, taking into account the volume relaxation only (*i.e.*, with atomic positions  
169 fixed, as in the left panels of Figs. 1-4), have been preliminarily reported by us<sup>11</sup>. The

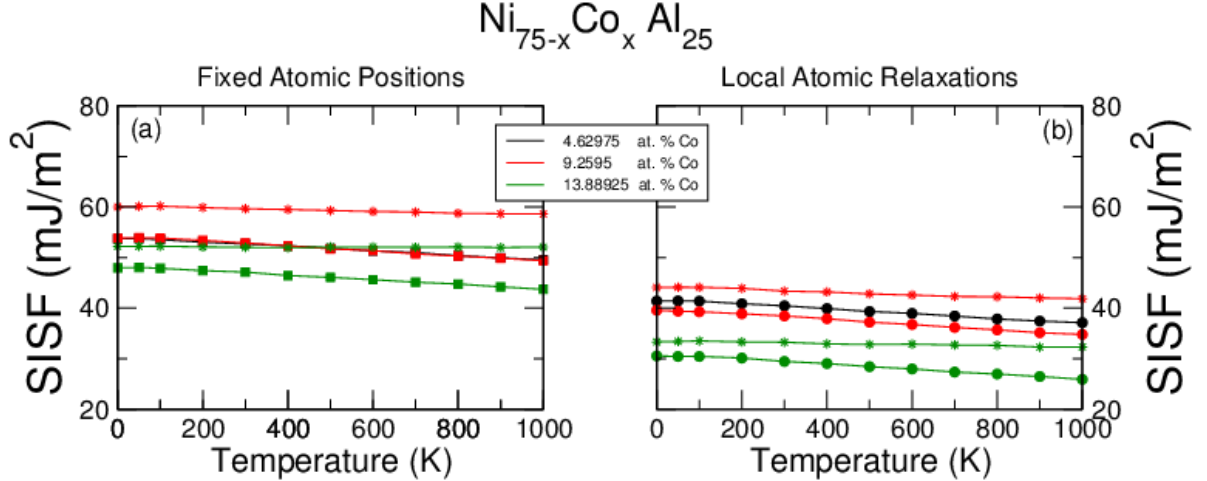


FIG. 1. Variation of the SISF energies as a function of temperature for the System  $L1_2$   $Ni_{75-x}Co_xAl_{25}$ . Panels (a) and (b) stand for fixed atomic positions and local atomic relaxations respectively. The star symbols designate spin-polarized calculations. In panel (a) the data corresponding to the composition 4.62975 at.% Co are not visible because they are extremely close to those of 9.2595 at.% Co. The lines going through the data are purely for visual reasons.

170 first thing to notice upon analyzing the results is the significant reduction in SISF energies  
 171 upon performing local atomic relaxations observed in all compositions and systems. It  
 172 is worth mentioning at this point that the values predicted with local-atomic-relaxation  
 173 scheme should be more close to the experimental values. The magnitude of the reduction  
 174 varies significantly between the studied systems and across the alloying compositions. The  
 175 reduction is highly pronounced in  $Ni_{75-x}Pd_xAl_{25}$  and  $Ni_{75-x}Pt_xAl_{25}$ , and less pronounced  
 176 in  $Ni_{75-x}Co_xAl_{25}$  and  $Ni_{75-x}Cu_xAl_{25}$ . For the sake of comparison, consider the composition  
 177 13.88925 at. %. Given this composition, the average difference (across temperature) between  
 178 volume and local-atomic-relaxation schemes reaches a value as large as 138  $mJ/m^2$  when  
 179 substituting Ni by Pt, to be compared with 26  $mJ/m^2$  when substituting Ni by Cu.

