

# Risk constrained short-term scheduling with dynamic line ratings for Increased Penetration of Wind power

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1 **Risk constrained short-term scheduling with dynamic line ratings for**  
2 **Increased Penetration of Wind Power**

3  
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16  
17 **Abstract**

18 Limited transmission capacity may lead to network congestion which results in wind  
19 curtailment during periods of high availability of wind. Conventional congestion  
20 management techniques usually involve generation management which may not always  
21 benefit large wind farms. This paper investigates the problem in detail and presents an  
22 improved methodology to quantify the latent scheduling capacity of a power system taking  
23 into account stochastic variation in line-thermal rating, intermittency of wind, and mitigating  
24 the risk of network congestion associated with high penetration of wind. The mathematical  
25 model converts conventional thermal constraints to dynamic constraints by using a  
26 discretized stochastic penalty function with quadratic approximation of constraint relaxation  
27 risk. The uniqueness of the approach is that it can limit the generation to be curtailed or re-  
28 dispatch by dynamically enhancing the network latent capacity as per the need. The approach  
29 is aimed at strategic planning of power systems in the context of power systems with short to  
30 medium length lines with a priori known unit commitment decisions and uses stochastic  
31 optimization with a two stage recourse action. Results suggest that a considerable level of

32 wind penetration is possible with dynamic line ratings, without adversely affecting the risk of  
33 network congestion.

34 Keywords – Wind Power, Network congestion, dynamic line rating, power system  
35 optimisation

## 36 **1. Introduction**

37 Network congestion is a major factor hindering the large scale integration of renewable  
38 energy generators into the grid. It is an undesirable result of insufficient capacity being  
39 available on a network to transport electricity from generation to loads which leads to  
40 volatility in locational marginal prices (LMP) and inequitable allocation of available network  
41 capacity to market participants. A number of publications have used the volatility in LMP as  
42 an indicator of network congestion [1-3]. In systems with large amount of wind power,  
43 network congestion hinders effective integration and utilization of wind as extra wind  
44 generated has to be curtailed thereby leading to uncertainty in revenue for wind power  
45 producers and overall higher costs for customers. The dynamic nature of wind results in large  
46 variations in power output over a short period of time, which makes effective utilization of  
47 wind an even bigger challenge in congested networks.

48 Currently, line ratings are based on worst case assumptions of ambient weather conditions  
49 according to the process outlined in IEEE Std 738-2012 [4]. The IEEE standard also covers  
50 transient and dynamic rating methodologies and a number of publications [5-9] have applied  
51 this methodology to demonstrate that the true thermal capacity of a transmission line is  
52 usually considerably higher than the rated values. This is to be expected since conventional  
53 ratings are calculated under the worst case weather assumption although such operating  
54 conditions occurs rarely in practice. It is possible to exploit this property by using dynamic  
55 line ratings (DLR) which model the thermal limit of transmission lines as a stochastically  
56 varying function of internal and external real time operating conditions such as ambient  
57 temperature, cooling due to wind, level of loading, and sag.

58 To partially account for variation in ambient conditions, some ISOs (independent system  
59 operators) currently use normal and emergency ratings as well as separate ratings for hot and  
60 cold weather. While these ratings consider some variation in ambient conditions they still  
61 assume the worst case scenario for a shorter period of time. These ratings are an  
62 approximation at best and the actual thermal limit has a high likelihood of being significantly  
63 different. In modern power systems which consist of multiple competing entities and fast

64 changing power flows due to presence of intermittent renewable generation, inaccurate  
65 estimation of real time ampacity can result in underutilization of network capacity and  
66 congestion. Any network investment requires strong economic justification and it may be  
67 viable to fully utilize existing network capacity prior to considering further investment in new  
68 assets. This is especially true for renewable generation which has to be competitive with  
69 conventional generation and cannot afford to add on the cost of increasing network capacity.  
70 Dynamic ratings can provide a significant increase in the normal and emergency operational  
71 flexibility of power transmission systems compared to the more traditional static rating and  
72 alleviate network congestion due to short periods of high wind power output. DLR is  
73 applicable for power systems with short to medium lines where thermal capacity as opposed  
74 to stability limit is the limiting factor to line capacity.

75 The benefit of DLR over conventional congestion management approaches is that it can  
76 potentially release latent capacity dynamically rather than relying on generation curtailment  
77 and demand reduction in congested parts of a network, thus improving the operational  
78 flexibility and deferring investments. Dynamic line ratings can exploit the advanced real time  
79 monitoring and control capabilities of smart grids to potentially alleviate network congestion,  
80 and ensure a more equitable allocation of costs between market participants.

81 The two immediate challenges of implementing the dynamic line rating methods presented in  
82 [5-8] are the need for an online, smart monitoring system to capture real time variation and  
83 the modelling of uncertainty in constraints in optimal scheduling. While uncertainty in  
84 optimization variables can be accounted for by stochastic optimization techniques,  
85 uncertainty in constraints is more challenging to model since analytical constrained  
86 optimization techniques only allow fixed constraints. Most of the power system applications  
87 of optimal scheduling problems model line power transfer limits as deterministic values and  
88 place less emphasis on dynamic variation in line capacity. Exceeding thermal limits for a  
89 short period of time results in an increased level of risk and it is important to account for this  
90 when modelling dynamic ratings. An alternative to this is chance constrained optimization  
91 which allows some flexibility in the constraint satisfaction by allowing constraint violation,  
92 provided their probability is limited to a specified value [10, 11].

