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An improved multi-objective discrete Bees algorithm for robotic

disassembly line balancing problem in remanufacturing

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Abstract Remanufacturing is an effective way to realize the reutilization of resources. Disassembly, as an essential step of remanufacturing, is usually finished by manual work which is low efficiency and high labor cost. Robotic disassembly provides an alternative way to reduce labor intensity and disassembly cost. Disassembly line is an efficient method to deal with end-of-life products on a large scale. To balance the workload of robotic workstations is the main objective of robotic disassembly line balancing problem. In this paper, an improved multi-objective discrete Bees algorithm is proposed to solve robotic disassembly line balancing problem. The feasible disassembly sequence is obtained by space interference matrix method. It is used to generate robotic disassembly line solution by robotic workstation assignment method. After that, the multi-objective robotic disassembly line balancing problem is proposed. With the help of efficient non-dominated Pareto sorting method, improved multi-objective discrete Bees algorithm is proposed to find Pareto optimal solutions. Based on a gear pump and a camera, the performance of improved multi-objective discrete Bees algorithm is analyzed under different parameters and compared with the other optimization algorithms. In addition, Pareto fronts of robotic disassembly line balancing problem are also compared with those of the other two cases. The result shows the proposed method can find better quality of solutions using comparable running time compared with the other optimization algorithms.

Keywords Remanufacturing • Robotic disassembly line balancing problem • Improved multi-objective discrete bees algorithm • Robotic disassembly • Optimization problems

1. Introduction

Traditional manufacturing industry has the disadvantages of high environmental pollution and low resource utilizations. Under this condition, sustainable manufacturing [1] and remanufacturing [2, 3] are the future trends of manufacturing industry. In China, according to statistics, there are approximately 5 million cars, 20 million mobile phones and 500 million tons of solid waste to be scrapped every year [4].

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Products are usually incinerated or buried after exceeding the service life. This always leads to resource waste and environmental pollution. Remanufacturing, which aims to recover the size and performance of used products [5], closes the materials loop and forms a closed-loop manufacturing system. According to statistics, the energy and resource consumption of remanufacturing a product are respectively a half and seven tenths of manufacturing a new one [6]. Thus, remanufacturing provides an economically and environmentally sound way to realize sustainable developments of manufacturing industry [7, 8]. In all steps of remanufacturing, disassembly is an inevitable process to handle end-of-life products (EoLP) [9-11]. Due to the uncertainty of EoLP's quality, traditional disassembly process is always finished by manual works [12]. To reduce labor intensity, much attention has been paid to robotic disassembly [13, 14]. The cognitive robotics used for robotic disassembly was proposed to handle uncertainties in the dynamic disassembly process [12]. Afterwards, the basic behavior control [8] and learning/revision strategies [15] of cognitive robotics were proposed to disassemble the liquid-crystal display (LCD) screens.

Successful production planning helps to improve capacity utilization [16, 17]. In the production planning process, a well-designed assembly/disassembly line [18] helps to improve production efficiency. The assembly/disassembly line balancing problem is a non-negligible problem for the assembly/disassembly line. The key problem of line balancing problem is to assign manufacturing tasks to a set of workstations in a balanced way [10]. Disassembly line consists of several disassembly workstations which are assigned different disassembly tasks [19]. The core objective of disassembly line balancing problem (DLBP) is to balance the workload of workstations. To find optimal disassembly line balancing solution of an EoLP with n parts, it requires investigating all the permutations of disassembly sequence (n! possible solutions). Searching this solution space is bounded by exponential time. The decision version of DLBP has been proven to be NP-complete problem and its optimization version is NP-hard problem [20]. Many researchers have studied DLBP. To disassemble smart phones, a linear physical programming method was proposed to balance the mixed-model disassembly line [21]. Based on a cell phone which contains 25 parts, Ding et al. [22] used multi-objective ant colony algorithm to simultaneously minimize the number of workstation, the demand rating and the measure of balance. After that, to optimize the balancing index and the design cost of disassembly line, genetic algorithm was used to find the optimal solutions of stochastic DLBP [23]. The reinforcement learning algorithm was also used to solve multi-objective DLBP within reasonable computation time [24]. Bentaha et al. [25] used known probability distributions to describe the disassembly task time and solved DLBP by two-stage stochastic linear mixed integer program and sample average approximation method. To minimize the number of workstations, Hezer et al. [26] used the shortest route model to solve parallel DLBP. Considering the uncertainties in disassembly process, hybrid discrete artificial bee colony algorithm was proposed to solve fuzzy DLBP [27]. To find optimal disassembly line balancing solutions within reasonable computation time, Mete et al. [28] used beam search algorithm to minimize the number of workstations. Recently, sequence-dependent DLBP (SDDLBP) is gradually paid more attention. In SDDLBP, if task A interacts with another task B (such as physical obstruction etc.), additional disassembly time should be considered. Kalayci et al. [29] used ant colony optimization to minimize the number of workstation, the demand rating, hazardous rating and balancing index of disassembly line. Particle swarm optimization algorithm with neighborhood-based mutation operator was also used to find multi-objective optimal solutions of SDDLBP [30]. Improved artificial bee colony algorithm was used to find optimal disassembly line balancing solutions with minimum environmental impact and maximum profit [31]. After that, tabu search [32], hybrid genetic [33] and artificial bee colony [34] algorithms were used to solve SDDLBP.

The robotic disassembly line is different from manual disassembly line. For manual disassembly line, the working efficiency of each workstation is influenced by the workload while for robotic disassembly line, it is not. In addition, in manual disassembly line, current researches always ignore the moving time between different parts in each workstation. When robotic disassembly line balancing problem (RDLBP) is considered, the moving path of industrial robot's end-effector should be considered to avoid obstacles caused by the contour of EoLP. However, it is always ignored in the existing researches. Until now, there is no research studies RDLBP. But there are similar researches in robotic disassembly sequence planning. Based on the personal computer, Alshibli et al. [35] used tabu search and genetic algorithm to find optimal disassembly sequence with minimum disassembly time. ElSayed et al. [36] used genetic algorithm to solve robotic disassembly sequencing problem and an intelligent disassembly cell was also proposed [37]. Based on the personal computer, an online genetic algorithm was used to minimize the total disassembly time [38]. Generally, the moving time of industrial robot's end-effector between different parts should be a part of total disassembly time for each workstation. However, in the aforementioned methods, the moving time is calculated by Euclidean distance between different parts and the moving speed of industrial robot's end-effector. It ignores obstacle caused by the contour of EoLP. When robotic disassembly is considered, the obstacle-avoiding path of industrial robot's end-effector should be considered.

Many meta-heuristic algorithms are used to solve DLBP such as genetic algorithm [20], ant colony optimization [39], *etc.* It is the first application of BA to solve RDLBP. BA is derived from the foraging behavior of bees and has been successfully applied in many fields. The Pareto-based multi-objective Bees algorithm (MOBA) was used to solve welded beam design problem [40]. To maximize the slackness index and the efficiency of the assembly line, BA was used to solve two-sided assembly line balancing problem under constrained fuzzy environment [41]. Ercin et al. [42] used multi-objective BA and artificial Bees colony algorithm to solve proportional-integral-derivative (PID) tuning problems. To minimize the total lead-time and the total cost, BA was used to find optimal configuration of supply chain networks [43]. Lu et al. [44] used BA to solve quality-of-experience (QoE) based spectrum allocation optimization problem of cognitive radio networks. Based on motorcycle assembly process, Xu et al. [45] used multi-objective BA to solve correlation-aware service aggregation optimization problem. The performance of BA was compared with multi-objective genetic algorithm and multi-objective particle swarm optimization algorithm.

DLBP is multi-objective optimization problem which can be solved by lexicographical optimization methods, objective weighting optimization methods and Pareto based optimization methods [46]. Comparing with the former two methods, Pareto based multi-objective optimization method treats all the objectives equally and provides several non-dominated solutions for the decision-makers to choose. However, recently, most of optimization algorithms used for solving DLBP is lexicographic-based multi-objective optimization algorithms [32-34] and few studies have reported Pareto-based multi-objective optimization algorithms to solve DLBP.

The major contribution of this paper is to solve robotic disassembly line balancing problem which has not been studied yet. Until now, no research considers the moving time between different parts as a part of total working time of robotic workstation, which can be calculated by the obstacle-avoiding path and moving speed of industrial robot's end-effector. In this paper, the significance and related works are discussed in section 1. The notations used in this paper are summarized in Section 2. In Section 3, disassembly model is built by space interference matrix method (SIMM) and robotic disassembly line solution is obtained by robotic workstation assignment method. In Section 4, multi-objective robotic disassembly line balancing problem is described. Then, improved multi-objective discrete Bees algorithm (IMODBA) are introduced in Section 5. In Section 6, case studies based on a gear pump and a camera are used to verify the effectiveness of proposed method and conclusions are drawn in Section 7.

2. Notation

Α	Allocation matrix used for robotic workstation assignment method
bt	Basic disassembly time
bdn	Number of solutions which dominate the provided solution
CT	Cycle time of robotic disassembly line
D_{set}	A set of solutions which is dominated by the provided solution
d_i	The Euclidean distance between i th member of obtained non-dominated solutions and its
	nearest member of Pareto optimal solutions
dt	The direction-change time
FSeq	Feasible disassembly sequences generated by SIMM
Fr	Set of Pareto rankings
Fr_i	Pareto ranking <i>i</i>
h_{pi}	Demand; quantity of part p_i requested
iter	Iteration number
т	Number of robotic workstation
md	Length of moving path between different disassembly parts
ms	Moving speed of industrial robot's end-effector
mt	Moving time between different disassembly parts
п	Number of parts in an EoLP
nd	Number of non-dominated solutions
nes	Number of elite sites
ns	Number of selected sites
Р	Population set
P^{*}	Sorted population set
P_{Fr}	Pareto sorted population set
rnes	Number of follower bees around elite sites
rns	Number of follower bees around non-elite selected sites
scou	tn Number of scout bee
Seq	Disassembly sequences
S_d	Space interference matrix ($d = x+, x-, y+, y-, z+, z-$)
$S_{x,y,z}$	Integrated space interference matrix
t _{i,total}	Total working time of i^{th} robotic workstation
t_{pi}	Basic disassembly time for part p_i
tta, ti	t Tool-change time

3. Disassembly model for EoLP

The disassembly model is always built by graph-based method [47, 48], Petri Net method [49] and matrix-based method [50, 51], *etc.* For robotic disassembly, feasible disassembly direction of each part should be provided for industrial robots. In this paper, SIMM [50, 51] which consists of space interference matrix and interference matrix analysis is used to generate feasible disassembly sequence and

disassembly direction.

