UNIVERSITY^{OF} BIRMINGHAM

University of Birmingham Research at Birmingham

Probing deformation mechanisms of a FeCoCrNi high-entropy alloy at 293 and 77 K using in situ neutron diffraction

Wang, Yiqiang; Liu, Bin; Yan, Kun; Wang, Minshi; Kabra, Saurabh; Chiu, Yu-Lung; Dye, David; Lee, Peter D.; Liu, Yong; Cai, Biao

DOI:

10.1016/j.actamat.2018.05.013

License:

Creative Commons: Attribution-NonCommercial-NoDerivs (CC BY-NC-ND)

Document Version
Peer reviewed version

Citation for published version (Harvard):

Wang, Y, Liu, B, Yan, K, Wang, M, Kabra, S, Chiu, Y-L, Dye, D, Lee, PD, Liu, Y & Cai, B 2018, 'Probing deformation mechanisms of a FeCoCrNi high-entropy alloy at 293 and 77 K using *in situ* neutron diffraction', *Acta Materialia*, vol. 154, pp. 79-89. https://doi.org/10.1016/j.actamat.2018.05.013

Link to publication on Research at Birmingham portal

Publisher Rights Statement:

Published in Acta Materialia on 10/05/2018

DOI: 10.1016/j.actamat.2018.05.013

General rights

Unless a licence is specified above, all rights (including copyright and moral rights) in this document are retained by the authors and/or the copyright holders. The express permission of the copyright holder must be obtained for any use of this material other than for purposes permitted by law.

- •Users may freely distribute the URL that is used to identify this publication.
- •Users may download and/or print one copy of the publication from the University of Birmingham research portal for the purpose of private study or non-commercial research.
- •User may use extracts from the document in line with the concept of 'fair dealing' under the Copyright, Designs and Patents Act 1988 (?)
- •Users may not further distribute the material nor use it for the purposes of commercial gain.

Where a licence is displayed above, please note the terms and conditions of the licence govern your use of this document.

When citing, please reference the published version.

Take down policy

While the University of Birmingham exercises care and attention in making items available there are rare occasions when an item has been uploaded in error or has been deemed to be commercially or otherwise sensitive.

If you believe that this is the case for this document, please contact UBIRA@lists.bham.ac.uk providing details and we will remove access to the work immediately and investigate.

Download date: 18. Apr. 2024

1 Probing deformation mechanisms of a FeCoCrNi high-entropy alloy at 293 and

- 2 77 K using in situ neutron diffraction
- 3 Yiqiang Wang^{a, b}, Bin Liu^c, Kun Yan^d, Minshi Wang^e, Saurabh Kabra^f, Yu-Lung
- 4 Chiu^e, David Dye^g, Peter D. Lee^{a, f}, Yong Liu^{c**}, Biao Cai^{e,b*},
- 5 ^a Culham Centre for Fusion Energy, Culham Science Centre, Abingdon, OX13 3DB,
- 6 *UK*
- 8 ^c The State Key Laboratory of Powder Metallurgy, Central South University, Changsha,
- 9 410083, P.R. China
- 10 d School of Materials, University of Manchester, M13 9PL, UK
- 11 ^e School of Metallurgy and Materials, University of Birmingham, Birmingham
- 12 f ISIS Facility, Rutherford Appleton Laboratory, Didcot OX11 0QX, UK
- 13 g Department of Materials, Imperial College London, Exhibition Road, London SW7
- 14 2AZ, United Kingdom

Abstract

15

16 17

18 19

20 21

22

23

24

25

26 27

28

29

30 31

32 33

34

35

36

The deformation responses at 77 and 293 K of a FeCoNiCr high-entropy alloy, produced by a powder metallurgy route, are investigated using in situ neutron diffraction and correlative transmission electron microscopy. The strength and ductility of the alloy are significant improved at cryogenic temperatures. The true ultimate tensile strength and total elongation increased from 980 MPa and 45% at 293 K to 1725 MPa and 55% at 77K, respectively. The evolutions of lattice strain, stacking fault probability, and dislocation density were determined via quantifying the *in situ* neutron diffraction measurements. The results demonstrate that the alloy has a much higher tendency to form stacking faults and mechanical twins as the deformation temperature drops, which is due to the decrease of stacking fault energy (estimated to be 32.5 mJ/m² and 13 mJ/m² at 293 and 77 K, respectively). The increased volume faction of nanotwins and twin-twin intersections, formed during cryogenic temperature deformation, has been confirmed by transmission electron microscopy analysis. The enhanced strength and ductility at cryogenic temperatures can be attributed to the increased density of dislocations and nano-twins. The findings provide a fundamental understanding of underlying governing mechanistic mechanisms for the twinning induced plasticity in high entropy alloys, paving the way for the development of new alloys with superb resistance to cryogenic environments.

Keywords: high entropy alloy, deformation twinning, neutron diffraction, cryogenic deformation, stacking fault energy

1. Introduction

37

38

39

40

41

42

43

44

45

46

47

48

49

50

51

52

53

54

55

56

57

58

High-entropy alloys (HEAs) were first introduced in 2004 [1, 2], which aimed to maximise the configuration entropy to form a single phase microstructure via combining four or more principle elements in equimolar or near equimolar ratios. The high configuration entropy, sluggish diffusion, cocktail effect and large lattice distortion lead to their promising properties such as high strength, excellent ductility, and superior fracture toughness [3-8]. One type of HEA and its variants, based on five 3d transition elements (Fe, Co, Cr, Mn, Ni), can form a single phase face-centered-cubic (fcc) structure, displaying an excellent combination of high strength, ductility and fracture toughness at both room and cryogenic temperatures. Their mechanical properties improve significantly with decreasing deformation temperatures [3-7]. We termed this group of HEA as tHEA to distinguish them from other high entropy alloys (such as multi-phase HEAs [8]). tHEAs have attracted significant interests for cryogenic applications, such as liquid nitrogen storage and transportation of liquid gas from offshore. Many microstructural studies [3-7], on strained or failed tensile specimens, have been carried out, confirming the occurrence of nano-twinning during low temperature deformation of tHEAs. Hence twinning induced plasticity is attributed to the tHEAs' superb mechanical performance. Twinning induced plasticity has been at the forefront of research recently as it is one of the micro-mechanistic mechanisms that can overcome the strength-ductility trade-off, which has been demonstrated by fcc metals and alloys with low stacking fault energy (SFE) such as the tHEAs and TWIP steels [9-11].

The deformation mechanisms of fcc metals and alloys are strongly related to the temperature- and composition- dependent stacking fault energy (SFE) [12]. With the drop of SFE, the deformation mechanisms change from dislocation glide alone, to dislocation glide and mechanical twinning, to dislocation glide and martensite transformation [13-15]. This has been demonstrated in many fcc metals and alloys, including austenite steels [16], TRIP and TWIP steels [3,4], and Cu-Al alloys [17]. The SFE of the tHEAs has been measured or calculated to be 10-40 mJ/m² at room temperature [18-20]. In this SFE range, deformation twinning is usually activated, which has been confirmed in tHEAs by a few experimental studies [3-7]. Recently, martensite phase transformation have been observed when tHEAs were deformed under hydrostatic high-pressure conditions [21, 22] at both room and high temperatures, demonstrating that the fcc tHEAs can be destabilized into hcp phase at high pressure (e.g. over 14 GPa [21]). It is known that the SFE will drop as the temperature decreases, hence at cryogenic temperatures, the formation of shear bands, deformation twins and stacking faults can be enhanced [6, 23]. Simulations using first-principles methods [24, 25] confirm the temperature dependent behaviour of SFE and some predict that the SFE of tHEAs can even be negative at cryogenic temperatures [19, 26-28]. To validate the simulated results, the SFE of tHEAs at cryogenic temperatures need to be determined experimentally. Although a few studies have measured room temperature SFE of tHEAs using TEM based methods [18], it is not a straight-forward task to measure low

59

60

61

62

63

64

65

66

67

68

69

70

71

72

73

74

75

76

77

78

temperature SFE using TEM, as the samples deformed at cryogenic temperatures need to be warmed up to room temperature for sample preparation, during which the dislocation and fault structure may have changed. Thereby the development of new methods to measure low temperature SFE is critically needed, which will provide much-needed validation for the simulations[19, 26] and pave the way for designing new tHEAs. To study deformation mechanisms of tHEAs, quantitative in situ mapping of microstructure evolution of tHEAs at room temperature has previously been carried out, using TEM [26, 29, 30], SEM [31], synchrotron X-ray diffraction [32] and neutron diffraction [33, 34]. The in situ TEM directly observed the motion of Shockley partials, the formation of stacking faults and 3D network of nano-twins [29, 30]. *In situ* neutron and X-ray diffraction, on the other hand, can quantify the grain-level behaviour during deformation, which includes the measurement of stacking fault probability [33], singlecrystal elastic constants [34], phase transformation [32], and SFE [33]. Those in situ works significantly improved our understanding of the microstructural and mechanistic origin of tHEAs' superb mechanical properties. Carrying out *in situ* studies at cryogenic temperatures can provide similar benefits, not only unravelling the underlying mechanisms determining the dramatic increase of strength and ductility at cryogenic temperatures of the alloys, but also determining critical material parameters such as

80

81

82

83

84

85

86

87

88

89

90

91

92

93

94

95

96

97

98

99

SFE.