93 This paper proposes a new mathematical framework and a methodology to incorporate  
94 benefits of real time variation in line ratings to temporarily relax constrained capacity of a  
95 network and to vary reinforcement thresholds. The technique allows the stochastically  
96 estimated real time ampacity to be included in scheduling decisions by allowing a degree of  
97 flexibility to satisfy dynamic thermal limit constraints. The uniqueness of the proposed

98 approach is that it replaces the current deterministic constraints (normal and emergency) in  
99 the optimal scheduling problem, with dynamic constraints. The approach dynamically  
100 quantifies the extent to which capacity could be relaxed by utilizing a discrete stochastic  
101 penalty function to model the risk associated with relaxing thermal limits. This method also  
102 incorporates the benefits of smart grid environments where real time data of system  
103 parameters such as sag and ambient temperature is available. The proposed approach could  
104 potentially provide considerable advantage over traditional approaches of using deterministic  
105 ratings due to the use of real time extraction of latent capacities during the optimization  
106 process. The proposed technique indicates the extent of congestion in a power network by  
107 weighting LMP at each node with respect to demand and finding the difference in the  
108 weighted LMP from the uncongested base case. The extended conic quadratic (ECQ)  
109 approach presented in [12] is used for optimization. It is modified to include dynamic line  
110 ratings.

111

## 112 **2. Dynamic Asset Rating**

### 113 **2.1 Stochastic Optimisation with Dynamic Asset Ratings**

114 The maximum thermal capacity of a line depends on the maximum allowable temperature of  
115 the line at which the conductors start to lose structural integrity or undergo annealing. IEEE  
116 Std 738 2012 outlines the process for calculating the maximum ampacity based on weather  
117 conditions for steady state, transient and dynamic scenarios. A number of models [5, 6, 8]  
118 apply the concepts in IEEE Std. 738 to determine dynamic line ratings which use weather  
119 data as an input. Kazerooni et al [7] have shown that when all the stochastic variations in  
120 weather are accounted for, the thermal capacity of the line can be modelled by the  
121 generalized extreme value probability distribution and in most cases the rated line capacity is  
122 on the lower end of the possible range of thermal capacities.

123 The correlation between wind speed and the cooling of the line was considered negligible in  
124 for this study, due the variation in weather conditions in different parts of a line [8]. While it  
125 is expected that weather conditions will mostly be favourable compared to the worst case  
126 assumptions for conventional line ratings, it is unlikely that all parts of the line will be  
127 exposed to high wind speeds which coincide with periods of high wind at the single location  
128 of the wind farm. It is assumed that the dynamic capacity is limited by regions where cooling  
129 due to wind is low and this provides a conservative estimate of the benefit due to DLR on

130 wind integration. Typical parameters for the probability distribution of line capacity are  
 131 provided in [7]. To determine the probability distribution of line ampacity historical weather  
 132 data across the line will be necessary as per the procedure outlined in [7]. If correlation  
 133 between wind speed and dynamic thermal ratings are to be accounted for, a different  
 134 approach is required where the probability distribution of line capacity is conditional based  
 135 on the probability of the wind speed distribution. A range of probability distributions for line  
 136 capacity would be necessary for different wind speeds. Such an approach should be used with  
 137 caution as it may overestimate the benefit of DLR.

138 The parameters of the probability distribution are determined according to the rated  
 139 maximum limit on transmission lines. Based on the analysis in [5] most utilities load their  
 140 lines such that the probability of exceeding the rated capacity ranges from 20 – 30%,  
 141 depending on the season. Thus it was assumed that the probability of exceeding the rated  
 142 capacity was 25% and an inverse distribution was used to determine the parameters for the  
 143 probability distribution. The probability distribution was discretised by considering ten  
 144 frequency and value pairs to represent the probability distribution. The actual probability can  
 145 vary depending on the utility but it is straightforward to perform the analysis with a different  
 146 value. A more detailed study might treat this as a random variable. The objective function  
 147 incorporating DLR as a penalty function with stochastic elements is shown in (1)

$$f(x) = C_g(P_g) + C_w(P_w) + C_{DLR} + C_{congestion} \quad (1)$$

148 where  $C_g(P_g)$ ,  $C_w(P_w)$ ,  $C_{DLR}$  and  $C_{congestion}$  represent cost of conventional generation, cost of  
 149 wind (including reserves), cost of dynamic ratings, and cost of congestion respectively.  
 150  $C_g(P_g)$  and associated constraints of conventional OPF (optimal power flow) problems are  
 151 given in [12-15].  $C_w(P_w)$  is the cost of uncertainty due to wind, which can be incorporated  
 152 into OPF by using stochastic optimization and is given in [12]. The problem is solved by  
 153 transforming to a conic quadratic optimization problem and using an interior point method  
 154 [12, 16]. This has the advantage that the objective function becomes quadratic and almost all  
 155 the constraints become linear. These transformations are not system dependent and hence can  
 156 be applied directly without a modification.

157

## 158 **2.2 Formulation**

159 The total cost of DLR ( $C_{DLR}$ ) in (1) is determined stochastically and represents the penalty for  
 160 temporarily relaxing the line thermal constraint. The stochastic penalty function enables  
 161 substitution of the static line thermal constraint with a dynamic constraint. The cost of DLR is

162 partly due to the long term cost of derating due to repeatedly overloading lines and the short  
 163 term risk of causing damage by severe overloading which causes line temperature to exceed  
 164 the maximum allowable value. It is assumed that when implementing DLR, the short term  
 165 risk and expected cost of thermal overload is considered much more significant than long  
 166 term derating costs. Separate studies by Wang [17] and Zhang [18] describe the variation of  
 167 thermal overload risk with line current and demonstrate that for low levels of current  
 168 overloading the risk of thermal overload is low but this increases rapidly for higher levels of  
 169 DLR. Thus, the sensitivity of the penalty function to dynamic overloading must increase with  
 170 increasing levels of DLR, thus suggesting an exponential penalty function. Instead it is  
 171 modelled using a quadratic function as given in (2) since it can approximate the exponential  
 172 function accurately for low levels of DLR, and the relative ease of calculating the Jacobian  
 173 and Hessian matrices for quadratic functions.