180 The drop in the calculated SISF energies due to inclusion of atomic relaxations can be  
 181 explained in terms of the size-argument *i.e.*, the atomic-radius mismatch. If we consider the  
 182 system  $Ni_{75-x}Pt_xAl_{25}$ , Pt atoms characterized by large Wigner-Seitz (WS) radii (1.5319 Å)  
 183 are substituting small Ni atoms (WS=1.3756 Å) and this atomic-size mismatch is responsi-  
 184 ble for important atomic relaxations leading the system into its lowest energy configuration  
 185 which is very much different from that of fixed-atomic-positions calculations. While, Cu



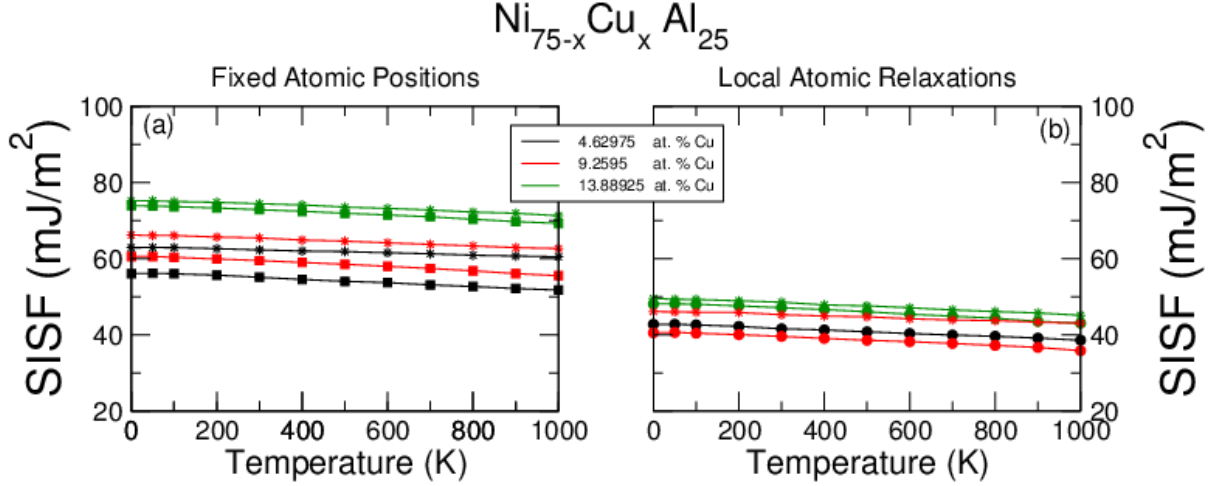


FIG. 2. Change of SISF energies upon temperature increase in the system  $L1_2 \text{Ni}_{75-x}\text{Cu}_x\text{Al}_{25}$ . Panels (a) and (b) stand for fixed atomic positions and local atomic relaxations respectively. The star symbols designate spin-polarized calculations. The lines going through the data are purely for visual reasons.