In the current study, we conducted uniaxial tensile deformation on a FeCoCrNi high-entropy alloy at 293 and 77 K. With the help of *in situ* neutron diffraction, we monitored and quantified the microstructural responses during tensile deformation, including the evolution of lattice strain, stack fault probability and dislocation density versus imposed strain at both temperatures. The different responses between 293 and 77 K were compared. We also calculated the stacking fault energy of the alloy at both 293 and 77 K. TEM observations were carried out on the deformed samples, providing correlative analysis. The work provides in-depth micro-mechanistic understanding involving the complex interaction of stacking faults, twins and dislocations for the studied tHEAs at cryogenic temperatures, which could pave the way for designing advanced metallic materials resistant to cryogenic environments.

2. Experimental details

The FeCoCrNi high entropy alloy was fabricated by powder metallurgical processes, which are detailed in Refs. [33, 35], namely, hot extrusion of gas-atomized FeCoCrNi powders. The alloy has a single fcc structure and the average grain size of the asextruded specimen was approximately 35 µm. The mechanical properties and microstructure of the alloy at room temperature can be found in Ref. [35]. In situ time-of-flight neutron diffraction measurements during tensile deformation were performed on the ENGIN-X neutron diffractometer, Rutherford Appleton Laboratory (RAL), ISIS, UK [36, 37]. A stress rig with a load capability of 100 KN was used for the experiments. An in-house built cold chamber, integrated with the stress rig, was used which provides a controlled cryogenic temperature environment (10-293 K) [38]. A schematic of the setup is shown in Fig. 1a. A low temperature extensometer was used to measure the displacement of the part of gauge length (10 mm). The rig was mounted on the diffractometer horizontally. The loading axis was oriented horizontally, parallel to the extruded direction and orientated 45° relatives to the incident beam. The two detectors (axial and radial) allow collection of the diffraction patterns at fixed horizontal scattering angles of ±90°, with diffraction vectors parallel and perpendicular to the loading direction, respectively. Dog bone-shaped uniaxial tensile specimens with a gauge length of 34.5 mm and diameter of 8 mm were prepared from the as-extruded material. A 4×4×4 mm³ neutron measurement gauge volume was used. Diffraction patterns were acquired for 20 min intervals between tensile loading steps, iterating until the sample failed. During the cooling down process for the cryogenic temperature deformation test, a stress level of 5 MPa was maintained via stress-control. During loading up, a stress-control was used before the yielding point, which was followed by strain-control. The diffraction spectra was analysed by Open G software which provides the information of d-spacing, peak intensity and full width at half maximum (FHWM). In order to calculate the stacking fault energy and dislocation density from the measured diffraction spectra, single peak fitting with a pseudo-voigt convolution was developed in Matlab. The measured diffraction patterns, after being deconvoluted with the instrument function, can be described by the convolution of a Gaussian and a Lorentz

122

123

124

125

126

127

128

129

130

131

132

133

134

135

136

137

138

139

140

141

142

function.

$$I(x) = I(0) \left[\mu \exp\left[-\pi \frac{(x - x_0)^2}{\beta_G^2} \right] + (1 - \mu) \frac{1}{\frac{\beta_C^2}{\pi^2} + (x - x_0)^2} \right]$$
(1)

143 where x_0 is the peak centre, and β_C and β_C are constant parameters of the Guassian and
144 Lorentz respectively. μ and $(1-\mu)$ denote the fraction of Guassian and Lorentz used. The
145 size strain and microstrain contribution are then related to the parameters of the
146 Guassian and Lorentz function by

$$D_{eff} = \frac{1}{\beta_c} \tag{2}$$

147 And

154

155

156

$$\langle \xi^2 \rangle_{hkl}^{1/2} = (\frac{2}{\pi})^{1/2} \beta_G d_{hkl} / 2 \tag{3}$$

respectively. D_{eff} is the effective dimension of coherently diffraction blocks (e.g. grains) and ξ is the microstrain and its root-mean-square could be interpreted to be proportional to the square root of dislocation density ($\rho^{1/2}$) as follows:

$$\rho = \frac{k\langle \xi^2 \rangle}{Fb^2} \tag{4}$$

where *b* represents the magnitude of Burgers vector. *F* and *k* are two constants, and *F* =1 and k = 1.61nm were chosen according to [39] for fcc crystal with a Burgers vector along <110>.

Transmission electron microscopy (TEM) study was conducted on a JEOL-2100 TEM operated at 200 kV to examine the microstructure of the specimens after the *in situ* neutron diffraction experiments. The TEM samples were extracted from regions close

to and away from the facture surfaces which represent samples with different strain levels. On the sample deformed at 77 K, TEM foils were extracted from the regions with cross-section diameters equal to 6.8 mm and 6.24 mm which correspond to reduction in the cross section area (ψ) during the tensile test of 27.8% and 39.2%, respectively. For sample deformed at 293 K, TEM foils were extracted from the regions with the cross-section diameters equal to 7.15 and 6.47 mm which correspond to the reduction in cross section area (ψ) during the tensile test of 20.1% and 34.6%, respectively. The foils extracted were ground down to ~80 μ m, then disks of 3 mm diameter were punched out and twin-jet electro-polished in a solution containing 100 mL HClO₄ and 900 mL CH₃COOH at approximately -10°C.

3. Results and discussion

3.1 Mechanical properties

Fig. 1b shows the true stress-true strain curves of the polycrystalline FeCoCrNi alloy tensile deformed to fracture at 77 and 293 K. The yield strength (YS) and ultimate tensile strength (UTS) increase from approximately 260MPa and 980MPa at 273 K to 480MPa and 1725 MPa at 77 K. The total elongation also increases from about 45% to 55% (corresponding to engineering strain of 55% and 72% respectively) as the test temperature is decreased from 293 to 77 K. This enhancement of strength and ductility of the tHEA alloys at cryogenic temperatures is also compared to a few selected previous studies, as summarized in Tab. 1. It can be shown that the yield strength and UTS often increased 1.5-2 times while the maximum elongation often increased 10-15% when the deformation temperature was dropped from 293 to 77 K. The mechanical

179 properties of FeCoCrNiMo_{0,23} alloy at both temperatures are also provided in Table 1 for comparison. It shows that micro-alloying the tHEA with Mo enhances the 180 mechanical properties. 181 The strain hardening rate (SHR), which represents by the derivative of the true stress 182 183 with respect to the true strain, is shown in Fig. 1c as a function of true stress. The area 184 below the line $d\sigma/d\varepsilon = \sigma$ reveals the region in which necking is predicted to occur according to Considre's criterion. The SHRs of the alloy at 77 and 293 K show a similar 185 186 trend, whereas two distinguished stages can be found in both curves – rapid drop of the 187 strain hardening rate at small stress level, then the decrease slows down at higher stress. The transition points between the two stages are marked in Fig. 1b. The transition point 188 189 for room temperature tensile test is at 410 MPa (5.6 %) true stress (strain) level, whereas 190 at 77 K, it is 682 MPa (6.3 %) true stress (strain). The SHR at 77 K is higher than at 191 room temperature, which is consistent with other studies [5, 6, 23]. 192 In summary, the FeCoCrNi alloy has significantly improved strength, ductility and 193 strain hardening capability at 77 K than at room temperature. The underlying mechanisms will be discussed with the help of *in situ* neutron diffraction and correlative 194 195 electron microscopies in the following sections. 3.2 The evolution of lattice strain 196 As shown in Fig. 2, the tHEA is a fcc single phase structure at both 293 and 77 K before 197 deformation. The lattice parameters at 293 and 77 K are 0.3604 and 0.3563 nm, 198

respectively, calculated by the average of five diffraction peaks. Cooling the sample to

199

deformation at both 293 and 77 K, the tHEA stays as a fcc structure (no additional peaks belongs to bcc and hcp structure appears), which means that martensite transformation do not occur in this alloy.

The changes in lattice strains can be calculated using

206

207

208

209

210

211

212

213

214

215

216

217

218

219

220

$$\varepsilon_{hkl} = \frac{d_{hkl} - d_{hkl}^0}{d_{hkl}^0} \tag{4}$$

where ε_{hkl} is the lattice strain in the $\{hkl\}$ grain family, d_{hkl} is the current sample lattice spacing and d_{hkl}^0 is the stress-free lattice spacing. The stress-free lattice spacing was taking from the measurement point at 5 MPa at the temperatures. Elastic lattice strains along the axial and radial directions in grain families having {111}, {200}, {220}, {311} and {222} crystallographic planes during tensile deformation at 77 and 293K, are shown in Fig. 2a and 2b, respectively. The uncertainties in the measured internal strains were approximately 30 microstrain [40]. Fig. 2a shows that the lattice strains increased with applied stress linearly from 0 to 450 MPa, and then nonlinearly when the applied stress was greater than 450MPa during tensile loading at 77 K. This is due to the fact that the load transfers from softer grain families (e.g. 220) to harder grain families (e.g. 200) [33]. The trend of lattice strain evolution at 293 K is similar to that at 77 K, except the nonlinear transition happened earlier than that at 77 K (above ~ 250MPa). Overall, at 77 K, the lattice strain values of all grain families in the axial direction are larger than at 293 K under similar deformation level.