3.1 Space interference matrix

Firstly, six interference matrices along six directions (x+, x-, y+, y-, z+ and z-) are described by Equation (1).

In the matrix S_d , element $s_{i,j}$ means whether component C_i can be removed along d direction (d = x+, x-, y+, y-, z+ or z-) when component C_j exists. If component C_i can be removed along d direction when component C_j exists, element $s_{i,j}$ in the matrix S_d is 0. Otherwise, it is 1. As shown in Figure 1, six interference matrices of this example are described by Equation (2). For instance, in the matrix S_{z+} , element s_{AG} is 0, because bolt A can be removed along z+ direction by unscrewing operation although component G has contact relationships with bolt A. In the matrix S_{z-} , element s_{GA} is 1, it is because component G cannot be removed along z- direction when bolt A exists.

$$S_{d} = \begin{bmatrix} C_{1} & C_{2} & \dots & C_{n} \\ C_{1} \begin{bmatrix} s_{1,1} & s_{1,2} & \dots & s_{1,n} \\ s_{2,1} & s_{2,2} & \dots & s_{2,n} \\ \dots & \dots & \dots & \dots \\ C_{n} \begin{bmatrix} s_{n,1} & s_{n,2} & \dots & s_{n,n} \end{bmatrix} & x + or \ x - d = or \ y + or \ y - or \ z + or \ z - or \ z + or \ z - d = or \ y + or \ z - d = or \ y + or \ z - d = or \ y + or \ z - d = or \ z + or$$





		A	В	С	D	Ε	F	G	Η			A	В	С	D	Ε	F	G	Η	
	A	0	0	0	1	0	0	1	1		A	0	0	0	0	0	0	1	1]	
	В	0	0	1	0	0	0	1	1		В	0	0	0	0	0	0	1	1	
	С	0	0	0	0	0	0	1	1		С	0	1	0	0	0	0	1	1	
c	D	0	0	0	0	0	0	1	1	c	D	1	0	0	0	0	0	1	1	
$S_{x+} =$	E	0	0	0	0	0	0	1	1	<i>S</i> _{<i>x</i>} =	E	0	0	0	0	0	1	1	1	
	F	0	0	0	0	1	0	1	1		F	0	0	0	0	0	0	1	1	
	G	1	1	1	1	1	1	0	0		G	1	1	1	1	1	1	0	0	
	Η	1	1	1	1	1	1	0	0		Η	1	1	1	1	1	1	0	0	

		A	В	С	D	Ε	F	G	Η		A	В	С	D	Ε	F	G	Η
	A	0	0	0	0	0	0	1	1]	A	0	0	0	0	0	0	1	1
	B	0	0	0	0	0	0	1	1	В	0	0	0	0	0	1	1	1
	C	0	0	0	0	0	0	1	1	C	0	0	0	0	1	0	1	1
s -	D	0	0	0	0	0	0	1	1	s^{-L}	0	0	0	0	0	0	1	1
ы _{y+} -	\overline{E}	0	0	1	0	0	0	1	1	$S_{y-} E$	0	0	0	0	0	0	1	1
	F	0	1	0	0	0	0	1	1	F	0	0	0	0	0	0	1	1
	G	1	1	1	1	1	1	0	0	G	1	1	1	1	1	1	0	0
	H	1	1	1	1	1	1	0	0	H	[1	1	1	1	1	1	0	0
		A	В	С	D	Ε	F	G	Η		A	В	С	D	Ε	F	G	Η
	A	A 0	В 0	С 0	D 0	Е 0	F 0	$G \\ 0$	H 0	A	$A = \begin{bmatrix} 0 \end{bmatrix}$	В 0	С 0	D 0	Е 0	F0	G1	H 1
	A B	A 0 0	В 0 0	C 0 0	D 0 0	E 0 0	F 0 0	G 0 0	H 0 0	A B	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	В 0 0	C 0 0	D 0 0	E 0 0	F 0 0	G 1 1	H 1 1
	$ \begin{array}{c} A \\ B \\ C \end{array} $	A 0 0	B 0 0 0	C 0 0	D 0 0	E 0 0	F 0 0	G 0 0	$ \begin{bmatrix} H \\ 0 \\ 0 \\ 0 \end{bmatrix} $	A B C	$ \begin{array}{c} A \\ 0 \\ 0 \\ 0 \end{array} $	B 0 0 0	C 0 0	D 0 0	E 0 0	F 0 0	G 1 1 1	H 1 1 1
s -	A B C D	A 0 0 0	B 0 0 0 0	C 0 0 0 0	D 0 0 0	E 0 0 0	F 0 0 0	G 0 0 0	$ \begin{array}{c} H \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} $	A B C $S = D$	$ \begin{array}{c c} A \\ \hline 0 \\ 0 \\ 0 \\ 0 \end{array} $	B 0 0 0	C 0 0 0	D 0 0 0	E 0 0 0	F 0 0 0	G 1 1 1	H 1 1 1 1
<i>S</i> _{z+} =	$ \begin{array}{c} A\\B\\C\\D\\E\end{array} \end{array} $	A 0 0 0 0	B 0 0 0 0 0	C 0 0 0 0 0	D 0 0 0 0	E 0 0 0 0	F 0 0 0 0	G 0 0 0 0	H 0 0 0 0 0	A B C $S_{z-} = \frac{D}{E}$	$ \begin{array}{c} A \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} $	B 0 0 0 0	C 0 0 0 0 0	D 0 0 0 0	E 0 0 0 0	F 0 0 0 0	G 1 1 1 1	H 1 1 1 1 1
<i>S</i> _{z+} =	$ \begin{array}{c} A\\B\\C\\D\\E\\F\\\end{array} $	A 0 0 0 0 0 0	B 0 0 0 0 0 0	C 0 0 0 0 0 0	D 0 0 0 0 0	E 0 0 0 0 0	F 0 0 0 0 0	G 0 0 0 0 0	H 0 0 0 0 0 0	A B C $S_{z-} = D$ E F	$ \begin{array}{c} A \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} $	B 0 0 0 0 0 0	C 0 0 0 0 0 0	D 0 0 0 0 0	E 0 0 0 0 0	F 0 0 0 0 0	G 1 1 1 1 1 1	H 1 1 1 1 1 1
<i>S</i> _{z+} =	$ \begin{array}{c} A\\B\\C\\D\\E\\F\\G\end{array} \end{array} $	A 0 0 0 0 0 0 1	B 0 0 0 0 0 0 1	C 0 0 0 0 0 0 1	D 0 0 0 0 0 1	E 0 0 0 0 0 1	F 0 0 0 0 0 1	G 0 0 0 0 0 0	H 0 0 0 0 0 0 0 0	A B C $S_{z-} = \frac{D}{E}$ F G	$ \begin{array}{c} A \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{array} $	B 0 0 0 0 0 1	C 0 0 0 0 0 0 1	D 0 0 0 0 0 1	E 0 0 0 0 0 1	F 0 0 0 0 0 1	G 1 1 1 1 1 1 0	H 1 1 1 1 1 1 1

(2)

Step 1 A B C D E F G H Result	Step 2 A B C D E F G H
A 000000 000000 100000 100000 000000 000000	R 000000 000000 100000 000000 000000 11101 11101
	D 010000 000000 000000 000000 000000 000000
$S_{x,y,z,l} = \frac{B}{E} \begin{bmatrix} 0.00000 & 0.000000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.000000 & 0.00000 & 0.00000 & 0.000000 & 0.000000 & 0.00000000$	$S_{x,y,z,l} = \frac{1}{E} \begin{bmatrix} 0.00000 & 0.000000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.000000 & 0.000000 & 0.000000 & 0.00000000$
F 000000 001000 000000 000000 100000 0111101 111101 111101	F 000000 001000 000000 000000 100000 111101 111101
G 111111 111111 111111 111111 111111 1111	G 111111 111111 111111 111111 111111 1111
H 111111 111111 111111 111111 111111 1111	H 111111 111111 111111 111111 111111 1111
Ster 2 A B D F F G H Recult	
Step 5 1 2 2 1 0 11101 11101 11101	Step 4 A D D D D D D A A A A A A A A A A A A
B 000000 000000 000000 000000 111101 111101	R 000000 000000 000000 000000 000100 111101 111101
S - E 000000 000000 000000 000000 111101 111101	
$S_{x,y,\xi,2} = E$ 000000 000000 000000 000000 010000 111101 111101	$S_{x,y,z,2} = E$ 000000 000000 000000 000000 010000 111101
	F 000000 001000 000000 100000 000000 111101 111101
	G 111111 111111 111111 111111 111111 000000
	$H \begin{bmatrix} 111111 & 111111 & 111 \\ 1111 & 111111 & 111111 & 111111 & 000010 & 000000 \end{bmatrix}$
Step 5 A B E E C II D b	Step 6 A B F F G H
A B E F G H Result	
	A 000000 000000 000000 000000 111101 111101
	B 000000 000000 000000 000100 111101 111101
$S_{x,y;z} = \frac{E}{E} \begin{bmatrix} 000000 & 000000 & 000000 & 010000 & 111101 & 111101 \\ 000000 & 001000 & 000000 & 111101 & 111101 \\ 111101 & 111101 \\ 111101 & 111101$	$S = \frac{E}{2} \begin{bmatrix} 000000 & 000000 & 000000 & 010000 & 111101 & 111101 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$
F 000000 001000 100000 000000 111101 111101 111101	$S_{x,y,z,3} F$ 000000 001000 100000 000000 111101 111101
	G 111111 111 111 111111 111111 000000 000001
$H_{[111111}$ 111111 111111 111111 000010 000000] 111111	H 111111 1111111 111111 111111 000010 000000
Step 7	Step 8
A E F G H Result	A E F G H
A 000000 000000 000000 111101 111101 111101	A 000000 000000 000000 111101 111101
E 000000 000000 010000 111101 111101 111101	E 000000 000000 010000 111101 111101
$S_{\text{max}} = F 000000 100000 000000 111101 11101 11101 11100 11000 1100000 1100000 1100$	$S_{i} = F_{i}^{\dagger} 000000 100000 000000 111101 111101$
G 111111 111111 000000 000001 111111	$G_{x,y,z,4} = 1$ 000000 100000 111101 111101
	H[111]111 111111 111111 000010 000000]
Step 9	Step 10 E F G H
E F G H Kesun	
E[000000 010000 111101 111101] 111101	E 000000 010000 111101 111101
F 100000 000000 111101 111101 11110	$F = \frac{F}{100000 - 0000000 - 111101 - 111101}$
$S_{x,y,z,5} = c$	$G_{x,y,z,5} G$ 111111 1111111 000000 000001
G 111111 111111 000000 000001 111111	H 111111 111 H 111111 000010 000000
$H \begin{bmatrix} 111111 & 111111 & 000010 & 000000 \end{bmatrix} $ 111111	
Step 11	Step 12
E G H Result	F G H
E 000000 111101 111101 111101	E 000000 111101 111101
$S_{x,y,z,6} = G \begin{bmatrix} 111111 & 000000 & 000001 \\ 111111 \end{bmatrix}$	$S_{max} = G \begin{bmatrix} 111\\111\\000000\\000001 \end{bmatrix}$
H 111111 000010 000000 1111111	X, y, z, b
Step 13	Step 14
G H Result	G H
	0 11
G = G 000000 000001 000001	$G \begin{bmatrix} 000000 & 000001 \end{bmatrix}$
$S_{x,y,z,7} = H 000010 000000 000010$	$S_{x,y,z,7} = \frac{1}{2}$
	H[000010 000000]

