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## Article

# Remaining Fatigue Life Predictions of Railway Prestressed Concrete Sleepers Considering Time-Dependent Surface Abrasion

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**Abstract:** One of the safety-critical components of ballasted track systems is railway sleepers whose main functions are to (i) transfer vertical load, (ii) maintain rail gauge, and (iii) restrain longitudinal rail movement. Railway sleepers can be manufactured using timber, concrete, steel, composite, and any other engineered materials. Prestressed concrete sleepers are the most commonly used type worldwide because of their superior value-for-money performance. In practice, railway sleepers experience thousands of cycles of aggressive wheel–rail dynamic loads and wear deterioration can be observed over their service life. Not only does the deterioration affect track quality and geometries, but it also undermines the structural integrity of the track structures. The wear and abrasion directly decrease the capacity of railway sleepers, resulting in the reduction in service life. In this paper, the emphasis is placed on the assessment of the fatigue life of prestressed concrete railway sleepers with imperfect geometry. This study is the world’s first to establish a new fatigue simulation of railway concrete sleepers considering accumulative non-constant amplitudes, which has been validated using full-scale experimental results and empirical analyses. Parametric studies have been conducted to obtain new insights into the fatigue performance of the worn sleepers. The new findings will improve railway sleeper maintenance and inspection criteria, and will provide a new guideline on track-condition monitoring networks.

**Keywords:** railway concrete sleepers; fatigue; S–N curve; finite element method (FEM); geometric damage; abrasion; remaining service life



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## 1. Introduction

At present, railway transport is one of the most sustainable and commonly used forms of transport for passengers and goods [1]. Conventional ballasted track systems can be divided into superstructures and substructures. The superstructure includes the rails, fastening systems, railway sleepers, rail pads, and ballast. The substructure consists of the sub-ballast, formation, subgrade, and structural fills. A railway sleeper is a safety-critical component, which transfers the force from the wheels to the substructure [2–4]. Prestressed concrete sleepers are the most widely used type of sleeper materials because of their good structural performance, low cost, and ease of maintenance [5]. However, repeated loads from wheel–rail interactions could result in accumulated damage on railway sleepers, which reduces the service life. Both the static and dynamic load-carrying capacities of railway sleepers can degrade over time. In addition, early deterioration could lead to premature failure of railway sleepers. Such problems are a form of serviceability limit states, which have become of great concern over the past few decades for railway engineers.

The most common causes of concrete sleeper failures have been ranked using the results obtained from a worldwide survey shown in Table 1 [6,7], where it can be seen that deterioration, abrasion, fatigue, and cracking are the most critical problems for railway sleepers. Such problems can lead to a combined reaction that accelerates the failure of railway sleepers. In limit-states design practice, the fatigue limit state shall be considered.

**Table 1.** Most common causes of concrete sleeper failures [6].

Main Causes	Problems	Worldwide Response <sup>1</sup>
Lateral load	• Abrasion on rail-seat	3.15
	• Shoulder/fastening system wear or fatigue	5.5
Vertical dynamic load	• Cracking from dynamic loads	5.21
	• Derailment damage	4.57
	• Cracking from center binding	5.36
Manufacturing and maintenance defects	• Tamping damage	6.14
	• Others (e.g., manufactured defects)	4.09
Environmental considerations	• Cracking from environmental or chemical degradation	4.67

<sup>1</sup> Ranked from 1 to 8, with 8 being the most critical.

In order to investigate the serviceability performance of prestressed concrete sleepers, the dynamic condition needs to be investigated. In reality, a dynamic load is usually related to the rail–wheel interaction and train speed [8]. Railway sleepers often experience impact loading due to wheel–rail interactions associated with abnormalities in either a wheel or a rail [9]. The high dynamic impact forces induced by wheel–rail irregularities could greatly exceed the static wheel load, which could cause deterioration. The most common forms of wear are rail-seat or soffit abrasion at mid-span [10]. These deterioration mechanisms can be observed in the field. Extensive experimental and analytical investigations have been conducted by Kaewunruen and Remennikov on the dynamic behavior of prestressed concrete sleepers [11–13]. In their research, the impact damage and failure patterns of prestressed concrete sleepers were studied, which provided a database for life cycle investigation. Chen et al. presented an experimentally validated three-dimensional finite element model of a prestressed concrete sleeper that can be used to study and improve the design and performance [14]. Bastos et al. investigated the deterioration of prestressed concrete sleepers under cyclic loads and exposed to moisture [15]. Parvez et al. investigated the efficiency of using steel fibers to improve the fatigue performance of prestressed concrete sleepers [16]. Riding et al. conducted a study of environmental and track factors that influenced the abrasion damage of prestressed concrete sleepers [17]. Kernes et al. investigated the mechanics of rail-seat deterioration and methods to improve the abrasion resistance of concrete sleepers at rail seats [18]. It is noted that, for high-quality concrete sleepers, most studies did not observe any bond slip in the prestress wires under static and high-cycle fatigue tests. This is due to the fact that, in various modern design standards (such as in Europe, Australia, Japan, and China), there is a restriction in the allowable dimension of the prestress wires which helps it to increase the total bond perimeters and restrict any

slip. In recent studies, Ngamkhanong et al. studied the effect of surface abrasion on the impact capacity of prestressed concrete sleepers [19,20]. Meanwhile, You et al. developed a nonlinear finite element model for determining the structural capacity of a prestressed concrete sleeper with rail-seat abrasion [21]. Further, Li et al. investigated creep and shrinkage of prestressed concrete sleepers influenced by surface abrasion [22]. Despite a number of previous studies into concrete sleepers and fatigue life, most studies focus on a general understanding in order to establish an empirical fatigue-life estimation that is relatively specific to the cases. On this ground, many factors related to time-dependent variables (such as wear, creep, and shrinkage, and so on) cannot be properly identified. This study has thus embarked on the development of nonlinear models of concrete sleepers capable of fatigue failure analyses and for virtual tests of the time-dependent factors.