We determined grain orientation dependent diffraction elastic constants (E_{hkl}) and Poisson's ratios (V_{hkl}) through fit linear responses to the purely elastic parts of each curve in Fig. 2. $E_{Rietveld}$ and $V_{Rietveld}$ have also determined through preform the Rietveld fitting of 8 peaks. All these values are listed in Tab. 2. The E_{hkl} values are very similar for both temperatures. The $E_{Rietveld}$, $V_{Rietveld}$ and V_{hkl} , are slightly lower at cryogenic temperatures than room temperature. Daymond et al. [41] show that the value of $E_{Rietveld}$ is very similar to the macroscopic Young's modulus. The current temperature dependent values of $E_{Rietveld}$ are compared with the temperature dependent Young's moduli of CoCrFeMnNi in Ref. [42] with excellent agreement.

3.3 Stacking fault probability

Before we start analysing the stacking fault probability (SFP), we shall note the relationship between twins and stacking faults. Upon deformation, passage of Shockley partial dislocation with Burger vector 1/6<112> on neighbouring two (111) planes creates an intrinsic stacking fault, and continuous passage of the partial dislocations on successive (111) planes creates multi-layer faults forming twin nucleuses; in the end larger twins can be formed by passage of more partials on neighbouring (111) planes [43]. For alloys with stacking fault between 18<SFE<45 mJ/m², twinning is more favourable to occur with external straining. At SFE values <18mJ/m², martensite formation occurs when the molar Gibbs energy of martensitic is negative. This martensitic transformation takes place either by fcc-hcp, or, for even lower SFE, martensite formation by fcc-hcp-bcc becomes the favoured transformation mechanism that affects the further deformation of the material [13]. The fcc to hcp transformation

243 can occur by shifting every two neighboring fcc (111) planes in the [11-2] direction by a distance of a/sqrt(6) (where a is the lattice parameter), which is realised by the partial 244 dislocation movements in the (111) planes [14]. When SFE exceeds 45 mJ/m², 245 plasticity and strain hardening are controlled solely by the glide of dislocations [15]. 246 247 Many studies [33, 44-46] have shown that stacking faults, if they occur in fcc crystals, 248 can change the Bragg scattering positions compared with a fault-free lattice. The peak 249 position shifts for successive orders of reflections such as {111} and {222} might be 250 different arising from the structure factor for stacking faults. This can be used to 251 estimate the stacking fault density in the sample. 252 We plot the lattice strain evolutions of {111} and {222} at axial and radial directions 253 for 77 and 293 K tensile tests in Fig. 4a and 4b, respectively. The separation of {111} 254 and {222} lattice strain in the axial direction after certain amount of strain is obvious 255 for both temperatures, which indicates the formation of stacking faults and possibly 256 twins in grains whose {hkl}|| plane-normals oriented "parallel" to the loading axis. Interestingly, at room temperature, the {111} and {222} lattice strain curves in the 257 258 radial detector bank, almost overlap for the sample deformed. However, at 77K, the two lattice strain show distinct difference. The radial detector registers a portion of the 259 260 grains whose {hkl} \preceq plane-normals are "perpendicular" to the loading axis. The results suggest that those grains registered are unfavourable for twinning at room 261 262 temperature but form stacking faults and twins at 77 K. In addition, it shows that 263 twinning and stacking fault formation are strongly orientation-dependent (e.g. grains

with {hkl}|| plane-normal oriented "parallel" to the loading axis are easier to form stacking faults and twins). At cryogenic temperature, twin nucleation and growth can be triggered in grains whose orientation is unfavourable for twinning at room temperatures.

Both (hkl) dependent macro-strain ($\varepsilon_{hkl}^{strain}$) and stacking faults (ε_{hkl}^{sf}) can contribute to the change of lattice strain (ε_{hkl}^{exp}) measured by the peak shift in the experiment. The measured lattice strain (ε_{hkl}^{exp}), (hkl) dependent macro-strain ($\varepsilon_{hkl}^{strain}$) and stacking faults (ε_{hkl}^{sf}) follow a relationship:

$$\varepsilon_{hkl}^{exp} = \varepsilon_{hkl}^{strain} - \varepsilon_{hkl}^{sf} = \varepsilon_{hkl}^{strain} - \frac{\sqrt{3}}{4\pi} \frac{\sum_{b} \pm (h+k+l)}{(u+b)(h^2+k^2+l^2)} SFP \tag{7}$$

where u and b are the numbers of non-broadened and broadened component due to 272 stacking faults; SFP represents stacking fault probability. With the help of Eq. (7), we 273 274 are able to calculate the stacking fault probability, which directly indicates the density 275 of stacking faults. The evolution of the stacking fault probability during loading up at 77 and 293 K 276 277 obtained from Eq. 7 are shown in Fig. 4a and 4b. At 77 K, the SFP increases from 0 to 3×10⁻³ after true strain reaches approximately 4.8%. After this, the SFP increases 278 279 almost linearly with the increase of true strain, especially after the true strain is larger than 10%. The SFP increases to 25.6×10^{-3} at the strain level of 47% (close to failure). 280

At 293 K, the SFP fluctuates below 0 when the true strain is smaller than 10%. After

10% true train, the SFP becomes positive and increases with true strain steadily up to 5.4×10^{-3} at the strain level of 48.6%, which is about five times smaller than that at 77 K. The evolutions of SFP with applied true strains for both temperatures can be fitted with a linear function in the true strain range from 3% to 55% (Fig. 4a and 4b). The slope at 77 K is 0.72, which is about three times larger than that at 293K (0.24). The fact that at 77 K, compared to room temperature, the sample shows much higher SFP at similar strain level and the SFP curve is much steeper, suggests that at low temperatures, the FeCoCrNi alloy can form more stacking faults in the sample and the nucleation and growth of twins might be much quicker than at room temperature. We then plot the SFP as a function of true stress of the FeCoNiCr and FeCoNiCrMo_{0.23} at both 77 and 293 K, as shown in Fig. 4c. For both alloys, the SFP values of the two deformation temperatures almost overlap at the same stress level when the true stress is over roughly 450 MPa. This implies that the density of stacking faults of tHEAs is mainly a function of stress levels, regardless of deformation temperature. FeCoNiCrMo_{0.23} alloy shows similar behaviour. At the same stress, the alloy with Mo

3.4 Stacking fault energy

addition has a slightly higher SFP.

282

283

284

285

286

287

288

289

290

291

292

293

294

295

296

297

298

299

300

301

The stacking fault energy (SFE) represents the easiness of dissociating a perfect dislocation into two partial dislocations and the tendency for the formation of SFs. It can be calculated by Reed and Schramm's equation [47]. Note that the SFE we

measured here by neutron diffraction is the so-called intrinsic stacking fault energy (γ_{iSF}) .

$$\gamma_{iSF} = \frac{6.6a_0}{\pi\sqrt{3}} \left(\frac{2c_{44}}{c_{11} - c_{12}}\right)^{-0.37} \frac{\langle \xi^2 \rangle_{111}}{SFP} \left(\frac{c_{44} + c_{11} - c_{12}}{3}\right) \tag{8}$$

where, γ_{iSF} is the intrinsic stacking fault energy, a_0 is the lattice parameter. 304 $\langle \xi^2 \rangle_{111}$ is the mean square microstrain, which is obtained by an integral breadth 305 method with a pseudo-voigt convolution [48]. The single crystal elastic constants 306 (SCEC) (C_{11} =271.0 GPa, C_{12} = 175.0 GPa, and C_{44} =189.3 GPa) are adopted from ab 307 *initio* atomistic simulation on an fcc FeCoNiCr alloy at 0 K [49]. The SCEC varies only 308 slightly between 77 K and room temperature according to the simulation work [25]. 309 310 The stacking fault probability is measured at around engineering strain level of 48% for 311 both temperatures. The SFE of the FeCoCrNi high-entropy alloy is then estimated by Eq. 8 to be 13 mJ/m² at 77 K and 32.5 mJ/m² at 293 K (Tab. 3). Expression (8), 312 however, is still approximate and we cannot determine reliable error values. There are 313 likely errors related to the calculation of the mean square micro-strain. Also, the 314 variation of SCEC between different temperatures and the measurement of SCEC by 315 316 atomistic simulation is not taken into account and may add additional uncertainty in the 317 estimated SFE due to many assumptions included in the model [49]. However, 318 measurements of SCEC is very limited and we would expect that accurately measuring 319 SCEC, both by experiments and simulation as a function of temperature, will provide a more robust determination of SFE using eq. 8. We also estimated the SFE of a 320