Fig. 2 A feasible disassembly sequence obtained by SIMM

3.2 Interference matrix analysis

Feasible disassembly sequence and disassembly direction are generated by space interference matrices and interference matrix analysis method. Based on the example used in Section 3.1, six space interference matrices are integrated to be matrix $S_{x,y,z,J}$ as shown in Figure 2. The column *Result* is obtained by step1 in Figure 2. The first element of column *Result* is 111101, the fifth bit '0' is obtained by 'OR' operator acted on the fifth bit of all the elements in the first row. Besides, bit '0' means corresponding part can be removed from given direction (the first bit for x+ direction, the second bit for

x- direction, the third bit for y+ direction, *etc.*). Otherwise, it cannot. For instance, the first element of column *Result* is 111101, the fifth bit is '0' while the other bits are '1'. It means bolt A can only be removed along z+ direction. Thus, in step 1, it is obvious that all the bolts A, B, C, D, E and F can be removed along z+ direction. If bolt C has been removed along z+ direction (the red circle in step 1), the corresponding row and column are deleted as shown in step 2. Under this condition, a new matrix $S_{x,y,z,2}$ is obtained as shown in step 3. It is also obvious that all the components A, B, D, E and F can be removed along z+ direction. If bolt D has been removed along z+ direction, the corresponding row and column are deleted as shown in step 2. Under this condition, a new matrix $S_{x,y,z,2}$ is obtained as shown in step 4. This procedure continues in the same manner as shown in steps 5 ~ 12. After bolts A ~ F have been removed, matrix $S_{x,y,z,7}$ is obtained in step 13. From the column of *Result* in step 13, it is obvious component G can be removed along x+, x-, y+, y- or z+ direction and component H can be removed along any direction of x+, x-, y+, y-, z+ or z- (direction z+ is chosen here). Thus, feasible disassembly sequence (C/D/B/A/F/E/G/H) is obtained and the corresponding disassembly direction is z+/z+/z+/z+/z+/z+.

4. Multi-objective robotic disassembly line balancing problem

Robotic disassembly line is the flow-oriented production system which consists of several robotic workstations. The disassembly tasks are consecutively launched down the line and EoLP is sequentially moved from one workstation to another. For each robotic workstation, disassembly operations are repeatedly performed within cycle time of robotic disassembly line. The decision problem of optimally assigning the disassembly tasks to different robotic workstations in a balanced way is defined as RDLBP.

4.1 Assumptions

In this paper, the following assumptions are made. Only single type of EoLP is disassembled on the robotic disassembly line. The structure and geometric information of EoLP are provided in advance so that industrial robot's end-effector can move along the predefined path. Each disassembly task is assigned to only one robotic workstation. The basic disassembly time, tool-change time and direction-change time are deterministic and constant [33]. All the EoLPs are used for complete disassembly. The total working time of robotic workstation should not exceed cycle time (CT) of robotic disassembly line.

4.2 Multi-objective formulation

The traditional DLBP only considers basic disassembly time of parts, tool-change time and direction-change time between different parts. The moving time between different parts is always ignored. When RDLBP is considered, the traditional method for solving DLBP is not applicable. The differences between DLBP and RDLBP are described in Figure 3.



Fig. 3 The differences between DLBP and RDLBP

In this paper, the multi-objectives of RDLBP are to simultaneously minimize the number of robotic workstations (f_1) , balance the workload of robotic workstations (f_2) and disassemble high demand parts as early as possible (f_3) as shown in Equations (3) ~ (5). Minimizing the number of robotic workstation helps to reduce the cost for enterprises. The second objective is used to ensure that idle time of robotic workstations is similar. It helps to level the workload of robotic workstations. Lower f_2 value means more similar idle time of robotic workstations. For the third objective, it means high demand parts should be disassembled as early as possible to reduce damage of high demand parts in the disassembly process. In this paper, lower f_3 value is more desirable [34].

$$\min f_1 = m \tag{3}$$

$$\min f_2 = \sum_{i=1}^{m} (CT - t_{i,total})^2$$
(4)

$$\min f_3 = \sum_{i=1}^n i^* h_{p_i}$$
(5)

Subject to:

 $Seq = (p_1, p_2, ..., p_n) \in FSeq$ (6)

$$\left[\frac{\sum_{i=1}^{n} t_{p_i}}{CT}\right] \le m \le n \tag{7}$$

$$t_{i,total} \le CT, \ i \in \mathbb{Z}, \ \forall i \in [0,m]$$
⁽⁸⁾

(9)

component p_i is only assigned to $RobWork_i$, $\forall i \in [0,m]$, $\forall j \in [0,n]$

In Equations (3) ~ (9), *m*, *n*, $t_{i,total}$ and h_{pj} respectively represent the number of robotic workstation, the number of parts in EoLP, the total working time of *i*th robotic workstation and the demand value of part p_j . *CT* is the cycle time of robotic disassembly line which is predefined in this paper. *FSeq* means the feasible disassembly sequences generated by SIMM. Equation (6) ensures that the disassembly sequence is feasible. Equation (7) guarantees the number of workstation is limited within permitted values. Equation (8) ensures the total working time of any robotic workstation should not exceed cycle time of robotic disassembly line and Equation (9) means any disassembly task should be assigned to only one robotic workstation.

For the moving time between different parts, strictly, it is influenced by not only the position of EoLP in the robot workspace, but also the type of industrial robot and the complexity of EoLP. In this paper, for simplicity, the moving time $(m_{i,j})$ is calculated by the length of moving path between part *i* and part *j* $(md_{i,j})$ and the moving speed (ms) of industrial robot's end-effector which is assumed to be constant. Besides, safe distance between the contour of EoLP and moving path of industrial robot's end-effector is also considered to protect industrial robot's end-effector from collision as shown in Figure 4. For the disassembly sequence '3-4-8-2-6-7-5-1', to calculate the moving distance between part 3 and part 4 $(md_{3,4})$ and the moving distance between part 3 and part 8 $(md_{3,8})$ are manually calculated by Equation (11). Hence, the corresponding moving time $(mt_{3,4} \text{ and } mt_{3,8})$ is calculated by the moving distance $(md_{3,4} \text{ and } md_{3,8})$ and the moving speed (ms).



Fig. 4 The moving path between different parts

	0	$md_{1,2}$	$md_{1,3}$	$md_{1,4}$	$md_{1,5}$	$md_{1,6}$	$md_{1,7}$	$md_{1,8}$
	$md_{2,1}$	0	$md_{2,3}$	$md_{2,4}$	$md_{2,5}$	$md_{2,6}$	$md_{2,7}$	md _{2,8}
	<i>md</i> _{3,1}	$md_{3,2}$	0	$md_{3,4}$	$md_{3,5}$	$md_{3,6}$	$md_{3,7}$	<i>md</i> _{3,8}
MD	$md_{4,1}$	$md_{4,2}$	$md_{4,3}$	0	$md_{4,5}$	$md_{4,6}$	$md_{4,7}$	$md_{4,8}$
MD =	$md_{5,1}$	$md_{5,2}$	$md_{5,3}$	$md_{5,4}$	0	$md_{5,6}$	$md_{5,7}$	<i>md</i> _{5,8}
	$md_{6,1}$	$md_{6,2}$	$md_{6,3}$	$md_{6,4}$	$md_{6,5}$	0	$md_{6,7}$	<i>md</i> _{6,8}
	$md_{7,1}$	$md_{7,2}$	$md_{7,3}$	$md_{7,4}$	$md_{7,5}$	$md_{7,6}$	0	md _{7,8}
	$md_{8,1}$	$md_{8,2}$	$md_{8,3}$	$md_{8,4}$	$md_{8,5}$	$md_{8,6}$	$md_{8,7}$	0

(10)

$$md_{3,4} = P_1P_2 + P_1P_3 + P_3P_4$$

$$md_{3,8} = P_1P_2 + P_1P_5 + P_5P_6 + P_6P_7 + P_7P_8 + P_8P_9$$
(11)

Different disassembly operations need different disassembly tools as shown in Figure 5. To finish different disassembly operations, industrial robot needs additional disassembly time to change disassembly tools. This additional time is described by Equation (12) ('*Sp*', '*Sc*', '*Gr*', '*Pl*', '*Ha*' and '*EC*' respectively mean spanners, screwdrivers, grippers, pliers, hammers and electrical cutting). After the disassembly operations have been determined, different disassembly tools should also be considered to handle different sizes of components. For example, to disassemble different sizes of bolts (M1, M2, M3, M4, *etc.*), different types of spanners should be considered. This also causes additional disassembly time for industrial robot to change disassembly tools as shown in Equation (13).