$$C_{DLR} = \sum_{p=1}^{N_L} \sum_{q=1}^{N_L} \left[ c_{OLp} \left( \sum_{k=1}^{N_k} h_{pq,k} a_{pq,k} \right)^2 \right] \quad (2)$$

174 where  $p-q$  represents a line from bus  $p$  to bus  $q$ . The cost of violating the constraint is  
 175 proportional to the magnitude by which the actual line flow exceeds the line capacity. The  
 176 constraints in (3) complement the expression for  $C_{DLR}$  in (2) to account for the cost of  
 177 uncertainty in stochastic line rating.

$$\begin{aligned} a_{pq,k} &\geq s_{\max,pq,k} - S_{sch,pq} \\ a_{pq,k} &\geq 0 \end{aligned} \quad (3)$$

178 The thermal capacity of line  $p-q$  is approximated by a discrete random variable where each  
 179 discrete value (represented by index  $k$ ) of  $s_{\max,pq,k}$  has corresponding probability  $h_{pq,k}$ . The  
 180 term  $a_{pq,k}$  (with per unit cost  $c_{OLp}$ ) represents the amount by which the actual line flow  
 181 exceeds the discrete line capacity in the  $k^{th}$  ordered pair and it corrects any violation in the  
 182 constraint  $S_{sch,pq} > s_{\max,pq,k}$ . Thus  $(h_{pq,k}, a_{pq,k})$  represents the probability distribution of dynamic  
 183 line rating and the average value of  $a_{pq,k}$  for all  $k$  represents the expected dynamic line rating.

184 The cost of DLR is based on the expected value of dynamic line rating which includes both  
 185 the amount of DLR ( $a_{pq}$ ) and the time for which it is implemented ( $h_{pq}$ ).  $h_{pq}$  is an array of  
 186 relative frequencies associated with each value of  $a_{pq}$ . If the time for which DLR is  
 187 implemented varies, the value of  $h_{pq,k}$  will change so that the probability distribution of  $a_{pq}$   
 188 changes. If the time for a specific amount of DLR is varied, it will change the probability  
 189 distribution (specifically a change in probability for that level of DLR) and hence the  
 190 expected value of DLR.

191 The DLR scheduling framework is to be used for a fixed scheduling period. This will

192 typically be in the order of 15 – 30 minutes as longer periods of DLR will result in substantial  
 193 risk of thermal overload. For the scheduling period under consideration, DLR is implemented  
 194 at all times or not at all and the risk of implementing DLR for that time is captured by the  
 195 cost function. In practice, smart monitoring systems will record the line temperature at the  
 196 start of the scheduling period and simulate the final line temperature at the end of the  
 197 scheduling period including the uncertainty based on the method in IEEE Std. 738. Based on  
 198 this, the probability of exceeding the maximum line temperature can be determined. The line  
 199 capacity probability distribution for the given scheduling period can be determined by the  
 200 generalized extreme value distribution and based on this capacity, current is scheduled to  
 201 minimize the time for which the line is overloaded. The severity associated with an outage in  
 202 the event that the risk of thermal overload is realized can be determined by the number of  
 203 customers affected by the outage and the total energy not supplied.

204 The risk associated with thermal overload includes both the likelihood of exceeding line  
 205 maximum temperature and the cost of an outage in the line under consideration. The value of  
 206  $c_{OLp}$  is chosen so that the quadratic function in (2) best fits the variation of risk of thermal  
 207 overload with current. Thus the risk of thermal overload is described by the expected cost of  
 208 outage in a particular line which is considered the cost/penalty of DLR. In the case studies, a  
 209 number of different values of  $c_{OLp}$  are used to determine the effect that the cost of DLR has  
 210 on the effectiveness of DLR.

211 The proposed approach assumes cost of congestion ( $C_{congestion}$ ) to increase linearly with the  
 212 extent of congestion in the system. The main contributor to  $C_{congestion}$  is the cost of  
 213 dispatching expensive reserve generation after lower cost generation has been curtailed. It is  
 214 assumed that these rapid response reserve generators have minimal startup cost and a much  
 215 smaller output range compared to large generators. They are distributed in the network and  
 216 the operating cost over the small range of output is approximated by linear cost functions.  
 217 Alternatively, load may have to be shed if redispatch cannot supply load. The penalty  
 218 associated with shedding load is also assumed to be linearly related to the load curtailed as  
 219 shown in (4).

$$C_{congestion} = \sum_{n=1}^N c_D P_{local,n} \quad (4)$$

s.t.

$$P_{local,n} \leq P_{D,n}, P_{local,n} \geq 0,$$

220 where  $P_{local,n}$  represents any adjustment of load (by calling on local reserves or load shedding)  
 221 at bus  $n$  (where the total number of buses is  $N$ ).  $P_{local,n}$  is required to balance the system when



222 congestion has occurred but it has a high cost per unit ( $c_D$ ). Cost of network congestion can  
 223 also represent the loss of revenue for generators since they cannot sell energy. This increased  
 224 cost required to balance the system under congestion is allocated unevenly among customers  
 225 which results in the volatility in nodal pricing that is observed during congestion.