321	FeCoNiCrMo _{0.23} to be 19 mJ/m ² at room temperature [33] and 10 mJ/m ² at 77 K (Table
322	3), which is lower than that of the FeCoNiCr alloy, suggesting that micro-alloying of
323	Mo can reduce the stacking fault energy of the tHEAs.
324	The estimated SFE at room temperature (32.5 mJ/m ²) agrees with the experimental
325	measurement on FeCoCrNi tHEA by the combined use of XRD and DFT simulation
326	(e.g. 17.4, 34.3 and 31.7 mJ/m ² depending on alloy composition used [50]) and TEM
327	(27±4 mJ/m ² [19]). Currently no experimental measurement of tHEAs' SFE at
328	cryogenic temperature is reported. Only a few simulations were performed on
329	FeCoNiCr alloy. Zhao et al. performed ab initio calculation on a series of fcc tHEAs.
330	Their results show that the SFE of FeCoNiCr stays negative at 0 K. Depending on which
331	models they used, the predicted SFE values vary around -20 mJ/m ² [19]). Zhang et al.
332	[26] reported that SFE at 0 K of fcc FeCoNiCr falls from -82 to -180 mJ/m ² . Beyramali
333	Kivyy and Asle Zaeem's simulation gives a SFE value of 31.6±0.9 mJ/m ² [19] although
334	the temperature at which the simulation was carried out is not reported. Our estimation
335	of SFE at 77 K may provide a validation for SFE simulations if one can carry out the
336	ab initio calculations at different temperatures such as the one performed by Huang et
337	al. on a FeCrCoNiMn alloy [25]. Their work obtains an SFE of 8 mJ/m ² at 77 K on
338	FeCrCoNiMn alloy, which is slightly lower than our measurement on the FeCrCoNi
339	alloy, indicating that variations in Mn contents can cause a change to SFE values.
340	The SFE is a critical parameter in the deformation properties of fcc metals and alloys.
341	The SFE influences phenomena such as the capacity of a dislocation to cross slip, the

formation of partial dislocation and twin boundaries [51]. Low SFE can lead to the domination of a highly planar slip on a well-defined (111) plane, suppressing dislocation cross-slip, hence augmenting the yield strength [51]. Additionally, Norihiko et al. [52] suggest that the increase of yield stress at cryogenic temperature of tHEAs is due to the thermal component of solid-solution hardening. The increase of yield stress at cryogenic temperature is due to both the thermal component of solid-solution hardening and the suppression of dislocation cross-slip. The very low SFE of the tHEA used in this study strongly supports the conclusion from section 3.3 that the alloy is prone to form twins when strained. Additionally, the drop of SFE at cryogenic temperatures suggests that more deformation twins are able to nucleate and grow when deformed at lower temperatures.

3.5 Critical stress for twinning (σ_{tw})

Experimental determination of σ_{tw} is challenging. It has been obtained via identifying the transition point in the work hardening curve [53], or through careful TEM observation on interrupted strained specimens [23, 35]. The critical stress for twinning was measured by a few studies using TEM previously, which demonstrates that the critical stress for twinning was independent of temperature and estimated to be ~720±30 for FeCrNiCoMn alloy [35] and 790±100 MPa for CrCoNi alloy [23]. The criteria used in those studies for determining the critical twinning stress level is that nano-twins start to be identified by TEM.

As we noted before, the stacking fault probability we measured is directly related to the
density of stacking faults. Hence the SFP curve might allow us to estimate critical points
of stacking fault and twinning formation. The SFP stays negative at very low strains,
and when it reaches over 0, it increases continuously as we increase deformation. The
first critical point we identify is when the stacking fault probability becomes positive
(just above 0). We use the linearly fitted equations (Fig. 4) to determine the stress level
at SFP=0, which are 450±30 MPa/9.6% strain at 77K and 500±15 MPa/0.717% strain
at 293 K. This point might mark the nucleation stage of stacking fault within the sample
as when stacking faults start to form, the peak positions of the (111) and (222) planes
begin to shift apart, reflecting the contribution from the stacking fault. However, due to
the large scattering of the SFP at lower strain levels, those values should be used with
-
cautions.
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a and 4b), at which sufficient and sizable stacking faults should have formed, lead to the
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a and 4b), at which sufficient and sizable stacking faults should have formed, lead to the nucleation of twin faults. The corresponding true stress values are 730±30 MPa/21.2%
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a and 4b), at which sufficient and sizable stacking faults should have formed, lead to the nucleation of twin faults. The corresponding true stress values are 730±30 MPa/21.2% strain at 293 K and 635±30 MPa/4.885% strain at 77 K (Table 3). The measurement is
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a and 4b), at which sufficient and sizable stacking faults should have formed, lead to the nucleation of twin faults. The corresponding true stress values are 730±30 MPa/21.2% strain at 293 K and 635±30 MPa/4.885% strain at 77 K (Table 3). The measurement is consistent with previous studies using TEM [23, 35], suggesting that the SFP curve
The second critical point we consider is when SFP = 0.003 (the purple line in Fig. 4a and 4b), at which sufficient and sizable stacking faults should have formed, lead to the nucleation of twin faults. The corresponding true stress values are 730±30 MPa/21.2% strain at 293 K and 635±30 MPa/4.885% strain at 77 K (Table 3). The measurement is consistent with previous studies using TEM [23, 35], suggesting that the SFP curve could be a reliable way to measure the critical stress for twinning.

stress for twinning (τ_{twin}) is proportional to intrinsic stacking fault energy (γ_{isf}) [53] $(\tau_{twin} \times b_p \sim \gamma_{isf})$. Based on this, various equations have been formulated, and we choose a few as shown in Table 4, together with the twinning stress values predicted based on the equations. The predicted twinning stress values seem to be temperature dependent. A significant discrepancy among different equations can also be observed. The huge variations of twinning stress among different models demonstrate that a systematic validation of the models with experiments is critically needed. Narita and Takamura's and Venable's models predict relatively low σ_{tw} . It is even lower than the yield strength at 77 K. Byun's model, on the other hand, gives relatively high values. According to Byun's model, a twinning stress of 1353 MPa is needed to prompt deformation twin at room temperature, which is above the UTS of the alloy. If this is the case, deformation twinning is very unlikely to form during room temperature deformation, unless some grains experience significant stress concentration. This is in contradiction with our TEM observation (TEM confirms the formation of nano-twins within the tensile strained sample, section 3.8). It has been suggested that Byun's model overestimates the twinning stress in TWIP steels [53], which seems to be the case according to our result. The twinning stresses predicted by Steinmetz et al. model (661 MPa at 77K, 799 MPa at 293 K) seems to agree reasonably well with the twinning stress values we determined from the SFP curves (635 MPa at 77K, 730 MPa at 293 K). Steinmetz et al. model, based on Mahajan-Chin three-layer twinning mechanism, has also been shown to accurately predict the twinning stress in TWIP steels [53].

383

384

385

386

387

388

389

390

391

392

393

394

395

396

397

398

399

400

401

402

It has been suggested that intrinsic SFE alone is not sufficient to predict deformation twinning mechanisms [53]. The generalized planar fault energy concept, recently developed, has proposed that the stacking fault formation and twinning process are controlled by the energy barriers, rather than just the intrinsic stacking fault energy. The energy barriers include the intrinsic stacking fault energy, the unstable stacking fault energy, the extrinsic stacking fault energy and the unstable twin fault energy [53]. The twinning stress is then directly correlated to the unstable twinning fault energy, together with the intrinsic stacking fault energy. However, to determine the unstable twinning fault energy by experiments is not possible, and it usually requires using first principle calculation. Hence, to accurately determine the critical twinning stress, *ab initio* calculation needs to be performed, which should be validated against the experimental values via the combined use of interrupted TEM investigation [23, 35] and *in situ* diffraction methods as demonstrated here.

3.6 Evolution of dislocation density

The higher strain hardening rate at 77 K could result from the high dislocation density in fcc matrix as well as the interaction between dislocations and nano-twins. Here, the dislocation density during tensile deformation at 77 and 293 K are measured using Eq. 3, which are shown in Fig. 5a as a function of true strain. It indicates that the dislocation density increases as the strains/stress increases. At the cryogenic temperature, a much higher density of dislocations is accumulated after plastic deformation. A linear

424 equation $(\rho = \rho_0 + K\varepsilon)$ can be used to describe the dislocation density and true strain 425 relationship:

$$\rho = 1.4 \times 10^{15} + 7.6 \times 10^{13} \varepsilon \tag{10}$$

and
$$\rho = 1.5 \times 10^{15} + 3.5 \times 10^{13} \varepsilon$$
 (11)

426 at 77 and 293 K, respectively.

429

430

431

The increases in the tensile stress, $\Delta \sigma$, due to forest dislocation interactions can be 427 428 described by:

$$\Delta \sigma = \alpha M G b \rho^{1/2} \tag{12}$$

where α is a constant, M is the Taylor factor (3.06), G is the shear modulus (85 GPa at 77 K; 80 GPa at 293K [42, 56]), b is the magnitude of the Burgers vector $(0.252 \text{ nm at } 77 \text{ K} \text{ and } 0.253 \text{ nm at } 293 \text{ K}) \text{ and } \rho \text{ is the dislocation density. Fig. 5b}$ shows the normalized increment of stresses $(\sigma - \sigma_v)/MG$ (where σ is the current stress) 432 433 at both 77 and 293 K, which can be fitted with a linear function. Only data beyond the 434 yielding is included. The slope of the linear function at 77 K is 0.53 which agrees with 435 that found in CrMnFeCoNi [6]. The slope of the linear function at 293 K is 0.95, which almost doubles the value at 77 K. However, we note that the physical meaning of α is 436 437 not very clear hence it is hard to interpret, and Eq. 12 ignores the contribution from the 438 other sources including dislocation-mechanical twin boundary interaction.

Gini *et al.* [57] proposed an equation that incorporates Eq. 12 and the plasticity model of Nes and Marthinsen [58]:

$$\Delta \sigma = \alpha M G b \rho^{1/2} + \frac{M \beta G b}{\Lambda} \tag{13}$$

where Λ is the dislocation mean free path, and β is a constant. The formation of mechanical twins reduces the dislocation mean free path. Thereby, according to Eq.13, it is the dynamic increase of boundaries, due to the formation of mechanical twinning, together with the continuously increase of dislocation density that leads to the enhanced strain hardening behaviour of the tHEA during plastic deformation.