Similarly, for each robotic workstation, the direction-change time between different parts is a part of the total working time. It is described by Equation (14).





Fig. 5 Disassembly operations and corresponding disassembly tools



В	Basic disassembly time Disassembly direction							2	2.5	2.5	2	7	2	1.5	2
Ε	Disas	seml	bly d	irecti	on			x+	y+	У-	y-	x+	z+	x+	\mathbf{x} +
	Dis	sasse	mbly	/ tool			2	Sp1	Sp2	Gr1	Gr1	Sp1	Sp2	Sp2	Gr1
			h_{pi}					3	3	2	1	4	3	3	1
	Ν	lovir	ng sp	eed							10 a	cm/s			
	Sp1 Sp2 Gr1 Gr2														
$TT = \begin{cases} Sp1 & Sp2 & Gr1 & Gr2 \\ Sp2 & 1 & 0 & 2 & 2 \\ Gr1 & 2 & 2 & 0 & 1 \\ Gr2 & 2 & 2 & 1 & 0 \\ \end{cases}$															(15)
	$Gr2\begin{bmatrix} 2 & 2 & 0 & 1 \\ 3 & 2 & 2 & 1 & 0 \end{bmatrix}$ $\begin{bmatrix} 0 & 14 & 21 & 18 & 12 \\ 14 & 0 & 25 & 20 & 15 \\ 21 & 25 & 0 & 15 & 19 \end{bmatrix}$					15 13 24	17 19 21	22 23 30							(16)
105	18	20	15	0	20	30	35	28							
MD =	12	15	19	20	0	25	10	10							
	15	13	24	30	25	0	20	15							
	13 13 24 30 23 17 19 21 35 10				20	0	17								
l	17 19 21 35 10 2 22 23 30 28 10 1				15	17	0								

An example is used here to calculate multi-objective values of a robotic disassembly line solution. For the disassembly sequence '3-4-8-2-6-7-5-1' as shown in table 1, the cycle time of robotic disassembly line is 20 s, the direction-change time, tool-change time and length of moving path between different parts are respectively defined by Equation (14), Equation (15) (Sp1, Sp2, Gr1, Gr2 respectively mean spanner-I, spanner-II, gripper-I and gripper-II) and Equation (16). Firstly, it needs to generate robotic disassembly line solutions based on feasible disassembly sequence. From Figure 6, disassembly tasks are assigned to robotic workstations with the help of an allocation matrix $A = [a_i]$. For example, as shown in step 1 of Figure 6, a_4 and a_6 are respectively calculated by Equation (17) and Equation (18). After the allocation matrix A is obtained in step 1, it is obvious that a_2 is less than the cycle time (20s) and a_3 is greater than the cycle time. Because the total working time of robotic workstation must not exceed the cycle time, only a_1 and a_2 should be selected. It means parts 3 and 4 should be assigned to the robotic workstation 1. After that, parts 3 and 4 are deleted in the disassembly sequence '3-4-8-2-6-7-5-1'. In step 2, the allocation matrix A = [2.5, 9.1, 22.6, 28.8, 31.6, 34] is obtained in the same manner and only the former two elements are less than the cycle time. It means parts 8 and 2 should be assigned to robotic workstation 2. Similarly, in steps 3 and 4, parts 6, 7 and 5 are assigned to robotic workstation 3 and part 1 is assigned to robotic workstation 4. Thus, the robotic disassembly line solution is obtained as shown in Figure 7. The multi-objective values (f_1 , f_2 and f_3) are calculated by Equations (19) ~ (21).

$$\begin{aligned} a_{4} &= bt_{3} + bt_{4} + bt_{8} + bt_{2} + mt_{3,4} + tt_{3,4} + dt_{3,4} + mt_{4,8} + tt_{4,8} + dt_{4,8} + \\ &mt_{8,2} + tt_{8,2} + dt_{8,2} + mt_{2,3} + tt_{2,3} + dt_{2,3} \\ &= 2 + 2.5 + 2.5 + 2 + 15/10 + 1 + 1 + 28/10 + 2 + 2 + 23/10 + 0 + 0 + \\ &25/10 + 2 + 1 = 27.1 \\ a_{6} &= bt_{3} + bt_{4} + bt_{8} + bt_{2} + bt_{6} + bt_{7} + mt_{3,4} + tt_{3,4} + dt_{3,4} + mt_{4,8} + tt_{4,8} + dt_{4,8} + \\ &mt_{8,2} + tt_{8,2} + dt_{8,2} + mt_{2,6} + tt_{2,6} + dt_{2,6} + mt_{6,7} + tt_{6,7} + mt_{7,3} + tt_{7,3} + dt_{7,3} \\ &= 2 + 2.5 + 2.5 + 2 + 7 + 2 + 15/10 + 1 + 1 + 28/10 + 2 + 2 + 23/10 + 0 + 0 + \\ &13/10 + 2 + 1 + 20/10 + 1 + 1 + 21/10 + 1 + 1 = 43 \end{aligned}$$



Fig. 7 The robotic disassembly line solution

5. Bees algorithm

5.1 The basic BA



Fig. 8 Flowchart of basic BA and IMODBA

BA is inspired by the foraging behavior of honey bees [52]. For the basic BA, several parameters should be initialized, namely: number of scout bees (*scoutn*), number of elite sites (*nes*), number of selected sites(*ns*), number of follower bees around elite sites (*rnes*), number of follower bees (*rns*) around non-elite selected sites (*ns* - *nes*) and the stopping criteria. As shown in Figure 8(a), *scoutn* scout bees randomly search the solution space (step 1), fitness of the sites visited by scout bees is evaluated and these sites are sorted by fitness value in step 2. After that, the stopping criteria (whether the maximum iteration is reached) is determined in step 3. The best *nes* sites and *ns* sites visited by scout bees are

respectively selected as 'elite sites' and 'selected sites'. For each elite site (*nes*), *rnes* follower bees are dispatched to search its neighborhood. The scout bee will be replaced by the follower bee only if the quality of the site visited by this follower bees are dispatched to search its neighborhood. The scout bee is better than the scout bee (step 4(a)). For each non-elite selected site (*ns - nes*), *rns* follower bees are dispatched to search its neighborhood. The scout bee will also be replaced by the follower bee only if the quality of the site visited by this follower bee only if the quality of the site visited by this follower bee is better than the scout bee (step 4(b)). The remaining *scoutn - ns* bees are dispatched to randomly explore the solution space (step 5). Then, *scoutn* scout bees are sorted by fitness value of the sites and the next iteration starts (step 6). The iteration process continues until the maximum iteration is reached. Finally, the best solution is saved in step 7.

5.2 IMODBA

The flowchart of IMODBA is described in Figure 8(b). The number of scout bees *scoutn*, number of selected sites *ns* and number of follower bees around selected sites *rns* are initialized. The disassembly sequence and disassembly direction of scout bees are generated by SIMM and the multi-objective values of the sites visited by scout bees are calculated by the method mentioned in Section 4 (step 1). Then, in step 2, these sites are sorted by efficient non-dominated Pareto sorting method (ENS) [53]. The sites which have the same front rankings are sorted by crowding-distance. When the maximum iteration *iter* is reached, this procedure stops (step 3). After that, each site visited by scout bee is assigned front number $Fr = [Fr_1, Fr_2, Fr_3, ..., Fr_n]$ and crowding distance. The best *ns* sites are selected as the selected sites. For each selected site, *rns* follower bees are dispatched to search the neighborhood (step 4). The remaining *scout-ns* scout bees randomly search the solution space by SIMM (step 5). After that, *scoutn+ns*rns* sites visited by scout bees and follower bees are sorted and the best *scoutn* bees are selected as the scout bees for the next iteration (step 6). The iteration process continues until the maximum iteration is reached. Finally, the Pareto optimal solutions of RDLBP are obtained (step 7).

5.2.1 Representation of Bees

A bee is represented in Figure 9. The feasible disassembly sequence and disassembly direction of bees are generated by SIMM used in Section 3. The robotic workstation array is obtained by the robotic workstation assignment method. After that, multi-objective values of the sites visited by scout bees are calculated by the method mentioned in Section 4.

Disassembly sequence	3	4	8	2	6	7	5	1
Disassembly direction	x+	y+	у-	у-	x+	z+	x+	x+
Robotic workstations	1	1	2	2	3	3	3	4
Disassembly tool	Sp1	Sp2	Gr1	Gr1	Sp1	Sp2	Sp2	Gr1
h_{pi}	3	3	2	1	4	3	3	1
Multi-objective values	4	515.06	86		•			

Fig. 9 The representation of bees

5.2.2 Initialization of IMODBA

In the initialization step of IMODBA, number of scout bees *scoutn*, number of selected sites *ns* and number of follower bees around selected sites *rns* are initialized and *scoutn* scout bees are dispatched to randomly search the solution space.