226 For low levels of DLR, cost of congestion is higher relative to the risk of thermal overload  
 227 from dynamically overloading lines. The optimization algorithm prefers to use DLR than call  
 228 on expensive reserves after redispatch due to the lower cost of DLR. However, there is a  
 229 maximum amount of DLR indicated by the intersection of the two functions in (2) and (4)  
 230 beyond which, risk of DLR is greater than cost of congestion. Beyond the threshold point  
 231  $C_{DLR}$  is greater than  $C_{congestion}$  thus forcing the optimization to not allow DLR beyond this  
 232 limit as the risk associated with further overloading would not be justifiable. The DLR limit  
 233 point represents both the maximum extent to which thermal limits can be relaxed and the  
 234 time for which it can be relaxed

235 In addition to  $C_{DLR}$  and  $C_{congestion}$  the basic OPF formulation includes generator fuel cost  
 236 ( $C_g(P_g)$ ) and constraints including real and reactive power balance, voltage limits, generator  
 237 limits, and minimum generator up and down time. Line thermal constraints are replaced by  
 238 the dynamic line rating formulation. The proposed approach modelled wind power  
 239 intermittency cost ( $C_w(P_w)$ ) using stochastic optimization by discretizing the probability  
 240 distribution of wind power and balancing probabilistic reserve cost with cost of wasted wind  
 241 [12] as shown in (5).

$$C_w(P_w) = \sum_{j=1}^{N_w} \left[ e_j P_{Wj} + c_{Wj} \sum_{k=1}^M f_{jk} s_{jk} + c_{Rj} \sum_{k=1}^M f_{jk} t_{jk} \right] \quad (5)$$

242 Where the power output of wind generator  $j$  is  $P_{Wj}$  and the unit feed in cost is  $e_j$ . The cost of  
 243 wind in (5) is subject to the constraints in (6).

$$\begin{aligned} t_{jk} &\geq P_{Wj} - w_{jk} \\ s_{jk} &\geq w_{jk} - P_{Wj} \\ t_{jk} &\geq 0, s_{jk} \geq 0 \end{aligned} \quad (6)$$

244 where  $(f_{jk}, w_{jk})$  is the  $k^{\text{th}}$  ordered pair (out of a total of  $M$ ) representing the discretized  
 245 probability distribution of wind generator  $j$ .  $N_w$  is the number of wind generators in the  
 246 system and  $c_{Wj}$  and  $c_{Rj}$  are the unit cost of wasted wind and reserve generation respectively at  
 247 wind generator  $j$ . The cost of wasted wind represents the opportunity cost of not being able to  
 248 sell the energy generated.

249 The problem was solved by transforming it to an extended conic quadratic (ECQ) form  
 250 using the transformations in (7) [12, 16].

$$\begin{aligned}
R_{in} &= V_i V_n \cos(\delta_i - \delta_n) \\
T_{in} &= V_i V_n \sin(\delta_i - \delta_n) \\
u_i &= \frac{V_i^2}{\sqrt{2}}
\end{aligned} \tag{7}$$

251 Adding the rotated conic quadratic and arctangent equality constraints in (8) captured the  
252 nonlinearity of the classical OPF problem [12, 16].

$$\begin{aligned}
2u_i u_n &= R_{in}^2 + T_{in}^2 \\
\delta_i - \delta_n &= \tan^{-1} \left( \frac{T_{in}}{R_{in}} \right)
\end{aligned} \tag{8}$$

253 All other constraints are transformed into linear expressions making the ECQ-OPF problem  
254 easily tractable by primal-dual interior point methods.

255

256

### 257 **2.3 Metrics for indicating the level of congestion**

258 The severity of congestion is quantified by the volatility in LMP and the amount of wind  
259 curtailment. Volatility in LMP is most commonly used as an indicator of network congestion  
260 as congestion cost is a significant component of LMP in transmission systems [2, 3, 19].

261 Pricing signals have been proposed as a control mechanism for renewable energy integration  
262 [20]. The proposed method first establishes a base case for LMP without incorporating  
263 network constraints. For each outage scenario, the LMP at each bus is compared to the base  
264 case LMP, weighted by the load at that bus and the overall weighted variation in LMP is  
265 found. To compare the LMP profile of a specific case to the base case, the term  $LMP_V$  is  
266 defined by (9).

$$LMP_V = \sqrt{\frac{1}{\sum_{i=1} P_{D,i}} \left( \sum_{i=1} P_{D,i} \left( \frac{LMP_i - LMP_{i,base}}{LMP_{i,base}} \right)^2 \right)} \tag{9}$$

267  $LMP_V$  is the LMP normalized by base LMP. A large value of  $LMP_V$  generally indicates that  
268 the given LMP profile is very different to the uncongested LMP profile which most likely  
269 suggests that the network is congested.

270 The other important indicator of network congestion in the context of the problem of wind  
271 curtailment is the level of curtailment compared to the uncongested base case. Wind  
272 curtailment is normalized with respect to the wind generation in the uncongested base case  
273 and determined by (10).

$$\text{wind curtailed} = \frac{P_{w,base} - P_w}{P_{w,base}} \quad (10)$$

274 The wind curtailed percentage is defined as difference between the wind scheduled in the  
 275 base case and the case under consideration, normalized with respect to wind scheduled in the  
 276 base case. The level of wind curtailment independently cannot indicate the level of  
 277 congestion as wind may be curtailed due to multiple reasons such as low demand. Similarly,  
 278 if the wind curtailment is low then the network congestion may not necessarily be low. Thus,  
 279 if both the variation in LMP and wind curtailment indicates that there is network congestion  
 280 then there is a high probability that congestion induced wind curtailment occurs. If  $LMP_V$  is  
 281 high but wind curtailment is low, then it indicates that there is network congestion but it may  
 282 not necessarily be leading to curtailment of wind power. Alternatively, congestion may have  
 283 affected individual wind farms but the total wind curtailed may not have changed.