3.7 Peak intensity

441

442

443

444

445

446

447

448

- Fig. 6 also shows the normalized peak intensity evolution of several lattice reflections parallel and perpendicular to the load axis versus true stress. A few points can be drawn regarding the changes of peak intensity and the differences at 77 and 293K:
- The peak intensity of the axial (220) decreased significantly when the applied 450 (i) 451 load was larger than the macroscopic yielding, as shown in Fig. 6. The (220) 452 peak at axial direction almost vanished when the applied stress was above 1500 MPa at 77 k and 800 MPa at 293 K. The fact that the (220) peak disappears 453 when the sample is strained close to failure in both samples is very interesting 454 and has been observed before in a FeCoNiCrMo_{0.23} alloy as well. In contrast, 455 the peak intensity of 220 at radial direction increased by a factor of 1.1 to 2 456 during the whole deformation. 457

- 458 (ii) The peak intensity of (200) at both axial and radial directions increased significantly at 77 K, but hardly changed at 293K.
- 460 (iii) For (111) and (222) grains families, the peak intensity increased in axial direction by a factor of 3 at 77 K but decreased in radial direction. The final peak intensity of (222) and (111) changed by a factor of ~5.5 at 293 K.

Significant difference in peak intensity evolution at 77 and 293 K was observed, signifying the different behaviour in terms of the re-orientation of grains during the tensile deformation, which could be due to slip/rotation of grains [59] and/or formation of mechanical twins [60]. However, it is not easy to distinguish the contribution from grain rotation and mechanical twins.

3.8 Microstructure characterisation

The microstructures of the deformed specimens after the *in situ* neutron studies were analysed by transmission electron microscopy (TEM) in order to gain a better understanding of the controlling deformation mechanisms. TEM bright field (BF) images and selected area diffraction patterns (SADP) of the samples deformed at 77 and 293 K are shown in Figs. 7 and 8, respectively, showing that nano-sized lamellas have formed to accommodate strain when the sample was deformed at both temperatures. The lamellas are twin structure as confirmed by the diffraction patterns in Fig. 7d and 8d. TEM samples for Fig. 7a and 7b are taken from the failed *in situ* samples at different reductions in cross-section area (ψ). The twin-twin intersections can also be readily observed in Fig. 7a and 7b, which can form a complex 3-dimensional network inhibiting dislocation propagation. Fig. 7a and 7b also show that at 77 K more

twins are formed at higher strain level. Comparing Fig. 7 with Fig.8, we conclude that less twins and twin-twin intersections are formed at room temperature, consistent with our measurement from *in situ* neutron diffraction. We do not observe matensite phase at both temperature through TEM, again, consistent with our observation by neutron diffraction (Fig. 2). A further drop of deformation temperature might lead to the formation of martensite as SFE will become ever lower.

The dramatic increase of nano-twins and twin-twin intersections at lower temperatures plays a key role for the higher strain hardening ability the alloy achieved at 77 K than 293 K as shown in Fig. 1b. The combination of enhanced dislocation hardening (higher dislocation density during cryogenic deformation) and mechanical twinning (higher twin volume fraction during cryogenic deformation) provide a larger work hardening rate during tensile deformation at 77 K than at 293 K.

4. Conclusions

In our work, we fabricated a FeCoNiCr high entropy alloy with a single phase fcc structure using a powder metallurgy route. We used *in situ* neutron diffraction to map the evolution of deformation microstructure at both 77 and 293 K, correlatively characterized by TEM. Several conclusions can be drawn based on the experimental results:

The alloy has a good combination of high ultimate tensile strength (UTS ~1725
 MPa) and ductility (elongation~55%) at 77 K, which is much higher than the room temperature properties (UTS ~ 980 MPa, and elongation ~45%). Higher

strain hardening rate is also obtained at cryogenic temperature than at room temperature.

- Via in situ neutron diffraction measurement, we are able to determine the stacking fault probability (SFP) as a function of stress level at both 77 and 293
 K. The SFP increases much quicker and reaches a much higher value at similar strain levels at cryogenic temperature than room temperature.
- 3. Using diffraction line profile analysis, stacking fault energy is estimated to be ~13 mJ/m² at 77 K and ~32.5 mJ/m² at 293 K. As the SFE drops at cryogenic temperature, more twin faults form as the alloy is deformed at cryogenic temperatures. Nano-twins at both 77 and 293 K of the alloy have been observed by TEM, and at 77 K, many more twins and twin-twin intersections are formed than at room temperature.
- 4. We used the stacking fault probability curve to determine the critical stress for twinning. The critical stress for twinning is set to stress levels when the SFP is 0.003. The corresponding true stress values are 730±30 MPa at 293 K and 635±30 MPastrain at 77 K, which agree with previous measurements on CrCoNi and CrMnFeCoNi alloys as well as Steinmetz *et al.* model.
- Dislocation density is calculated for both temperatures from neutron diffraction spectra. Higher dislocation density is found during low temperature plastic deformation than at room temperature.

6. The combination of dislocation hardening and mechanical twinning provides large work hardening rate and high strength during tensile deformation for the high entropy alloy. The superior mechanical properties at the cryogenic temperature is attributed to the enhanced dynamic Hall-Petch hardening and dislocation hardening as at lower temperatures, increased amount of nano-twins and dislocation are formed.

Acknowledgements

The authors thank ISIS (the Rutherford Appleton Laboratory, UK) for providing the beamtime (RB1610297) and staff at EnginX beamline for support. Y.Q.W. and P.D.L. acknowledge the support provided by the Research Complex at Harwell, funded in part by EPSRC ((EP/K007734/1 and EP/L018705/1).. B.C. acknowledges the support from Diamond Birmingham Collaboration. Y.L. and B.L. acknowledge the National Natural Science Foundation of China (51671217), and the Projects of Innovation-driven Plan in Central South University of China (2015CX004).

Tables

 Table 1. Comparison of yield strength (YS), ultimate tensile strength (UTS), and total elongation obtained at 77K and 293K from the present study to selected prior studies.

Materials	Temp. (K)	YS (MPa)	UTS (MPa)	Elongation (%)
E.C.C.Wi	77	480	1725	55
FeCoCrNi	293	260	980	45
E-C-C-NiM-	77	602	1863	51
FeCoCrNiMo _{0.23}	293	360	1238	48
CrCaNi: [22]	77	560	1625	44
CrCoNi [23]	293	360	750	30
CaMa Fo Co Ni: 161	77	460	1060	60
CrMnFeCoNi [6]	293	265	600	45

Table 2. Uniaxial materials properties of FeCoCrNi HEA at 77 and 293 K

Temp.	a	E ₁₁₁	E ₂₀₀	E ₂₂₀	E ₃₁₁	E _{Rietveld}	V_{111}	V_{200}	V_{220}	V ₃₁₁	$V_{ m Rietveld}$
(K)	(nm)	(GPa)	(GPa)	(GPa)	(GPa)	(GPa)					
77	0.3563	146.3	97.0	191.6	214.0	<mark>229</mark>	0.138	0.232	0.168	0.234	0.20
293	0.3604	136.6	98.0	175.0	237.2	190	0.198	0.349	0.348	0.321	0.27

Table 3. Stacking fault energy of FeCoCrNi tHEA at 77 and 293 K

	FeCoCrNi	FeCoCrNi	FeCoCrNiMo _{0.23}	FeCoCrNiMo _{0.23}
Temperature	77 K	293 K	77 K	293 K
SFE (mJ/m ²)	13	32.5	10	19
Twinning Stress	635 ± 30	730 ± 30	-	-

Table 4. Critical stress for twinning of FeCoCrNi tHEA at 77 and 293 K

Sources	Equations	Temp.	$ au_{tw}(\text{MPa})$	σ_{tw} (MPa)
Narita and	$\tau_{tw} = \frac{\gamma_{isf}}{2b_n}$	77 K	45	135
Takamura [55]	$2b_p$	293 K	110	337
Venable [54, 61]	$\tau_{tw} = \frac{b\gamma_{isf}}{b_p(nb - b_p)}$	77 K	37-63	113-193
	$b_p(nb-b_p)$	293 K	91-155	278-474
Byun [62]	$\tau_{tw} = \frac{2\gamma_{isf}}{b_n}$	77 K	178	545
2) ## [02]	b_p	293 K	442	1353
Steinmetz et al. [63]	$\tau_{tw} = \frac{\gamma_{isf}}{3b_p} + \frac{3Gb_p}{L_0}$	77K	216	661
	$3b_p$ L_0	293 K	261	799

^{*} n is the stress-concentration factor (n=1 represents no stress concentration while $n \ge 3$ means static tension, here n = 2-3) [20];

^{*} L_0 is the width of a twin embryo (approximately 200 nm);

^{*} $\sigma_{tw} = M\tau_{tw}$, where *M* is the Taylor factor.