5.2.3 Pareto optimal solution

In this paper, the goal of IMODBA is to minimize three objectives mentioned in Section 4 as shown by Equation (22).

$$\min F(Seq) = [f_1(Seq), f_2(Seq), f_3(Seq)] \quad Seq \in FSeq$$

$$\tag{22}$$

Suppose both Seq_1 and Seq_2 are feasible disassembly sequences, Seq_2 is dominated by Seq_1 if and only if

$$(f_i(Seq_1) \le f_i(Seq_2)) \&\& (f_j(Seq_1) < f_j(Seq_2)) \quad \forall i = 1, 2, 3 \; \exists j = 1, 2, 3 \; (23)$$

If a solution is not dominated by any other solutions, it is Pareto optimal solution. The Pareto optimal set is a solution set which consists of all the Pareto optimal solutions, corresponding function value is the Pareto optimal front.

5.2.4 Pareto sorting





The goal of Pareto sorting is to assign front rankings to all the solutions based on their dominance

relationships. Most of the Pareto-based multi-objective optimization methods use the fast non-dominated sorting method [54]. An example is used to describe the process of this method in Figure 10. For any solution in the population *P*, *bdn* represents the number of solutions that dominate this solution while D_{set} is a set of solutions which is dominated by this solution. For example, in step 1 (Figure 10), solution 2 is only dominated by solution 8, thus, *bdn* of solution 2 is 1. Solutions 1 and 4 are dominated by solution 2, thus, D_{set} of solution 2 is [1, 4]. From step 2, it is obvious that solutions 3, 5 and 8 are the non-dominated solutions (*bdn* is 0) and they are assigned front ranking Fr_1 . After that, solution 3, 5 and 8 are deleted. In step 2, D_{set} of solutions 3, 5 and 8 (3 solutions). Thus, in step 3, after solutions 3, 5 and 8 are deleted, *bdn* of solution 1 should minus 3. It is the same with solutions 2, 4, 6 and 7 in step 3. It is obvious the solutions 2 and 7 are deleted and *bdn* of the other solutions are updated (the blue font in step 4). This procedure continues in the same manner as shown in steps 5 and 6. Finally, all the solutions are assigned front rankings as shown in Figure 10.



However, the traditional Pareto sorting method is poor efficiency [55]. ENS is proposed to improve the efficiency of Pareto sorting method without changing the sorting results [53]. As shown in Figure 11, population P is sorted in ascending order according to the first objective value. If the first objective values of two solutions are the same, then the solutions are sorted in ascending order according to the second objective value. If the first and second objective values are still the same, these solutions are sorted in ascending order according to the third objective value. After that, the sorted population P^* is obtained. It is obvious that solution $P^*(1)$ (solution 5) should be assigned front ranking Fr_I , because no solution in

							Тŀ	10 5/	orted r	opulati	ion P^*			The I	Doroto	conted non	ulation	D
7	Vo.	f ₁	f_2	f3			No.	f_1	Jiteu j	f2	f_3	-	-	No.	f_l	f_2	f_3	$\frac{Fr}{Fr}$
	1	5	6	5			5	1		3	3	-	-	5	1	3	3	Fr_1
	2	3	4	2			3	2		1	3			3	2	1	3	Fr_1
	3	2	1	3		Ν	7	2		2	4		Ν	8	3	4	1	Fr_1
	4	4	7	6			8	3		4	1			2	2	2	2	Fr ₂ Fr.
	5	1	3	5			2	3		4	2		-	6	4	2	6	Fr_3
	7	4	2	4			4	4		2	6			1	5	6	5	Fr_3
	8	3	4	1			1	5		6	5			4	4	7	6	Fr_4
									1	r		-						
Th	ne so	orted non	ulation <i>I</i>	Step 1		Pareto so	orting			_Т	ne sorte	d populati	Sto on P*	ep 2		Pareto sor	ting	
No.	f_i	f:	2	f_3 No	fi	f2	, ting	f3	Fr	No.	f_l	f ₂	f3	No	f_1	f ₂	f3	Fr
5	1	3		3 - 5	1	3		3	Fr_1	5	1	3	3	5	1	3	3	Fr_1
3	2	1		3						3	2	1	3	►3	2	1	3	Fr_{I}
7	2	2		4						7	2	2	4					
8	3	4		1						8	3	4	1					
2	3	4		2 6						6	3 4	4	6					
4	4	7		5						4	4	7	6					
1	5	6		5						1	5	6	5					
		F	opulatio	n 5 is as	signec	I with Fr_1						Popu	lation 3	3 is as	signed	I with Fr_I		
				Step 3									St	ep 4				
Th	ne so	orted pop	ulation I	»*	-	Pareto so	orting			Th	e sorte	d populati	ion P*		6	Pareto sor	ting	
No.	f_1		2 .	$\frac{f_3}{2}$ No		<u>f2</u>		f_3	Fr	<u>No.</u>	f_I	f_2	f3	No.		<u>f2</u>		Fr
2		3		5 5 2 4 2	2	3		3	Fr_1	2		3 1	3	3	2	3 1	3	rr_1 Fr_2
7	$\frac{2}{2}$	2		4	2	1		5	111	7	2	2	4	8	3	4	1	Fr_1
8	3	4		1 7	2	2		4	Fr_2	8	3	4	1	7	2	2	4	Fr_2
2	3	4		2						2	3	4	2	-				
6	4	2		5						6	4	2	6					
4	4	7		5						4	4	7	6					
	5	6		<u> </u>			6	1		<u> </u>	5	6	5				c	<u> </u>
Poj	pula	last one	compare to the fir	d with tr	ie soft is assi	gned with	r_1 from Fr_2	n th	ie	Pop	pulation lasi	1 8 1s com t one to th	pared v e first a	with th and it	e solu is assi	gned with	i from t Fr ₂	he
				G. 5		0	-						C+	on 6		6	2	
Th	ne so	orted pop	ulation I	Step 5		Pareto so	orting			Tł	ne sorte	d populat	ion P^*	еро		Pareto so	rting	
No.	f_1	f	2.	f ₃ No	f_I	f_2		f_3	Fr	No.	f_I	f_2	f_3	No	f_l	f_2	f_3	Fr
5	1	3		3 5	1	3		3	Fr_1	5	1	3	3	5	1	3	3	Fr_1
3	2	1		3 3	2	1		3	Fr_1	3	2	1	3	3	2	1	3	Fri
7	2	2		4 8	3	4		1	Fr		2	2	4	8	3	4	1	
8	3	4		$\frac{1}{2}$	2	2		4	Fr_2		3	4	2	/ <u>) /</u>	3	4	4	F_{r_2}
6	4	2		5		-		2	112	6	4	2	6	F 6	4	2	6	Fr ₃
4	4	7		5						4	4	7	6					
_1	5	6		5						_1	5	6	5					
		Pop	oulation	2 is is as	signe	d with Fr_2						Populat	ion 6 is	is as	signeo	d with Fr_3		
T			1.0	Step 7		Densta				T		1	St	ep 8		Denste en		
	f_1	f	ulation I	$\frac{1}{f_2}$ No	f_1	Pareto so	orting	f2	Fr	$\frac{11}{No}$	f_i	f ₂	$\frac{100 P}{f_2}$	<u>No</u>	f_1	f2	rung f2	Fr
5	1	3	2 .	$\frac{1}{3}$ $\frac{1}{5}$	1	3		3	$\frac{1}{Fr_1}$	5	1	3	3	- 110	1	3	3	Fr ₁
3	2	1		3 3	2	1		3	Fr_1	3	2	1	3	3	2	1	3	Fr_1
7	2	2		4	3	4		1	Fr_{l}	7	2	2	4	18	3	4	1	Fr ₁
8	3	4		1 7	2	2		4	Fr_2	8	3	4	1	7	2	2	4	Fr_2
2	3	4		$\frac{2}{6}$	3	4		2	Fr_2	2	3	4	2	$\prod_{i=1}^{2}$	5	4	2	Fr.
0	4	2		5	4	2		0	rr ₃	4	4	2 7	6		4 5	2 6	5	Fr ₃
1	5	6		5 4	4	7		6	Fr ₄	1	5	6	5	4	4	7	6	Fr ₄
		Por	ulation	1 is is as	signer	with Fr.						Populat	ion 1 i	s is as	signe	d with Fr.		

population P^* dominates it. For solution $P^*(i)$ (i = 2, 3...), it should be compared with the solutions which have been assigned Fr_k (k = 1) from the last solution to the first solution. If no solution which has been

Fig. 12 An example of ENS method

assigned Fr_k dominates $P^*(i)$, then $P^*(i)$ is assigned Fr_k . If any solution which has been assigned Fr_k dominates $P^*(i)$, k increases by 1. If k is not greater than the length of set Fr, solution $P^*(i)$ should be compared with the solutions which have been assigned Fr_k from the last solution to the first solution. If k is greater than the length of set Fr, it means there is no front ranking Fr_k in set Fr. Hence, front ranking Fr_k is added in set Fr and $P^*(i)$ is assigned Fr_k . This procedure continues until all the solutions are assigned front rankings. Finally, Pareto sorted population P_{Fr} is obtained.

An example is used here to show the workflow of ENS. As shown in step 1 (Figure 12), based on the same population used in Figure 10, the sorted population P^* is firstly obtained. Obviously, the first solution (solution 5) in the sorted population P^* is assigned Fr_1 . In step 2, the second solution (solution 3) is compared with solutions which have been assigned Fr_l from the last one to the first one (only solution 5 is assigned Fr_1). However, solution 3 is not dominated by solution 5. Thus, solution 3 is assigned Fr_1 . In step 3, solution 7 is compared with solutions which have been assigned Fr_1 from the last one to the first one (in order of solutions 3 and 5). Because solution 3 dominates solution 7 and there is no front ranking Fr_2 in set Fr. Fr_2 is added to set Fr and solution 7 is assigned Fr_2 . In step 4, solution 8 is compared with solutions which have been assigned Fr_i from the last one to the first one (in order of solutions 3 and 5). There is no solution which has been assigned Fr_1 dominates solution 8. Thus, solution 8 is assigned Fr_1 . In step 5, solution 2 is compared with solutions which have been assigned Fr_1 from the last one to the first one (in order of solutions 8, 3 and 5). Because solution 2 is dominated by solution 8, it should be compared with solutions which have been assigned Fr_2 from the last one to the first one (only solution 7 is assigned Fr_2). It is obvious that solution 2 is not dominated by solution 7. Thus, solution 2 is assigned Fr_2 . In step 6, solution 6 is compared with solutions which have been assigned Fr_1 from the last one to the first one (in order of solutions 8, 3 and 5). It is dominated by solution 3 and then it should be compared with solutions which have been assigned Fr_2 from the last one to the first one (in order of solutions 2 and 7). However, solution 6 is dominated by solution 7 and there is no front ranking Fr_3 in set Fr. Thus, Fr_3 is added to set Fr and solution 6 is assigned Fr_3 . This procedure continues until all the solutions are assigned front rankings as shown in Figure 12.