284 A third indicator of network congestion, in addition to the LMP volatility and wind curtailed,  
 285 is the spare capacity in the network. It is measured as the total available capacity expressed  
 286 relative to the total rated capacity of all lines and is determined by equation (11).

$$\text{spare capacity} = \frac{\sum_{all\ lines} (I_{max} - I_{flow})}{\sum_{all\ lines} I_{max}} \quad (11)$$

287 Where  $I_{max}$  is the magnitude of maximum current in a line and  $I_{flow}$  is the magnitude of  
 288 current actually flowing in the line.  $I_{max}$  is the deterministic thermal limit of the line and when  
 289 DLR is implemented the spare capacity may be negative. This is because  $I_{flow}$  will exceed the  
 290 deterministic  $I_{max}$ . In the case studies, additional spare capacity required to relieve network  
 291 congestion with deterministic ratings is used to determine the capacity released by DLR.

292 The metrics presented in this section are not exhaustive. Considering all three metrics would  
 293 indicate the likelihood that congestion is occurring and that a detailed investigation of nodal  
 294 pricing distribution and wind generation profile should be undertaken. Table 1 shows how to  
 295 interpret the metrics for cases when no DLR has been implemented.

296

297

298

299

300

Table 1 Matrix for network congestion and wind curtailment

	Spare capacity high		Spare capacity low	
	$LMP_V$ high	$LMP_V$ low	$LMP_V$ high	$LMP_V$ low
Wind curtailed high	May be localised congestion	Wind curtailment but not due to network congestion	High likelihood of network congestion and wind curtailment	Wind curtailment but not due to network congestion. Outage may result in congestion
Wind curtailed low	localised congestion not leading to wind curtailment	Low likelihood of congestion	There is congestion, but it is not leading to wind curtailment.	Network is not significantly congested but an outage may result in congestion.

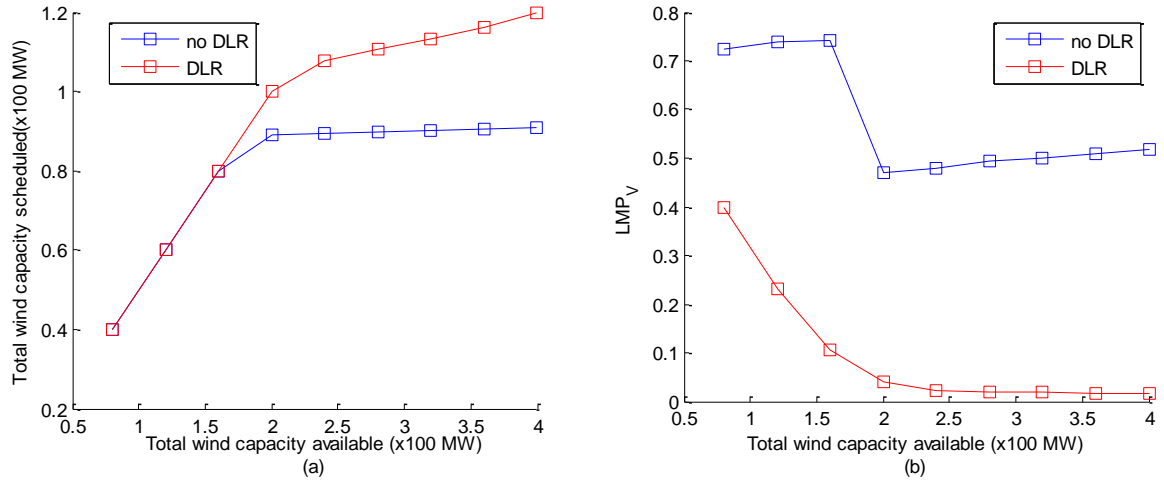
301

302 If DLR is implemented, the spare capacity will be negative in lines with DLR as the flow will  
 303 exceed the deterministic thermal limit. The overall spare capacity may not be negative if the  
 304 congestion is localised and DLR is only implemented in a few lines in the network. The other  
 305 indicators can be used in the same way as shown in Table 1.

306 **3. Results and discussion**

307 **3.1 Effect of wind penetration level**

308 Figure 1 shows the effect of varying the total available wind capacity on the scheduled wind  
 309 and the  $LMP_V$  for DLR and non DLR cases in the IEEE 14 bus test system.



310

311 Figure 1 Effect of varying wind penetration level on (a) wind scheduled and (b)  $LMP_V$   
 312 for IEEE 14 bus test system