563564 List of figures

- Fig. 1. (a) Schematic of the in situ neutron diffraction set-up; (b) True stress-strain
- curves of uniaxial tensile tests at 77 K and 293 K and (c) the corresponding working
- hardening rate versus true stress.
- Fig. 2. Diffraction patterns collected at the axial detector as a function of stress at (a)
- 569 293 K; and (b) 77 K.
- 570 Fig. 3. The evolution of elastic lattice strains along the axial and radial directions in
- grain families having {111}, {200}, {220}, {311} and {222} crystallographic planes
- during tensile loading at (a) 77 K and (b) 293 K;
- 573 Fig. 4. The (111) first order and (222) second order reflections together with the
- stacking fault probability as a function of true strain at (a) 77 K and (b) 293 K.
- Fig. 5. The evolution of dislocation density versus (a) true strain, and (b) normalised
- 576 work hardening $(\sigma \sigma_v)/MG$ versus $b\rho^{1/2}$.
- Fig. 6. The evolution of normalized peak intensity along the axial and radial directions
- in grain families having {111}, {200}, {220}, {311} and {222} crystallographic planes
- 579 during tensile loading at (a) 77 K and (b) 293 K.
- Fig. 7. TEM bright field micrographs of samples with (a) 27.8 % and (b) 39.2% strain
- at 77 K, which show nano-twins. (c) Higher magnification BF images with an inserted
- SAD pattern obtained from the matrix and (f) the composite SAD pattern obtained from
- 583 the blue circled region in Fig. 7c which has contribution from both the matrix and the
- 584 nano-twin.
- Fig. 8. TEM bright field micrographs of samples with (a) 20.1% and (b) 34.6% strain
- at 293k, which show nano-twins. (c) Higher magnification BF images with an inserted
- SAD pattern obtained from the matrix and (f) the composite SAD pattern obtained from
- the blue circled region in Fig. 8c which has contribution from both the matrix and the
- 589 nano-twin.

590

591

592

Reference

- 596 [1] B. Cantor, I. Chang, P. Knight, A. Vincent, Microstructural development in
- 597 equiatomic multicomponent alloys, Materials Science and Engineering: A 375 (2004)
- 598 213-218.
- 599 [2] J.W. Yeh, S.K. Chen, S.J. Lin, J.Y. Gan, T.S. Chin, T.T. Shun, C.H. Tsau, S.Y.
- 600 Chang, Nanostructured high-entropy alloys with multiple principal elements: novel
- alloy design concepts and outcomes, Advanced Engineering Materials 6(5) (2004) 299-
- 602 303.
- 603 [3] B. Gludovatz, A. Hohenwarter, D. Catoor, E.H. Chang, E.P. George, R.O. Ritchie,
- A fracture-resistant high-entropy alloy for cryogenic applications, Science 345(6201)
- 605 (2014) 1153-1158.
- 606 [4] F. Otto, A. Dlouhý, C. Somsen, H. Bei, G. Eggeler, E.P. George, The influences of
- 607 temperature and microstructure on the tensile properties of a CoCrFeMnNi high-
- 608 entropy alloy, Acta Materialia 61(15) (2013) 5743-5755.
- 609 [5] J. Moon, S.I. Hong, J.W. Bae, M.J. Jang, D. Yim, H.S. Kim, On the strain rate-
- 610 dependent deformation mechanism of CoCrFeMnNi high-entropy alloy at liquid
- 611 nitrogen temperature, Materials Research Letters (2017) 1-6.
- 612 [6] G. Laplanche, A. Kostka, O. Horst, G. Eggeler, E. George, Microstructure evolution
- and critical stress for twinning in the CrMnFeCoNi high-entropy alloy, Acta Materialia
- 614 118 (2016) 152-163.
- 615 [7] A. Gali, E.P. George, Tensile properties of high-and medium-entropy alloys,
- 616 Intermetallics 39 (2013) 74-78.
- [8] Z. Li, K.G. Pradeep, Y. Deng, D. Raabe, C.C. Tasan, Metastable high-entropy dual-
- phase alloys overcome the strength–ductility trade-off, Nature 534(7606) (2016) 227.
- 619 [9] D.T. Pierce, J.A. Jiménez, J. Bentley, D. Raabe, J.E. Wittig, The influence of
- stacking fault energy on the microstructural and strain-hardening evolution of Fe–Mn–
- 621 Al–Si steels during tensile deformation, Acta Materialia 100 (2015) 178-190.
- 622 [10] K. Yan, D.G. Carr, M.D. Callaghan, K.-D. Liss, H. Li, Deformation mechanisms
- 623 of twinning-induced plasticity steels: In situ synchrotron characterization and
- 624 modeling, Scripta Materialia 62(5) (2010) 246-249.
- 625 [11] K. Rahman, V. Vorontsov, D. Dye, The effect of grain size on the twin initiation
- 626 stress in a TWIP steel, Acta Materialia 89 (2015) 247-257.
- 627 [12] M. Jo, Y.M. Koo, B.-J. Lee, B. Johansson, L. Vitos, S.K. Kwon, Theory for
- 628 plasticity of face-centered cubic metals, Proceedings of the National Academy of
- 629 Sciences 111(18) (2014) 6560-6565.
- 630 [13] S. Curtze, V.-T. Kuokkala, Dependence of tensile deformation behavior of TWIP
- steels on stacking fault energy, temperature and strain rate, Acta materialia 58(15)
- 632 (2010) 5129-5141.

- 633 [14] K. Tao, J.J. Wall, H. Li, D.W. Brown, S.C. Vogel, H. Choo, In situ neutron
- diffraction study of grain-orientation-dependent phase transformation in 304L stainless
- steel at a cryogenic temperature, Journal of applied physics 100(12) (2006) 123515.
- 636 [15] O. Grässel, L. Krüger, G. Frommeyer, L. Meyer, High strength Fe–Mn–(Al, Si)
- 637 TRIP/TWIP steels development—properties—application, International Journal of
- 638 plasticity 16(10-11) (2000) 1391-1409.
- 639 [16] H. Barman, A. Hamada, T. Sahu, B. Mahato, J. Talonen, S. Shee, P. Sahu, D.
- Porter, L. Karjalainen, A Stacking Fault Energy Perspective into the Uniaxial Tensile
- Deformation Behavior and Microstructure of a Cr-Mn Austenitic Steel, Metallurgical
- and Materials Transactions A 45(4) (2014) 1937-1952.
- 643 [17] Y. Tian, L. Zhao, S. Chen, A. Shibata, Z. Zhang, N. Tsuji, Significant contribution
- of stacking faults to the strain hardening behavior of Cu-15% Al alloy with different
- grain sizes, Scientific reports 5 (2015) 16707.
- [18] X. Xu, P. Liu, Z. Tang, A. Hirata, S. Song, T. Nieh, P. Liaw, C. Liu, M. Chen,
- Transmission electron microscopy characterization of dislocation structure in a face-
- centered cubic high-entropy alloy Al0. 1CoCrFeNi, Acta Materialia 144 (2018) 107-
- 649 115.
- 650 [19] S. Liu, Y. Wu, H. Wang, J. He, J. Liu, C. Chen, X. Liu, H. Wang, Z. Lu, Stacking
- fault energy of face-centered-cubic high entropy alloys, Intermetallics (2017).
- 652 [20] H. Diao, R. Feng, K. Dahmen, P. Liaw, Fundamental deformation behavior in
- 653 high-entropy alloys: An overview, Current Opinion in Solid State and Materials
- 654 Science (2017).
- 655 [21] C.L. Tracy, S. Park, D.R. Rittman, S.J. Zinkle, H. Bei, M. Lang, R.C. Ewing, W.L.
- Mao, High pressure synthesis of a hexagonal close-packed phase of the high-entropy
- alloy CrMnFeCoNi, Nature communications 8 (2017) 15634.
- 658 [22] F. Zhang, S. Zhao, K. Jin, H. Bei, D. Popov, C. Park, J.C. Neuefeind, W.J. Weber,
- Y. Zhang, Pressure-induced fcc to hcp phase transition in Ni-based high entropy solid
- solution alloys, Applied Physics Letters 110(1) (2017) 011902.
- 661 [23] G. Laplanche, A. Kostka, C. Reinhart, J. Hunfeld, G. Eggeler, E. George, Reasons
- for the superior mechanical properties of medium-entropy CrCoNi compared to high-
- entropy CrMnFeCoNi, Acta Materialia 128 (2017) 292-303.
- 664 [24] P. Sahu, S. Shee, A. Hamada, L. Rovatti, T. Sahu, B. Mahato, S.G. Chowdhury,
- D. Porter, L. Karjalainen, Low strain rate deformation behavior of a Cr–Mn austenitic
- steel at 80° C, Acta Materialia 60(20) (2012) 6907-6919.
- 667 [25] S. Huang, W. Li, S. Lu, F. Tian, J. Shen, E. Holmström, L. Vitos, Temperature
- dependent stacking fault energy of FeCrCoNiMn high entropy alloy, Scripta Materialia
- 669 108 (2015) 44-47.
- 670 [26] Y. Zhang, Y. Zhuang, A. Hu, J. Kai, C. Liu, The origin of negative stacking fault
- energies and nano-twin formation in face-centered cubic high entropy alloys, Scripta
- 672 Materialia 130 (2017) 96-99.
- [27] Z. Zhang, H. Sheng, Z. Wang, B. Gludovatz, Z. Zhang, E.P. George, Q. Yu, S.X.
- Mao, R.O. Ritchie, Dislocation mechanisms and 3D twin architectures generate