The differences between the traditional Pareto sorting and ENS are described in Figure 13. It is obvious that the traditional Pareto sorting method assigns the front rankings to several solutions at a time and ENS assigns front rankings to the solutions individually.



(a) The traditional Pareto sorting method(b) The efficient non-dominated sorting methodFig. 13 The differences between traditional Pareto sorting and ENS

5.2.5 Crowding-distance computation

After all the solutions are assigned front rankings, the solutions which have the same front rankings are sorted by crowding-distance [54]. Firstly, it sorts the solutions according to each objective function value in ascending order. For each objective value, the solutions which have the smallest and largest objective values are assigned infinite distance value. For the other intermediate solutions, distance value (the absolute normalized difference of two adjacent solutions' objective value) is assigned. The crowding-distance of all the solutions is calculated by the sum of distance values of each objective. The procedure of crowding-distance computation is described in Figure 14.



Fig. 14 The procedure of crowd-distance computation

Based on Pareto sorting and crowding-distance computation, if two solutions have different front rankings, the solution with better front ranking is preferred (such as Fr_1 is better than Fr_2). If two solutions have the same front rankings, the solution with greater crowding distance is preferred.

Before mutating	3	4	8	2	6	7	5	1	After	3	4	8	2	6	7	5	1
mutating	x+	y+	у-	у-	x+	z+	x+	x+	mutating	x+	y+	у-	y+	x+	z+	x+	x+
								C	One-bit mutati	ng							
Before	3	4	8	2	6	7	5	1	After	3	4	7	8	2	6	5	1
inserting	x+	y+	y-	у-	x+	x+ z+ x+ x+ inserti		inserting	x+	y+	Z+	у-	у-	x+	x+	x+	
								C	ne-bit insertir	ıg							
Before	3	4	8	2	6	7	5	1	After	3	4	7	2	6	8	5	1
swapping	x+	y+	у-	у-	x+	Z+	x+	x+	swapping	x+	y+	Z+	у-	X-	у-	x+	x+
								Т	wo-bit swappi	ng							
Before	3	4	8	2	6	7	5	1	After	3	7	6	2	8	4	5	1
inversing	x+	y+	у-	у-	x+	Z+	x+	x+	inversing	x+	Z+	x+	у-	y-	y+	x+	x+
In								Inversing									

Fig. 15 The neighborhood search strategy

5.2.6 Neighborhood search strategy

Each follower bee randomly searches the neighborhood of the sites visited by scout bees. The neighborhood search strategy which includes one-bit mutating operator, one-bit inserting operator, two-bit swapping operator and inversing operator is used in this paper as shown in Figure 15.

One-bit mutating operator acts on random bit of disassembly direction array and the corresponding direction changes 180 degrees (such as from x+ direction to x- direction). One-bit inserting operator randomly selects one bit of disassembly sequence and disassembly direction arrays and this bit inserts to random position of disassembly sequence and disassembly direction arrays. Two-bit swapping operator is used to exchange random two bits of disassembly sequence and disassembly direction arrays. Inversing operator is used to invert random part of disassembly sequence and disassembly direction arrays. The feasibility of follower bee needs to be checked by SIMM. If the follower bee is unfeasible disassembly sequence, this follower bee continues to search the neighborhood until it is feasible disassembly sequence.

6. Experiments and Results

6.1 Case studies



Fig. 16 Case studies based on a gear pump and a camera

As shown in Figure 16, cases studies based on a gear pump and a camera [56] are used to verify the effectiveness of proposed method. The workflow of proposed method is described in Figure 17. The properties of all the parts of the gear pump and the camera are listed in Table 2.

EoLPs are disassembled by robotic disassembly line as shown in Figure 18. CT of this robotic disassembly line is 30 s. The direction-change and tool-change time are respectively described by Equations (14) and (15).

	140	e 2 The properties of an ale	pures o	r the geta pump and the ear	neru	
EoLP	Parts	Task name	<i>bt</i> /s	Disassembly point (mm)	Tools	h_{pi}
	1	Unscrew the Bolt A	3	[49.4, -12.6, 105.5]	Spanner-I	1
	2	Unscrew the Bolt B	3	[74.4, -12.6, 81]	Spanner-I	1
	3	Unscrew the Bolt C	3	[74.4, -12.6, 45]	Spanner-I	1
	4	Unscrew the Bolt D	3	[49.4, -12.6, 20.5]	Spanner-I	1
	5	Unscrew the Bolt E	3	[24.4, -12.6, 45]	Spanner-I	1
	6	Unscrew the Bolt F	3	[24.4, -12.6, 81]	Spanner-I	1
Gear	7	Remove the Cover	4	[49.4, -20.6, 63]	Gripper-II	2
pump	8	Remove the Gasket	3	[49.4, 1.4, 105.5]	Gripper-I	2
	9	Remove the Gear A	6	[49.4, 3.4, 81]	Gripper-I	3
	10	Remove the Gear B	6	[49.4, 3.4, 45]	Gripper-I	3
	11	Remove the Shaft A	4	[49.4, -7.6, 81]	Gripper-I	1
	12	Remove the Base	8	[49.4, 49.4, 81]	Gripper-II	4

Table 2 The properties of all the parts of the gear pump and the camera

	13	Remove the Shaft B	4	[49.4, 152.4, 45]	Gripper-I	2
	14	Remove the Packing Gland	2	[49.4, 91.4, 45]	Gripper-I	2
	15	Unscrew the Gland Nut	3	[49.4, 96.4, 45]	Spanner-II	1
	1	Unscrew the Bolt A	3	[37.4, -28, 39.9]	Spanner-I	1
	2	Unscrew the Bolt B	3	[12.7, -18.5, 39.9]	Spanner-I	1
	3	Unscrew the Bolt C	3	[12.7, -18.5, 16]	Spanner-I	1
	4	Remove the Cover A	2	[28.1, -26, 29.8]	Gripper-I	2
	5	Remove the Part A	5	[30.3, -24.5, 32.4]	Gripper-I	3
	6	Remove the Part B	4	[23.1, -25.5, 26.6]	Gripper-II	3
	7	Remove the Part C	3	[24.4, -13.5, 28.8]	Gripper-I	2
	8	Remove the Part D	4	[25.1, -12.5, 43.4]	Gripper-II	2
Camera	9	Remove the Part E	3	[24.5, -0.5, 43.4]	Gripper-I	2
	10	Remove the Camera	8	[24.5, -20.1, 27.8]	Gripper-II	5
	11	Remove the Part F	4	[23, 0, 56.4]	Gripper-II	2
	12	Remove the Part G	2	[10.7, 13.5, 28.1]	Gripper-I	1
	13	Remove the Part H	3	[30, 24, 56.4]	Gripper-II	2
	14	Unscrew the Bolt D	3	[22.5, 26.5, 45.9]	Spanner-II	1
	15	Unscrew the Bolt E	3	[42.6, 26.5, 45.9]	Spanner-II	1
	16	Unscrew the Bolt F	3	[21, 26.5, 10]	Spanner-II	1
	17	Unscrew the Bolt G	3	[36.3, 26.5, 10]	Spanner-II	1



Fig. 17 The workflow of proposed method

The safe distance between the contour of EoLP and the moving path of industrial robot's end-effector is 10 mm. The moving time matrix ($MT = [mt_{ij}]$; i, j = 1, 2... 15) between different parts is calculated by moving distance matrix ($MD = [md_{ij}]$; i, j = 1, 2... 15) which is manually calculated and moving speed (ms) which is assumed to be 12 cm/s[®] [57]. For example, as shown in Figure 19, the moving time $mt_{1,13}$ is calculated by Equation (24).

$$mt_{1,13} = md_{1,13} / ms$$

$$= (P_1P_2 + P_2P_3 + P_3P_4 + P_4P_5 + P_5P_6 + P_6P_7) / ms$$

$$= (10 + 18.92 + 72.01 + 127.67 + 20 + 10) / 12 = 21.55s$$
(24)



Fig. 18 The robotic disassembly line



Fig. 19 The moving path from Bolt A to Shaft B

6.2 Performance analysis

In this section, simulations are taken on personal computer with 2.3GHz Intel core i5-6200U CPU, 4 GB memory using Matlab 2014b® [58]. This section consists of three parts: 1. performance analysis of IMODBA under different iterations and populations; 2. performance comparisons between IMODBA and the other multi-objective optimization algorithms; 3. comparisons of Pareto optimal fronts of three cases.

For single-objective optimization problem, it is easy to evaluate the quality of solutions through fitness value. For multi-objectives optimization algorithm, auxiliary methods need to be used to evaluate the quality of non-dominated solutions [59]. Existing performance indexes (PI) used for evaluating the quality of non-dominated solutions contain distance-based accuracy PI, volume-based accuracy PI, *etc* [60]. In this paper, hypervolume indicator (HI) and generational distance (GD) are used. HI [61] is a widely used volume-based accuracy PI. It can evaluate the convergence and distribution of non-dominated solutions by quantitative comparisons without knowing the real Pareto optimal fronts [62]. As shown in Figure 20(a), HI of non-dominated solutions (P_1 , P_2 and P_3 are the obtained non-dominated solutions) is the volume of the areas surrounded by cuboids P_1R , P_2R and P_3R (R is the reference point) as

shown in Equation (25). For minimum optimization problem, the non-dominated solutions with greater HI value are preferred. GD [60] is used to represent the distance between the obtained non-dominated solutions (P_1 , P_2 and P_3 in Figure 20(b)) and the Pareto optimal solutions ($P_{opt,1}$, $P_{opt,2}$ and $P_{opt,3}$ in Figure 20(b)). It is calculated by Equation (26), where *nd* is the number of obtained non-dominated solutions, d_i (the red dotted line in Figure 20(b)) is the Euclidean distance between i^{th} member of obtained non-dominated solutions and its nearest member of Pareto optimal solutions. The non-dominated solutions with lower GD value are preferred.