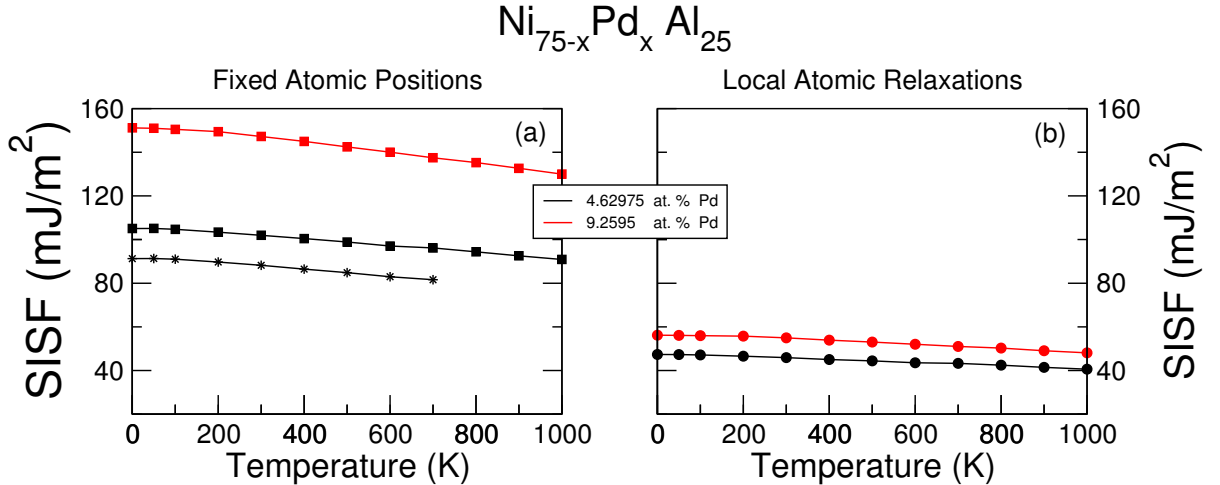


FIG. 3. Temperature dependence of SISF energies in  $L1_2 \text{Ni}_{75-x}\text{Pd}_x\text{Al}_{25}$ . Panels (a) and (b) stand for fixed atomic positions and local atomic relaxations respectively. The star symbols indicate spin-polarized calculations. The lines connecting the points are only to help guiding the eyes through the data.

186 characterized by  $WS=1.4107 \text{ \AA}$  which is not much larger than Ni ( $WS=1.3756 \text{ \AA}$ ), hence  
 187 the effect of local-atomic-relaxations is less pronounced in comparison with systems having  
 188 Pt and Pd ( $1.52 \text{ \AA}$ ) as alloying elements. We need to emphasize here that we have derived

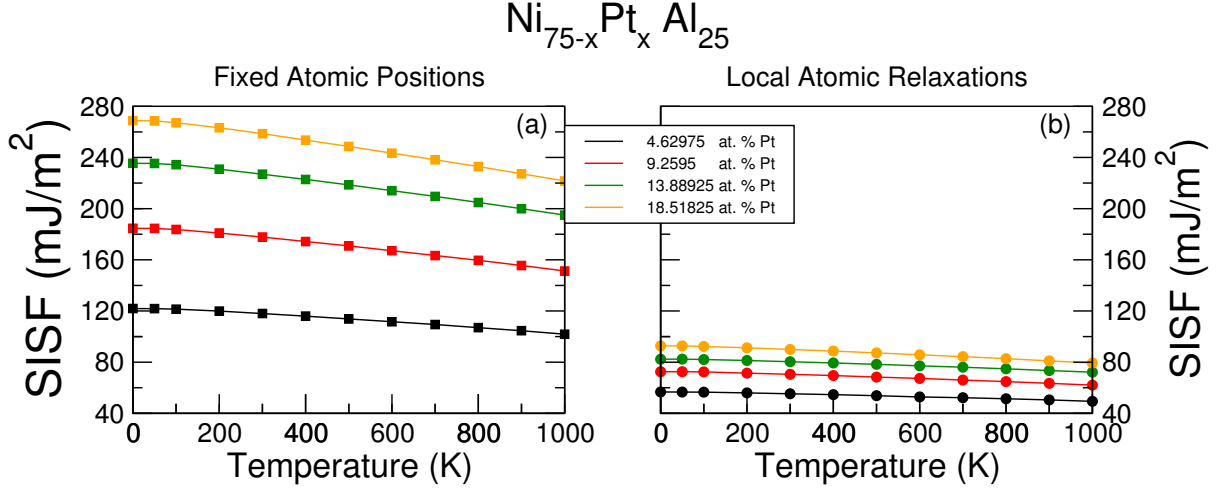


FIG. 4. Temperature dependence of SISF energies in  $L1_2$   $\text{Ni}_{75-x}\text{Pt}_x\text{Al}_{25}$ . Panels (a) and (b) stand for fixed atomic positions and local atomic relaxations respectively. The lines connecting the points are only to help guiding the eyes through the data.