- exceptional strength-ductility-toughness combination in CrCoNi medium-entropy
- alloy, Nature communications 8 (2017) 14390.
- 677 [28] S. Zhao, G.M. Stocks, Y. Zhang, Stacking fault energies of face-centered cubic
- 678 concentrated solid solution alloys, Acta Materialia 134 (2017) 334-345.
- [29] Z. Zhang, M. Mao, J. Wang, B. Gludovatz, Z. Zhang, S.X. Mao, E.P. George, Q.
- Yu, R.O. Ritchie, Nanoscale origins of the damage tolerance of the high-entropy alloy
- 681 CrMnFeCoNi, Nature communications 6 (2015) 10143.
- [30] J. Liu, C. Chen, Y. Xu, S. Wu, G. Wang, H. Wang, Y. Fang, L. Meng, Deformation
- twinning behaviors of the low stacking fault energy high-entropy alloy: An in-situ TEM
- 684 study, Scripta Materialia 137 (2017) 9-12.
- 685 [31] M. Wang, Z. Li, D. Raabe, In-situ SEM observation of phase transformation and
- twinning mechanisms in an interstitial high-entropy alloy, Acta Materialia 147 (2018)
- 687 236-246.
- 688 [32] L. Ma, L. Wang, Z. Nie, F. Wang, Y. Xue, J. Zhou, T. Cao, Y. Wang, Y. Ren,
- Reversible deformation-induced martensitic transformation in Al 0.6 CoCrFeNi high-
- entropy alloy investigated by in situ synchrotron-based high-energy X-ray diffraction,
- 691 Acta Materialia 128 (2017) 12-21.
- 692 [33] B. Cai, B. Liu, S. Kabra, Y. Wang, K. Yan, P.D. Lee, Y. Liu, Deformation
- 693 mechanisms of Mo alloyed FeCoCrNi high entropy alloy: In situ neutron diffraction,
- 694 Acta Materialia 127 (2017) 471-480.
- 695 [34] Y. Wu, W. Liu, X. Wang, D. Ma, A.D. Stoica, T. Nieh, Z. He, Z. Lu, In-situ
- 696 neutron diffraction study of deformation behavior of a multi-component high-entropy
- 697 alloy, Applied Physics Letters 104(5) (2014) 051910.
- 698 [35] B. Liu, J. Wang, Y. Liu, Q. Fang, Y. Wu, S. Chen, C. Liu, Microstructure and
- 699 mechanical properties of equimolar FeCoCrNi high entropy alloy prepared via powder
- 700 extrusion, Intermetallics 75 (2016) 25-30.
- 701 [36] J. Santisteban, M. Daymond, J. James, L. Edwards, ENGIN-X: a third-generation
- neutron strain scanner, Journal of Applied Crystallography 39(6) (2006) 812-825.
- 703 [37] S.Y. Zhang, A. Evans, E. Eren, B. Chen, M. Pavier, Y. Wang, S. Pierret, R. Moat,
- 704 B. Mori, ENGIN-X-instrument for materials science and engineering research, Neutron
- 705 News 24(3) (2013) 22-26.
- 706 [38] O. Kirichek, J. Timms, J. Kelleher, R. Down, C. Offer, S. Kabra, S. Zhang, Sample
- environment for neutron scattering measurements of internal stresses in engineering
- materials in the temperature range of 6 K to 300 K, Review of Scientific Instruments
- 709 88(2) (2017) 025103.
- 710 [39] G. Williamson, R. Smallman, III. Dislocation densities in some annealed and cold-
- 711 worked metals from measurements on the X-ray debye-scherrer spectrum,
- 712 Philosophical Magazine 1(1) (1956) 34-46.
- 713 [40] Y. Wang, S. Hossain, S. Kabra, S. Zhang, D. Smith, C. Truman, Effect of boundary
- 714 conditions on the evolution of lattice strains in a polycrystalline austenitic stainless
- 715 steel, Journal of Materials Science 52(13) (2017) 7929-7936.
- 716 [41] M. Daymond, M. Bourke, R. Von Dreele, B. Clausen, T. Lorentzen, Use of
- 717 Rietveld refinement for elastic macrostrain determination and for evaluation of plastic

- strain history from diffraction spectra, Journal of Applied Physics 82(4) (1997) 1554-
- 719 1562.
- 720 [42] G. Laplanche, P. Gadaud, O. Horst, F. Otto, G. Eggeler, E. George, Temperature
- dependencies of the elastic moduli and thermal expansion coefficient of an equiatomic,
- single-phase CoCrFeMnNi high-entropy alloy, Journal of Alloys and Compounds 623
- 723 (2015) 348-353.
- 724 [43] S. Kibey, J. Liu, D. Johnson, H. Sehitoglu, Predicting twinning stress in fcc metals:
- 725 Linking twin-energy pathways to twin nucleation, Acta materialia 55(20) (2007) 6843-
- 726 6851.
- 727 [44] J. Jeong, W. Woo, K. Oh, S. Kwon, Y. Koo, In situ neutron diffraction study of
- 728 the microstructure and tensile deformation behavior in Al-added high manganese
- 729 austenitic steels, Acta Materialia 60(5) (2012) 2290-2299.
- 730 [45] J. Jeong, Y. Koo, I. Jeong, S. Kim, S. Kwon, Micro-structural study of high-Mn
- 731 TWIP steels using diffraction profile analysis, Materials Science and Engineering: A
- 732 530 (2011) 128-134.
- 733 [46] J.t. Cohen, C. Wagner, Determination of twin fault probabilities from the
- diffraction patterns of fcc metals and alloys, Journal of Applied Physics 33(6) (1962)
- 735 2073-2077.
- 736 [47] R. Reed, R. Schramm, Relationship between stacking-fault energy and x-ray
- 737 measurements of stacking-fault probability and microstrain, Journal of Applied Physics
- 738 45(11) (1974) 4705-4711.
- 739 [48] S. Harjo, Y. Tomota, P. Lukáš, D. Neov, M. Vrana, P. Mikula, M. Ono, In situ
- 740 neutron diffraction study of α - γ Fe-Cr-Ni alloys under tensile deformation, Acta
- 741 materialia 49(13) (2001) 2471-2479.
- 742 [49] F. Tian, L.K. Varga, N. Chen, L. Delczeg, L. Vitos, Ab initio investigation of high-
- entropy alloys of 3 d elements, Physical Review B 87(7) (2013) 075144.
- 744 [50] A. Zaddach, C. Niu, C. Koch, D. Irving, Mechanical properties and stacking fault
- energies of NiFeCrCoMn high-entropy alloy, Jom 65(12) (2013) 1780-1789.
- 746 [51] J.P. Hirth, J. Lothe, Theory of dislocations, (1982).
- 747 [52] N.L. Okamoto, S. Fujimoto, Y. Kambara, M. Kawamura, Z.M. Chen, H.
- 748 Matsunoshita, K. Tanaka, H. Inui, E.P. George, Size effect, critical resolved shear
- stress, stacking fault energy, and solid solution strengthening in the CrMnFeCoNi high-
- entropy alloy, Scientific reports 6 (2016) 35863.
- 751 [53] B.C. De Cooman, Y. Estrin, S.K. Kim, Twinning-induced plasticity (TWIP) steels,
- 752 Acta Materialia 142 (2018) 283-362.
- 753 [54] J. Venables, Deformation twinning in face-centred cubic metals, Philosophical
- 754 magazine 6(63) (1961) 379-396.
- 755 [55] N. Naeita, J. Takamura, Deformation twinning in silver-and copper-alloy crystals,
- 756 Philosophical Magazine 29(5) (1974) 1001-1028.
- 757 [56] A. Haglund, M. Koehler, D. Catoor, E. George, V. Keppens, Polycrystalline elastic
- 758 moduli of a high-entropy alloy at cryogenic temperatures, Intermetallics 58 (2015) 62-
- 759 64.

- 760 [57] G. Dini, R. Ueji, A. Najafizadeh, S. Monir-Vaghefi, Flow stress analysis of TWIP
- 761 steel via the XRD measurement of dislocation density, Materials Science and
- 762 Engineering: A 527(10) (2010) 2759-2763.
- 763 [58] E. Nes, K. Marthinsen, Modeling the evolution in microstructure and properties
- 764 during plastic deformation of fcc-metals and alloys-an approach towards a unified
- model, Materials Science and Engineering: A 322(1) (2002) 176-193.
- 766 [59] W. Woo, E.-W. Huang, J.-W. Yeh, H. Choo, C. Lee, S.-Y. Tu, In-situ neutron
- 767 diffraction studies on high-temperature deformation behavior in a CoCrFeMnNi high
- 768 entropy alloy, Intermetallics 62 (2015) 1-6.
- 769 [60] D. Brown, M. Bourke, M. Stout, P. Dunn, R. Field, D. Thoma, Uniaxial tensile
- deformation of uranium 6 wt pct niobium: a neutron diffraction study of deformation
- twinning, Metallurgical and Materials Transactions A 32(9) (2001) 2219-2228.
- 772 [61] J.W. Christian, S. Mahajan, Deformation twinning, Progress in materials science
- 773 39(1-2) (1995) 1-157.

782

- 774 [62] Y.-F. Shen, Y. Wang, X.-P. Liu, X. Sun, R.L. Peng, S.-Y. Zhang, L. Zuo, P.K.
- Liaw, Deformation mechanisms of a 20Mn TWIP steel investigated by in situ neutron
- 776 diffraction and TEM, Acta Materialia 61(16) (2013) 6093-6106.
- 777 [63] D.R. Steinmetz, T. Jäpel, B. Wietbrock, P. Eisenlohr, I. Gutierrez-Urrutia, A.
- 778 Saeed–Akbari, T. Hickel, F. Roters, D. Raabe, Revealing the strain-hardening behavior
- 779 of twinning-induced plasticity steels: Theory, simulations, experiments, Acta
- 780 Materialia 61(2) (2013) 494-510.