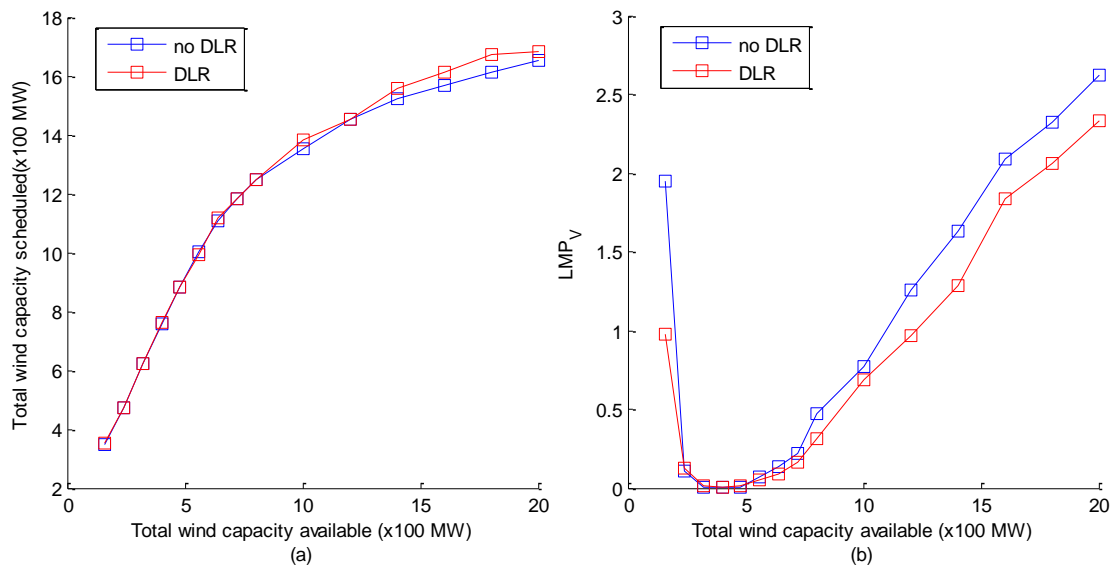
313 In Figure 1 the wind scheduled with and without DLR appears to increase linearly until  
 314 approximately 150 MW of wind is available. The wind scheduled is identical between DLR  
 315 and non DLR cases. If the total wind available is increased above 150 MW, the DLR case  
 316 shows a higher amount of wind scheduled than the non DLR case. Furthermore, above 200  
 317 MW of available wind, no additional wind is scheduled as available wind is increased for the  
 318 non DLR case. However, if DLR is implemented, the amount of wind scheduled continues to  
 319 increase as the available wind capacity is increased. Thus, without DLR the amount of wind  
 320 in the system reaches saturation much earlier than with DLR.

321 Figure 1 shows the variation in  $LMP_V$  with varying wind penetration. When no DLR is  
 322 implemented the level of congestion appears quite insensitive to the total available wind  
 323 capacity until it is increased to 150 MW. Beyond this value there is a drop in the level of  
 324  $LMP_V$  indicating a reduction in congestion between a total available wind capacity of 150  
 325 MW to 200 MW. Above 200 MW the variation in  $LMP_V$  appears to be minimal with a  
 326 slightly increasing trend. Since additional wind in the system is not scheduled as per Figure 1,  
 327 the associated cost of wind curtailment may cause slight increase in the  $LMP_V$ . However, this  
 328 increase is small since the cost of wind curtailment is typically considered to be negligible  
 329 considered to cost of unsupplied load and cost of scheduling emergency generation.

330 When DLR is implemented the  $LMP_V$  decreases with increasing levels of wind availability  
 331 and reaches a minimum value at 250 MW of wind availability. This is possibly due to the  
 332 extra latent capacity released by DLR which can accommodate the increased wind

333 availability. Since the cost of wind and ancillary services is lower than the cost of supplying  
 334 demand during congestion, this leads to a reduction in the  $LMP_V$ . As evident from 0, not all  
 335 the available wind is scheduled when DLR is used, however, a fixed percentage of available  
 336 wind is scheduled.

337 Figure 2 shows the effect of varying wind penetration level for the IEEE 118 bus system. In  
 338 contrast to the 14 bus system, the trend for the wind scheduled versus wind available is nearly  
 339 identical for DLR and non DLR cases. This indicates that DLR does not lead to any increase  
 340 in the wind scheduled.



341

342 Figure 2 Effect of varying wind penetration level on (a) wind scheduled and (b)  $LMP_V$   
 343 for IEEE 118 bus test system

344 An examination of the variation in  $LMP_V$  shows that DLR causes a reduction in the level of  
 345  $LMP_V$  for almost all levels of available wind. In a large system with multiple generators it  
 346 may not necessarily be economical to allocate latent capacity released by DLR to wind  
 347 generation. The overall effect on the system due to DLR is not as high as for the 14 bus  
 348 system. However, DLR may still be effective to relieve localised congestion if a smaller part  
 349 of the network was considered as seen in the 14 bus system.

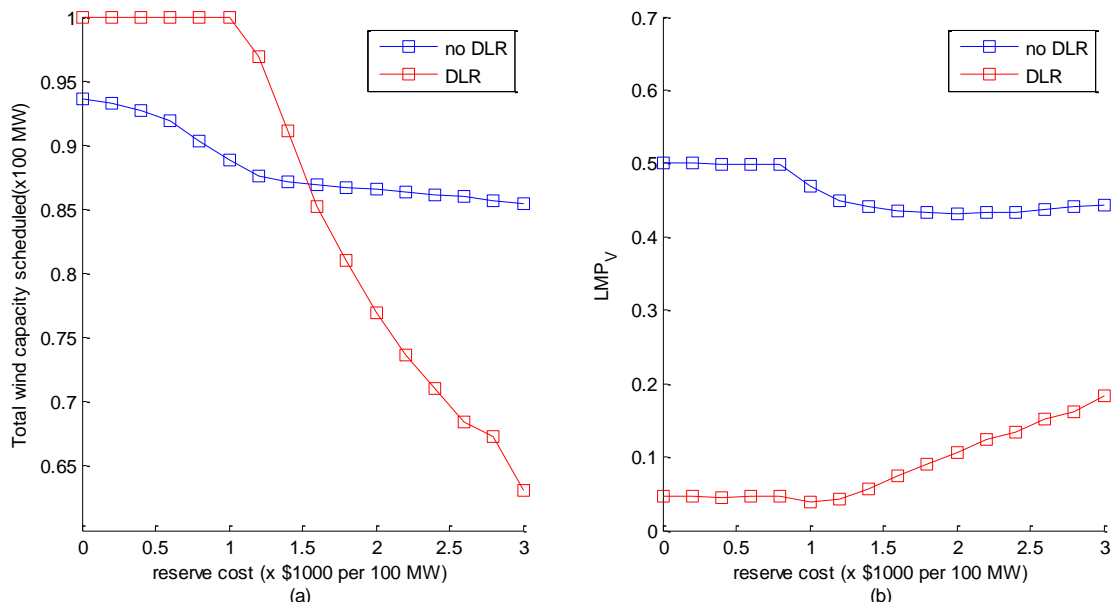
350 According to Figure 2(b) the  $LMP_V$  reaches a minimum value at an available wind capacity of  
 351 500 MW with and without DLR. This indicates there is an optimum penetration level of wind  
 352 at which network congestion will be minimised. This point nearly coincides with the point in  
 353 Figure 2(a) where the sensitivity of wind scheduled to available wind decreases significantly.