189 the equilibrium Wigner-Seitz radii (WS) from the room temperature (R.T.) experimental  
 190 atomic volumes<sup>35</sup> ( $V_{exp}^{RT} = \frac{4}{3}\pi WS^3$ ) of the alloying element ground state structure.  
 191 On the other hand, the variation of the local-atomic-relaxation SISF energies upon increas-  
 192 ing temperature exhibits a small linear decrease relative to 0 K values for the whole studied  
 193 compositions. The magnitude of this decrease barely reaches 10 mJ/m<sup>2</sup> at its maximum.  
 194 In fact, in our previous investigation<sup>11</sup> we have shown that the change in SISF energies as  
 195 a function of alloying compositions, upon allowing local-atomic-relaxations, for the solutes  
 196 Co, Cu, Pd and Pt is not significant, which is in contrast to the large increase induced by  
 197 solutes substituting for Al sites. Consequently, it follows from the results presented here  
 198 and Ref.<sup>11</sup> that both alloying and temperature effects have little impact on changing the  
 199 SISF energies in  $\text{Ni}_{75-x}\text{X}_x\text{Al}_{25}$  alloys.

#### 200 IV. CONCLUSIONS

201 A combined computational scheme consisting of DFT, QHD and AIM in conjunction with  
 202 a quasistatic approach enabled us to establish the temperature-dependence of SISF energies  
 203 in  $L1_2$   $\text{Ni}_{75-x}\text{X}_x\text{Al}_{25}$  alloys. We find that a proper relaxation of both  $L1_2$  and  $D0_{19}$  phases  
 204 is indispensable to predict a reliable estimation of the SISF energies. Our results, without  
 205 an exception, all display a linear decline of the SISF energies as a function of composition.

206 Interestingly, this decline is very modest, in average it is less than 10 mJ/m<sup>2</sup> (SISF value  
207 at 1000 K relative to 0 K). This insignificant decrease in SISF energies and consequently  
208 the minor effect of temperature on the 0 K value is motivating, as it reduces drastically  
209 the computational cost required to calculate the SISF energies at every single temperature.  
210 Hence, it seems plausible to consider the 0 K SISF energy of a L1<sub>2</sub> multicomponent alloy  
211 (Ni,Cu,Pd,Pt)<sub>75</sub>Al<sub>25</sub> valid to use in physics-based deformation models<sup>36</sup> needed to predict  
212 primary creep of Ni-superalloys at their operating temperature. We assert that this conclu-  
213 sion is only valid for alloying elements substituting for Ni-sites, and therefore can not be  
214 extended to include elements substituting for Al-sites. We also emphasize that our SISF  
215 energy temperature-dependence is based on volume expansion as the only thermal effect.

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## List of figure captions

275 Figure 1: Variation of the SISF energies as a function of temperature for the System  
276  $L1_2 Ni_{75-x}Co_xAl_{25}$ . Panels (a) and (b) stand for fixed atomic positions and local atomic  
277 relaxations respectively. The star symbols designate spin-polarized calculations. In panel  
278 (a) the data corresponding to the composition 4.62975 at.% Co are not visible because they  
279 are extremely close to those of 9.2595 at.% Co. The lines going through the data are purely  
280 for visual reasons.

281 Figure 2: Change of SISF energies upon temperature increase in the system  $L1_2 Ni_{75-x}Cu_xAl_{25}$ .  
282 Panels (a) and (b) stand for fixed atomic positions and local atomic relaxations respectively.  
283 The star symbols designate spin-polarized calculations. The lines going through the data  
284 are purely for visual reasons.

285 Figure 3: Temperature dependence of SISF energies in  $L1_2 Ni_{75-x}Pd_xAl_{25}$ . Panels (a) and  
286 (b) stand for fixed atomic positions and local atomic relaxations respectively. The star  
287 symbols indicate spin-polarized calculations. The lines connecting the points are only to  
288 help guiding the eyes through the data.

289 Figure 4: Temperature dependence of SISF energies in  $L1_2 Ni_{75-x}Pt_xAl_{25}$ . Panels (a) and  
290 (b) stand for fixed atomic positions and local atomic relaxations respectively. The lines  
291 connecting the points are only to help guiding the eyes through the data.