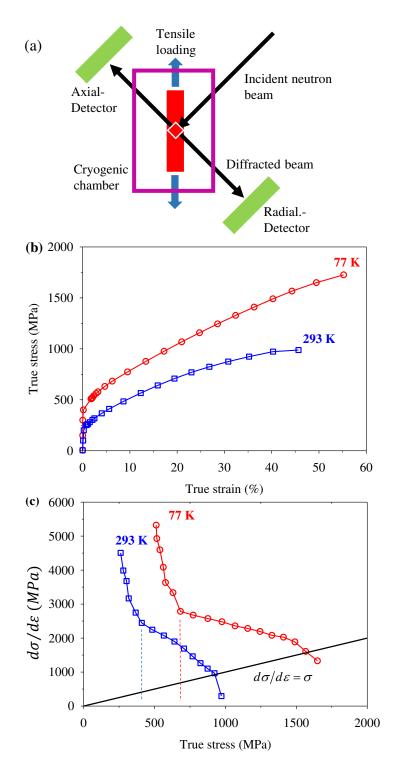


Fig. 1. (a) Schematic of the *in situ* neutron diffraction setup; (b) True stress-strain curves of uniaxial tensile tests at 77 K and 293 K and (c) the corresponding work hardening rate versus true stress.

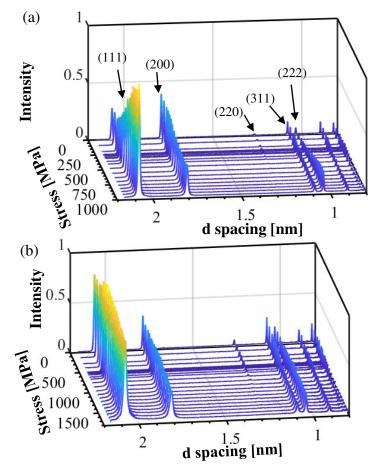


Fig. 2. Diffraction patterns collected at the axial detector as a function of stress at (a) 293 K; and (b) 77 K.

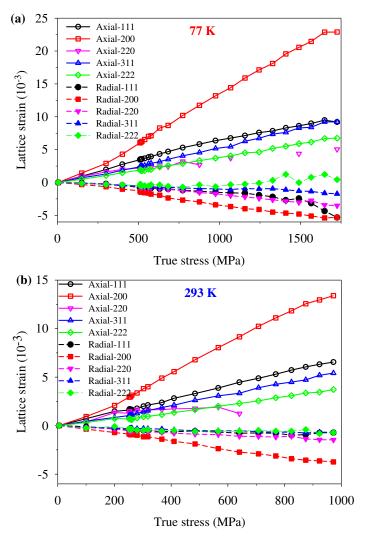


Fig. 3. The evolution of elastic lattice strains along the axial and radial directions in grain families having {111}, {200}, {220}, {311} and {222} crystallographic planes during tensile loading at (a) 77 K and (b) 293 K;

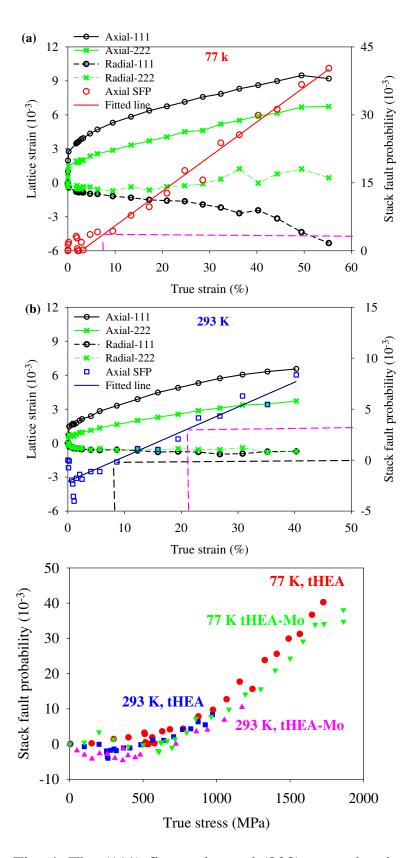


Fig. 4. The (111) first order and (222) second order reflections together with the stacking fault probability as a function of true strain at (a) 77 K and (b) 293 K; (c) stacking fault probability as a function of true stress (tHEA: FeCoCrNi; tHEA-Mo: FeCoCrNi $Mo_{0.23}$).

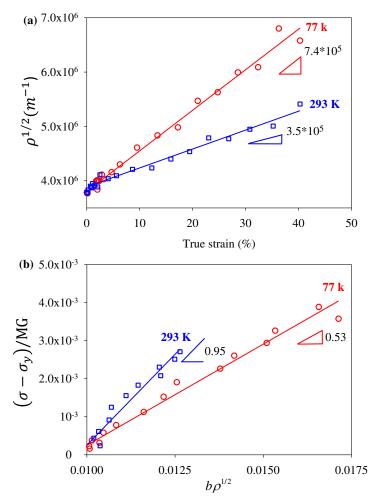


Fig. 5. The evolution of dislocation density versus (a) true strain, and (b) normalised work hardening $(\sigma - \sigma_y)/MG$ versus $b\rho^{1/2}$.

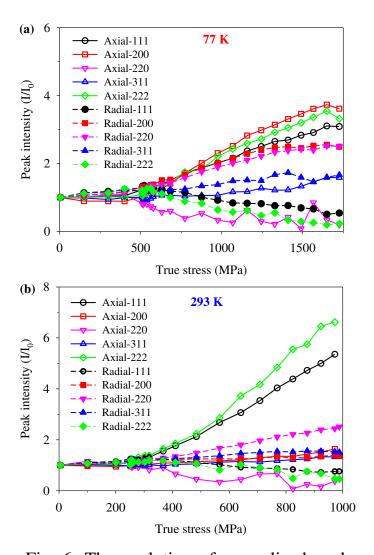


Fig. 6. The evolution of normalized peak intensity along the axial and radial directions in grain families having {111}, {200}, {220}, {311} and {222} crystallographic planes during tensile loading at (a) 77 K, and (b) 293 K.

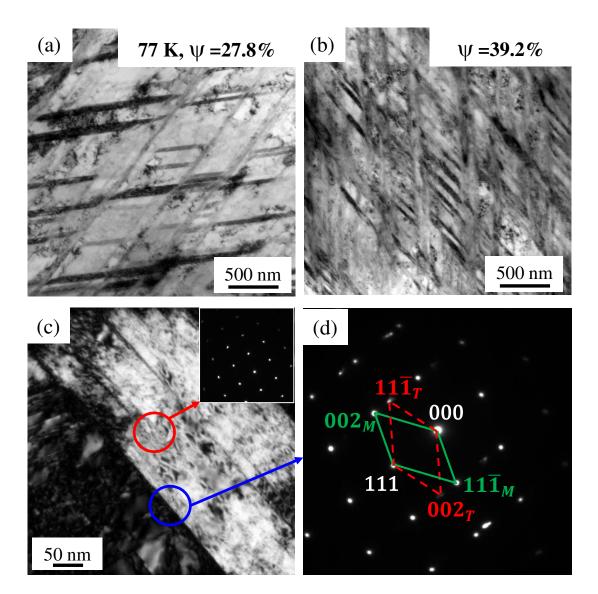


Fig. 7. TEM bright field micrographs of samples with (a) 27.8 % and (b) 39.2% strain at 77 K, which show nano-twins. (c) Higher magnification BF images with an inserted SAD pattern obtained from the matrix and (f) the composite SAD pattern obtained from the blue circled region in Fig. 7c which has contribution from both the matrix and the nano-twin.

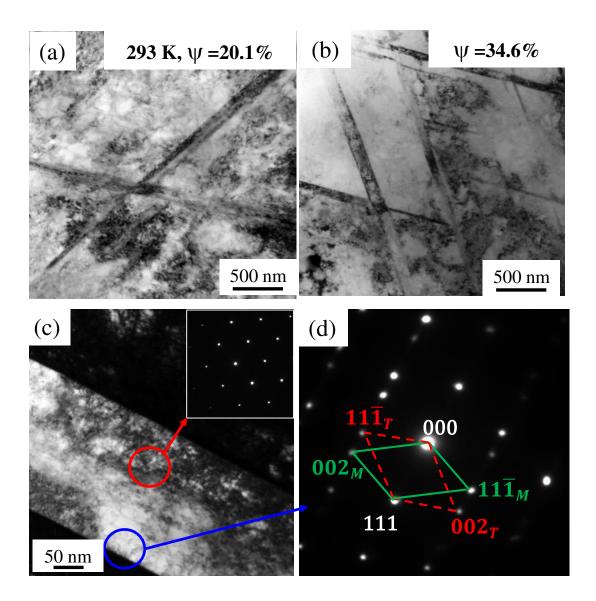


Fig. 8. TEM bright field micrographs of samples with (a) 20.1% and (b) 34.6% strain at 293k, which show nano-twins. (c) Higher magnification BF images with an inserted SAD pattern obtained from the matrix and (f) the composite SAD pattern obtained from the blue circled region in Fig. 8c which has contribution from both the matrix and the nano-twin.