354 Initially wind penetration is limited by network capacity but as penetration of wind increases,  
355 cost of reserves starts to limit the amount of wind that can be scheduled. This eventually  
356 leads to a maximum level of wind penetration and any wind added above this level is  
357 unutilised. This maximum penetration was 150 MW in the 14 bus system and 500 MW in  
358 118 bus system. If cost of reserves did not limit the wind scheduled, the curve in Figure 2(a)  
359 may have shown a linear increase. Due to the high cost of reserves relative to conventional  
360 generation, the cost of reserves is the limiting factor for the maximum penetration of wind  
361 rather than available network capacity. Thus the reserve cost is expected to have an impact on  
362 how much latent capacity is released and how this is allocated to various generation sources.

### 363 **3.2 Effect of varying reserve cost on wind scheduling**

364 Reserves are necessary to manage the intermittency of wind. These reserves may be storage  
365 or additional generation maintained on site at the wind farm to enable the wind power  
366 producer to regulate their output to the grid. In this case the cost of the reserves is borne by  
367 the wind power producer and they can make decisions on how much wind to commit to the  
368 system. Alternatively, the system operator may choose to maintain reserves in the grid if  
369 there is a large penetration of renewables. These may be in the form of thermal generators'  
370 inherent capability to adjust output over a range, grid connected storage, or smaller high  
371 speed generators. Impact of cost of reserves on the effect of DLR for the IEEE 14 bus system  
372 is shown in Figure 3. Reserve cost is expressed in \$1000 per 100 MW of reserves.

373



374

375 Figure 3 Effect of varying reserve cost on (a) wind scheduled (b)  $LMP_V$  for IEEE 14  
376 bus test system.

377 According to Figure 3(a) there are three distinct regions in the curve. For reserve cost less  
378 than 1, wind scheduled due to DLR is constant. Between reserve cost 1 to 1.5, the wind  
379 scheduled with DLR decreases sharply and becomes less than the wind scheduled without  
380 DLR. Above reserve cost of 1.5, the wind scheduled without DLR decreases at a much  
381 slower rate than wind scheduled with DLR.

382 In region 1, the  $LMP_V$  in Figure 3(b) does not vary with reserve cost for reserve cost up to 1.  
383 However, the  $LMP_V$  is lower with DLR than without since any latent capacity is allocated to  
384 low cost wind generation. As the wind scheduled does not change significantly with reserve  
385 cost in this region, there is no change in  $LMP_V$ .

386 In region 2, the DLR cost is higher, and it starts to become uneconomical to allocate latent  
387 capacity to wind. As a result, the wind scheduled with DLR decreases sharply. Since cost of  
388 wind has increased, this leads to an overall increase in generation cost which results in the  
389 increase in  $LMP_V$  in Figure 3(b). In the case without DLR, wind scheduled does not decrease  
390 as sharply as the DLR case, since the lack of transmission capacity may not allow this. The  
391 reduced wind may allow more economical forms of generation which leads to a slight  
392 decrease in  $LMP_V$ . However, this  $LMP_V$  is still higher than the  $LMP_V$  with DLR.

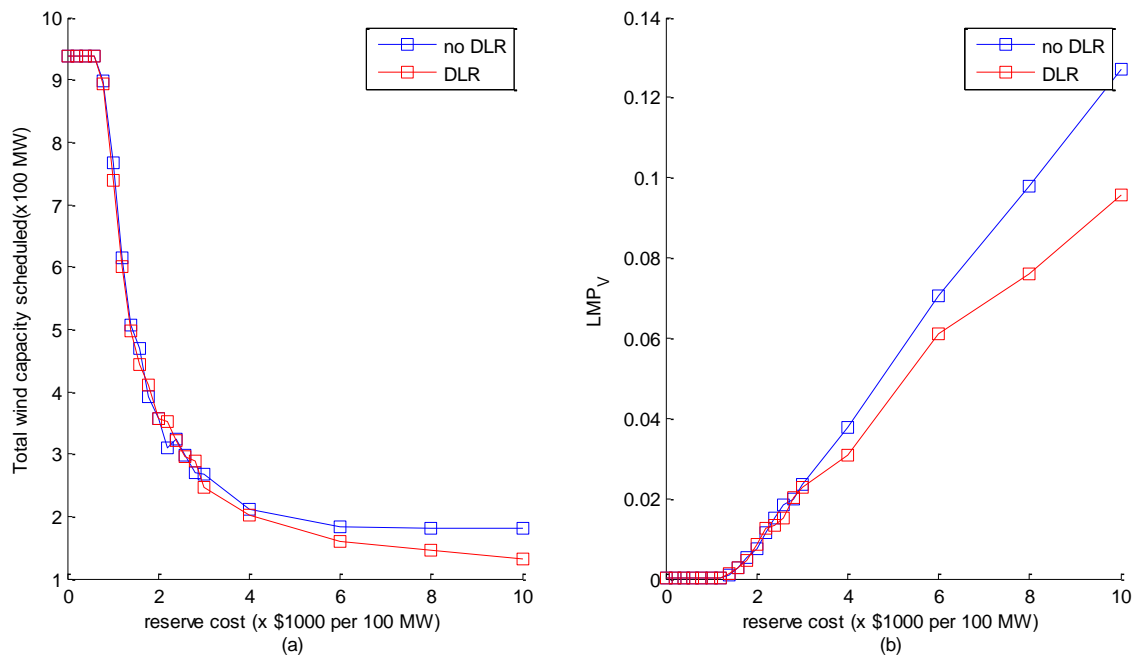
393 In region 3, less wind is scheduled with DLR than without indicating it is uneconomical to  
394 allocate latent capacity released by DLR to wind. The overall cost of generation continues to