 $HI = Volume(cuboid_{P,R} \cup cuboid_{P,R} \cup cuboid_{P,R})$



(a) HI of non-dominated solutions (b) GD of non-dominated solutions

Fig. 20 performance indicators of non-dominated solutions

(25)

Before calculating HI and GD values of non-dominated solutions, it is important to normalize multi-objective values by Equation (27). For the gear pump, $f_{1,min}$, $f_{1,max}$, $f_{2,min}$, $f_{2,max}$, $f_{3,min}$ and $f_{3,max}$ are respectively 3, 5, 0.0548, 765.6372, 228 and 259. For the camera, $f_{1,min}$, $f_{1,max}$, $f_{2,min}$, $f_{2,max}$, $f_{3,min}$ and $f_{3,max}$ are respectively 3, 4, 1.0411, 858.3914, 268 and 338. For both the gear pump and the camera, the reference point for calculating HI value is [1.2, 1.2, 1.2] and the optimal Pareto solutions for calculating GD value are listed in Tables 7 and 8.

$$f_{i,norm} = (f_i - f_{i,\min}) / (f_{i,\max} - f_{i,\min}) \quad i = 1, 2, 3$$
(27)

For both the gear pump and the camera, the selected sites number *ns*, follower bees number *rns* of IMODBA are respectively 15 and 1. The average running time, average HI and average GD are compared under different iterations (from 100 to 800) and populations (from 30 to 80). Each simulation is repeated 50 times. As shown in Figure 21, when the iteration number and the population number are respectively 80 and 800, it has the best quality of solutions (for the gear pump, average HI and average GD are respectively 1.5450 and 0.00; for the camera, average HI and average GD are respectively 0.8612 and 0.0025). But it takes the longest running time (for the gear pump, it is 67.55s and for the camera, it is 76.55s). When iteration number and population number are respectively 30 and 100, it takes the shortest running time (for the gear pump, it is 3.26s and for the camera, it is 3.89s) but it has the worst quality of solutions (for the gear pump, average HI and average GD are respectively 1.4825 and 0.0149; for the camera, average HI and average GD are respectively 1.4825 and 0.0149; for the camera, average HI and average GD are respectively 1.4825 and 0.0149; for the camera, average HI and average GD are respectively 1.4825 and 0.0149; for the camera, average HI and average GD are respectively 0.5529 and 0.016).





(a) Average running time of IMODBA under different (b) Ariterations and populations based on the gear pump itterations and populations based on the gear pump itteration.







(c) Average HI of IMODBA under different iterations and (d) Average HI of IMODBA under different iterations and populations based on the gear pump populations based on the camera



(e) Average GD of IMODBA under different iterations and f) Average GD of IMODBA under different iterations and populations based on the gear pump populations based on the camera

Fig. 21 Performance analysis of IMODBA under different iterations and populations

For the performance comparisons between IMODBA and the other multi-objective optimization algorithms, the average running time, average HI and average GD under different iterations and populations are analyzed.

- IMODBA: the proposed method in this paper is used. The selected sites number *ns*, follower bees number *rns* are 15 and 1 respectively.
- MODBA: multi-objective discrete Bees Algorithm (MODBA) uses the traditional Pareto sorting method [54] and the input parameters are the same with IMODBA.

- Multi-objective artificial Bees colony (MOABC): it consists of employed bees, onlooker bees and scout bees. The neighborhood search strategies of MOABC are the same with IMODBA. For onlooker bees, the probability value is calculated by the method used in [63]. When a food source has not been updated over *thred* iterations (*thred* is 10 here), employed bee becomes scout bee to randomly explore new food source.
- Multi-objective genetic algorithm (MOGA): it uses selection procedure (roulette wheel method), the Pareto sorting methods [64], two point crossover procedure [65] and mutation procedure (the same with neighborhood search strategies of IMODBA). The parameter of chromosome selection is 0.1 [64]. The crossover rate and mutation rate are 0.8 and 0.2 respectively.

	1			-					
EoLP	Iterations	100	200	300	400	500	600	700	800
	IMODBA	5.31s	10.77s	15.71s	20.98s	26.18s	31.16s	36.55s	41.86s
Gear	MODBA	5.63s	11.57s	17.29s	22.93s	28.19s	33.54s	39.50s	45.42s
pump	Improvement	0.32s	0.80s	1.58s	1.95s	2.01s	2.38s	2.95s	3.56s
	Percentage	5.68%	6.91%	9.14%	8.50%	7.13%	7.10%	7.47%	7.84%
	IMODBA	6.04s	11.98s	18.12s	24.17s	30.15s	36.23s	42.21s	48.76s
Camera	MODBA	6.68s	12.94	19.22s	25.67s	31.99s	38.36s	44.86s	51.28s
	Improvement	0.64s	0.96s	1.10s	1.50s	1.84s	2.13s	2.65s	2.52s
	Percentage	9.58%	7.42%	5.72%	5.84%	5.75%	5.55%	5.91%	4.91%

Table 3 Improvement of running time of IMODBA under different iterations

Table 4 Improvement of running time of IMODBA under different populations						ulations	
EoLP	Populations	30	40	50	60	70	80
	IMODBA	16.19s	21.41s	26.18s	31.38s	36.27s	40.92s
Gear	MODBA	17.83s	22.85s	28.19s	33.02s	38.14s	43.03s
Pump	Improvement	1.64s	1.44s	2.01s	1.64s	1.87s	2.11s
	Percentage	9.20%	6.30%	7.13%	4.97%	4.90%	4.90%
	IMODBA	18.20s	24.72s	30.15s	35.98s	41.82s	47.83s
Camera	MODBA	20.08s	26.01s	31.99s	37.55s	43.28s	49.12s
	Improvement	1.88s	1.29s	1.84s	1.57s	1.46s	1.29s
	Percentage	9.36%	4.96%	5.75%	4.18%	3.37%	2.63%

When the population number is 50, the average running time, average HI and average GD are compared under different iterations (from 100 to 800) as shown in Figures 22(a) ~ 22(f). Each simulation is repeated 50 times. From Figures 22(a) and 22(b), for both the gear pump and the camera, MODBA needs the longest running time than the others. With the help of ENS, IMODBA needs less running time than MODBA. The improvement of running time of IMODBA under different iterations is listed in Table 3. From Figures 22(c) ~ 22(f), for both the gear pump and the camera, it is obvious that IMODBA and MODBA can find better quality of non-dominated solutions than MOABC and MOGA. The quality of



Fig. 22 Comparisons of the four optimization algorithms under different iterations based on the gear pump and the camera

solutions obtained by IMODBA is nearly the same with MODBA, because ENS sorts the solutions using less running time without changing the Pareto sorting results. From Figures 22(c) and 22(d), MOABC performs better than MOGA in terms of HI value while MOGA performs better than MOABC in terms of GD value from Figures 22(e) and 22(f). It is because MOABC performs better than MOGA in the diversity of solutions while MOGA performs better than MOABC in the convergence of solutions. When the iteration number is 500, simulations are made under different populations (from 30 to 80). Each simulation is repeated 50 times. From Figures 23(a) and 23(b), for both the gear pump and the camera, the

average running time of IMODBA is less than MODBA and it is comparable with MOABC and MOGA. The improvement of running time of IMODBA under different populations is listed in Table 4. From Figures $23(c) \sim 23(f)$, for both the gear pump and the camera, it is obvious that IMODBA and MODBA can also find better quality of solutions than MOABC and MOGA. MOGA performs worse than MOABC in terms of HI value from Figures 23(c) and 23(d), but it performs better than MOABC in terms of GD value from Figures 23(e) and 23(f). It is because MOGA performs better than MOABC in the convergence of solutions and it performs worse than MOABC in the diversity of solutions.



(a) Average running time of four optimization under different populations based on the gear pump



(c) Average HI of four optimization under different populations based on the gear pump





(b) Average running time of four optimization under different populations based on the camera



(d) Average HI of four optimization under different populations based on the camera



populations based on the camera

Fig. 23 Comparisons of the four optimization algorithms under different populations based on the gear pump and the camera

The Pareto fronts obtained by the following three cases are also compared to verify the effectiveness of proposed method.

- Case 1: it considers the basic disassembly time of each part, the tool-change time and the direction-change time between different parts, but the moving time between different parts is ignored.
- Case 2: it considers the basic disassembly time of each part, the tool-change time, the direction-change time and the moving time between different parts. The moving time is calculated by Euclidean distance between different parts and moving speed of industrial robot's end-effector (ElSayed et al. 2012).
- Case 3: RDLBP is solved by the proposed method in this paper.

The iteration number, scout bees number, the selected sites number and follower bees number of IMODBA are 800, 80, 15 and 1 respectively. Simulations are repeated 100 times. 100 groups of non-dominated solutions are sorted to get the Pareto optimal solutions. Because ENS sorts the solutions without changing the Pareto sorting results, Pareto fronts obtained by MODBA are not listed in Tables 5 and 6. In Tables 5 and 6, for both the gear pump and the camera, it is obvious that Pareto fronts obtained by case 3 are different from the other cases. Case 1 ignores the moving time between different parts. Case 2 uses the Euclidean distance to calculate the moving time. It ignores the obstacle caused by the contour of EoLP. Thus, compared with cases 1 and 2, Pareto fronts obtained by case 3 are more applicable for robotic disassembly line. Besides, in Table 5, in terms of case 3, the 4th solution of MOABC is dominated by the 4th solution of IMODBA, the 5th and 6th solutions of MOABC are dominated by the 5th solution of IMODBA and the 8th solution of MOABC is dominated by the 7th solution of IMODBA. The number of Pareto fronts obtained by IMODBA is greater than MOGA. In Table 6, in terms of case 3, the 1st and 2nd solutions of MOABC is dominated by the 2nd solution of IMODBA and the 9th solution of MOABC is dominated by the 8th solution of IMODBA. The number of Pareto fronts obtained by IMODBA is also greater than MOGA. Thus, IMODBA performs better than MOABC and MOGA in terms of Pareto fronts. Finally, the Pareto optimal solutions of RDLBP based on the gear pump and the camera are listed in Tables 7 and 8 (for the disassembly direction, '1' and '2' mean 'Y+' and 'Y-' respectively).

7. Conclusion

In this paper, RDLBP is solved by IMODBA. Firstly, SIMM is used to generate feasible disassembly sequence and disassembly direction. After that, the feasible disassembly sequence and disassembly direction are used to obtain robotic disassembly line solution by robotic workstation assignment method. The multi-objectives used in this paper are to minimize the number of robotic workstations, balance the workload of robotic workstations and disassemble high demand parts as early as possible. With the help of ENS, IMODBA is proposed to solve RDLBP using less running time. Based on a gear pump and a camera, simulations are carried out to show the performance of IMODBA under different iterations and populations. The performance of IMODBA is also compared with MODBA, MOABC and MOGA under different iterations and populations. After that, Pareto fronts obtained by these optimization algorithms under different cases are also compared. It shows that IMODBA generates better quality of solutions than MOABC and MOGA. However, in this paper, SIMM is used to build disassembly model of EoLP which can be disassembled along orthogonal axes. In the future, more works should be finished to build disassembly model of EoLP with complex structure. In addition, the obstacle avoiding trajectory planning of industrial robot and the uncertainties in disassembly process will also be studied in the future.

Table 5 Pareto fronts of three cases based on the gear pump									np			
						Case 2						
10GA IMODBA			IMODBA			MOABC			MOGA			IMODB.
f_2	f_3	f_l	f_2	f_3	f_l	f_2	f_3	f_{I}	f_2	f_3	f_l	f_2
1	234	3	0.5262	238	3	0.5262	238	3	0.5262	238	3	0.0548
5	232	3	2.9193	235	3	2.9193	235	3	2.9193	235	3	0.0860
6	230	3	3.2023	234	3	3.2023	234	3	3.2023	234	3	0.1899
10	228	3	7.5069	233	3	7.5069	233	3	14.3724	232	3	1.0637
		4	14.3724	232	3	14.3724	232	4	198.9339	231	3	2.0211
		4	198.9339	231	4	198.9339	231	4	251.9134	230	3	3.8500
		4	251.9134	230	4	251.9134	230	4	355.8085	229	3	6.3106
		4	355.8085	229	4	355.8085	229	4	448.1330	228	4	27.0273
		4	448.1330	228	4	448.1330	228				4	27.2973
											4	27.4623
											4	263.5929
											4	284.1421

Table 6 Pareto fronts of three cases based on the camera															
								Case 2							
		мос	βA	IMODBA N			MOABC	C MOGA				IMODBA			
e ₃	f_l	f_2	f_3	f_l	f_2	f_3	f_l	f_2	f_3	f_l	f_2	f_3	f_l	f_2	f_3
10	3	0	310	3	0.2506	321	3	0.4466	294	3	0.4466	294	3	1.0411	331
92	3	1	292	3	0.4466	294	3	0.4501	293	3	0.4501	293	3	1.3141	319
84	3	2	284	3	0.4501	293	3	0.7571	275	3	0.7571	275	4	2.3049	318
80	3	5	280	3	0.7571	275	3	2.1059	274	3	2.1059	274	4	2.8017	312
75	3	9	275	3	2.1059	274	3	37.7046	271	3	37.7046	271	4	2.8432	309
74	3	14	274	3	37.7046	271	3	58.2641	269	3	58.2641	269	4	6.5750	307
70	3	52	270	3	58.2641	269	4	842.9434	268	4	842.9434	268	4	6.7485	306
58	3	68	268	4	842.9434	268							4	7.2913	303
													4	7.7011	288
													4	17.3577	287
													4	29.1523	275
													4	81.4263	273
													4	188.9248	272
													4	336.9715	270
													4	360.4361	268

Table 7 Pareto optimal solutions of RDLBP obtained by different optimizatio	n
algorithms based on the gear pump	

Diagaamble as man as	Disassembly direction	Robotic worksta			
Disassembly sequence	Disassembly sequence Disassembly direction				
5-6-2-3-1-7-15-8-14-12-9-13-11-10	2-2-2-2-2-2-1-2-1-1-2-2-1-1	1-1-1-1-1-1-2-2-2-2			
2-3-5-6-1-7-15-8-14-12-10-9-13-11	2-2-2-2-2-2-1-2-1-1-2-1-2-2	1-1-1-1-1-1-2-2-2-2			
2-3-5-6-1-7-15-14-12-8-10-9-13-11	2-2-2-2-2-2-1-1-1-2-2-1-2-2	1-1-1-1-1-1-2-2-2-2			
-14-3-5-4-6-1-2-7-9-8-12-13-10-11	1-1-2-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
-14-13-2-6-3-5-1-4-7-8-12-10-9-11	1-1-1-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
6-5-3-2-4-7-10-9-15-14-12-8-13-11	2-2-2-2-2-2-2-2-1-1-1-1-1-1	1-1-1-1-1-1-2-2-2-2			
-14-13-5-6-1-2-3-4-7-9-12-10-8-11	1-1-1-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
-14-3-6-13-5-1-4-2-12-9-7-8-10-11	1-1-2-2-1-2-2-2-1-1-2-1-2-1	1-1-1-2-2-2-3-3-3			
-14-3-6-13-4-1-5-2-12-9-7-10-8-11	1-1-2-2-1-2-2-2-1-1-2-1-2-1	1-1-1-2-2-2-3-3-2			
-14-5-2-13-3-1-4-6-12-9-7-8-11-10	1-1-2-2-1-2-2-2-2-1-1-2-1-2-1	1-1-1-2-2-2-3-3-3			
-14-13-3-4-1-5-2-6-12-9-7-10-8-11	1-1-1-2-2-2-2-2-1-1-2-1-2-1	1-1-1-2-2-2-2-3-2			
-14-13-3-4-1-5-2-6-12-9-10-7-8-11	1-1-1-2-2-2-2-2-1-1-1-2-2-1	1-1-1-2-2-2-2-3-2			
-14-13-6-2-3-5-1-4-7-11-12-9-10-8	1-1-1-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
-14-13-2-3-5-1-4-6-7-8-12-10-11-9	1-1-1-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
-14-13-2-3-5-6-1-4-7-8-12-10-9-11	1-1-1-2-2-2-2-2-2-2-1-1-1-1	1-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
-14-3-6-13-4-1-5-2-12-9-8-7-11-10	1-1-2-2-1-2-2-2-1-1-1-2-1-2	1-1-1-2-2-2-3-3-3			
The remaining solution	ons are the same with the $1^{st} \sim 3^{rd}$	and $7^{th} \sim 12^{th}$ solutions			
The Pareto optimal solu	tions are the same with the $1^{st} \sim 3$	3^{rd} and $5^{th} \sim 12^{th}$ solution			

			Table 8 Pareto optimal solutions of RDLBP obtained by different				
EoLP	Algorithms	No.	Disassembly sequence	Disassembly			
		1	1-3-17-14-15-16-4-5-2-6-7-8-13-12-9-11-10	2-2-1-1-1-2-2-2-			
		2	15-16-1-3-17-14-4-5-2-6-7-8-9-10-13-11-12	1-1-2-2-1-1-2-2-2-			
		3	15-3-17-1-4-2-5-16-6-14-13-12-11-10-7-9-8	1-2-1-2-2-2-1-2-			
		4	1-4-16-5-17-3-15-2-14-13-6-12-11-10-7-9-8	2-2-1-2-1-2-1-2-1-			
		5	1-4-16-5-17-2-15-3-6-14-13-12-11-10-7-9-8	2-2-1-2-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
		6	1-4-16-5-2-17-14-3-6-7-15-8-13-9-10-12-11	2-2-1-2-2-1-1-2-2-			
		7	1-4-16-5-15-3-17-2-6-7-8-14-13-9-10-12-11	2-2-1-2-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
	IMODBA	8	1-4-17-5-3-2-6-16-15-7-14-8-13-9-10-12-11	2-2-1-2-2-2-1-1-			
		9	1-4-5-3-15-2-6-16-7-8-9-14-10-17-11-13-12	2-2-2-2-1-2-2-1-2-			
Camera		10	1-4-5-2-15-3-6-7-16-8-9-14-10-17-11-13-12	2-2-2-2-1-2-2-2-1-			
		11	1-4-2-5-3-6-7-8-16-9-10-14-15-17-11-13-12	2-2-2-2-1-2-2-2-1-			
		12	1-4-5-3-2-6-7-8-16-9-10-14-15-17-11-13-12	2-2-2-2-2-2-1-			
		13	1-4-5-3-2-6-7-8-9-16-10-14-15-17-11-13-12	2-			
		14	1-4-2-5-3-6-7-8-9-10-16-15-14-17-11-13-12	2-			
		15	1-4-5-2-3-6-7-8-9-10-16-15-14-17-11-13-12	2-			
		1	15-16-14-1-3-17-4-5-2-6-7-8-13-12-9-11-10	1-1-1-2-2-1-2-2-2-			
	MOABC	2	3-17-14-15-16-1-4-5-2-6-7-8-9-10-11-13-12	2-1-1-1-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2-2			
		3	1-4-16-5-3-2-6-17-15-7-14-8-13-9-10-12-11	2-2-1-2-2-2-1-1-			
		4-16	The remaining	solutions are the sa			
	MOGA	1-14	The Pareto optim	al solutions are the			

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