395 increase leading to the increase in  $LMP_V$  in Figure 3(b). In the no DLR case, the trend from  
 396 region 2 continues for the wind scheduled. The  $LMP_V$  appears to reach a constant value due  
 397 to any decrease in wind scheduled being compensated by conventional generation which has  
 398 a similar cost.

399 Generally, increasing reserve costs adds to the overall cost of wind generation since reserves  
 400 are required to manage intermittency, thus leading to less utilization of wind. When the  
 401 reserve cost is comparable to cost of conventional generation, more wind is scheduled since it  
 402 is more economical than conventional generation. Lack of transmission capacity does not  
 403 limit the wind generation in this case since conventional generation is reduced accordingly.

404 The variation of wind scheduled and  $LMP_V$  with reserve cost for the IEEE 118 bus test  
 405 system is shown in Figure 4



406

407 Figure 4 Effect of varying reserve cost on (a) wind scheduled (b)  $LMP_V$  for IEEE 118  
 408 bus test system

409 In Figure 4(a) the trends are less prominent. The wind scheduled is similar between DLR and  
 410 no DLR cases for low reserve cost. As reserve cost increases, the total wind scheduled with  
 411 DLR is lower than total wind schedule without DLR. Similar to the 14 bus system, the  
 412 capacity released by DLR is not allocated to wind if the cost of reserves is too high. In Figure  
 413 4(b) the  $LMP_V$  with and without DLR are similar for reserve costs below 3.5. However, at  
 414 higher reserve costs  $LMP_V$  is lower with DLR. The steady increase in  $LMP_V$  is due to the

415 overall increasing cost of generation when reserve costs are increased. However, any latent  
416 capacity released is allocated to less expensive generation sources thus ensuring that  $LMP_V$  is  
417 lower when DLR is used.

418 The weather patterns will determine the amount of wind available and the available network  
419 capacity will determine the extent of wind utilisation. While the analysis in this section refers  
420 to congestion under normal operating conditions (without outages), there is always a risk of  
421 further congestion if a system contingency occurs. When DLR is not used, the risk of  
422 network congestion for a given penetration level of wind would be significantly higher and  
423 the risk is reduced by using dynamic line ratings.

424 For systems without contingencies, the effect of DLR may not be evident in large systems.  
425 However, localised congestion may be relieved when DLR is implemented. While DLR  
426 usually releases some amount of latent capacity, this is allocated to the most efficient forms  
427 of generation which may or may not be wind. Thus while DLR can reduce congestion, it may  
428 not necessarily increase wind integration.

429 Dynamic Line rating methodologies present a viable temporary alternative to network  
430 reinforcement and expansion to alleviate localised congestion. Smart grid infrastructure for  
431 monitoring ambient conditions as well as asset conditions need to be in place to implement  
432 dynamic line ratings. Protection devices will have to adapt to levels of current flow which  
433 would exceed conventional ratings. Distance relays monitor voltage in addition to current so  
434 it is likely to operate under DLR events compared to current relays. Alternatively, smart  
435 protection devices may be used which could operate on the basis of line temperature or line  
436 sag exceeding a specified limit rather than line current.

#### 437 **4. Conclusion**

438 The paper proposed a new mathematical framework to assess the potential ability of DLR to  
439 reduce the level of network congestion and limit the curtailment levels of wind power in  
440 power systems. The model converts conventional thermal constraints to dynamic constraints  
441 by using a discretized stochastic penalty function with quadratic approximation of constraint  
442 relaxation risk. The novelty of this method is that it allows real time variation of dynamic line  
443 rating to be modelled stochastically and incorporated into planning and scheduling decisions  
444 while controlling the extent of DLR by varying the cost parameters. This method is ideal for

445 application in a smart grid environment where real time data about the network status is  
446 readily available.

447 Case studies suggest that DLR can potentially release a considerable amount of capacity of  
448 network assets in systems under congestion, enabling increased wind power integration. DLR  
449 is especially effective in reducing localised congestion and may be considered as an  
450 alternative for deferring or completely avoiding network expansion in congested areas. While  
451 DLR releases latent network capacity it does not directly influence the allocation of the latent  
452 capacity released among generators. The effect of DLR on increasing wind integration  
453 depends on factors such as reserve cost and the level of available wind relative to  
454 conventional generation.

455 Power systems need periodic investment planning to meet growth in demand, uncertainties,  
456 and risks associated with active operation. In that context, the proposed approach can be used  
457 to monitor the net network reinforcement requirement in power systems by utilizing the  
458 benefits that can be offered by DLR of assets under normal operation and credible  
459 contingencies.

460

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