Numerous numerical and experimental investigations have been initially conducted to establish rational railway-sleeper models by the authors [23]. Our studies into the fatigue life of concrete sleepers originated with the damage accumulation method [24,25]. This tailored method is extended from Miner's rule. Traditionally, the cumulative damage under various loads is regarded as equivalent fatigue stress with constant amplitude [26]. Our study is unique in the way that the fatigue rule has been modified to enable iterative and variable stress fields (or non-constant amplitude), which can be more realistic and suitable for track load spectra. The critical literature review reveals that the fatigue life-cycles of prestressed concrete sleepers have not been fully studied, especially when the sleepers are deteriorated by excessive wear [27,28]. This paper is thus the world's first to investigate and present an advanced railway concrete-sleeper model capable of parametric analysis into the effect of surface abrasion on the fatigue life of prestressed concrete sleepers. This model is highly original since it can cope with the accumulative, non-constant amplitudes of fatigue loads. The emphasis of this paper is placed on the fatigue life of prestressed concrete sleepers when subjected to wear or abrasion in comparison with intact railway sleepers. The new findings and insights will help track engineers to have a better understanding of the remaining fatigue life of damaged sleepers and provide a guideline to identify appropriate damage-detection technology for track systems. The new insight into fatigue life will also improve the safety and reliability of railway infrastructure.

## 2. Theoretical Life-Cycle Assessment Method of Prestressed Concrete Sleepers

### 2.1. Damage Accumulation Method

You et al. [29,30] demonstrated a new approach based on the damage accumulation method to analyze the life-cycle of prestressed concrete sleepers. The cumulative damage index is calculated by Miner's rule:

$$\sum_i D_i = \sum_i \frac{n(\Delta\sigma_i)}{N(\Delta\sigma_i)} \quad (1)$$

where  $n(\Delta\sigma_i)$  is the applied number of cycles at a stress range  $\Delta\sigma_i$ ;  $N(\Delta\sigma_i)$  is the resisting number of cycles at a stress range  $\Delta\sigma_i$ .

The fatigue life can be determined by:

$$L_f = \frac{1}{D_i} \quad (2)$$

### 2.2. Material Properties of Fatigue

The S–N curve can be defined as the number of cycles to failure when a material is repeatedly loaded through an alternating stress range. Therefore, the fatigue life of prestressed concrete sleepers can be determined as the maximum applied number of cycles to failure. [24,31]. The typical S–N curve for concrete and prestressing tendons is illustrated in Figures 1 and 2.

$$S_{c, max} = \frac{|\sigma_{c,max}|}{f_{ck,fat}} \quad (3)$$

$$S_{c, min} = \frac{|\sigma_{c,min}|}{f_{ck,fat}} \tag{4}$$

where  $S_{c, max}$  is the maximum compressive stress level;  $S_{c, min}$  is the minimum compressive stress level;  $\sigma_{c,max}$  is the maximum compressive stress;  $\sigma_{c,min}$  is the minimum compressive stress;  $f_{ck,fat}$  is the fatigue-reference compressive strength.

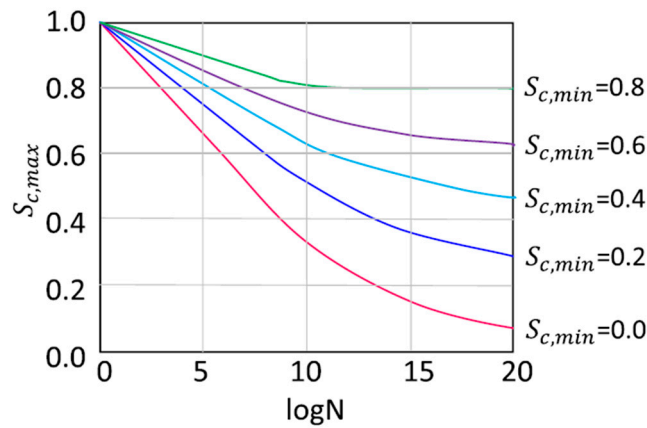


Figure 1. S–N curve for concrete [31].

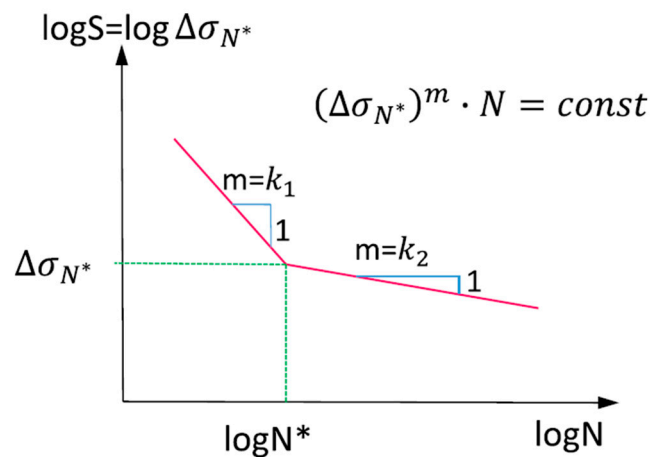


Figure 2. S–N curve for prestressing tendons [31].

If  $(\Delta\sigma > \Delta\sigma_{N^*})$

$$\log N_f = \log N^* - k_1 [\log(\Delta\sigma) - \log(\Delta\sigma_{N^*})] \tag{5}$$

If  $(\Delta\sigma < \Delta\sigma_{N^*})$

$$\log N_f = \log N^* + k_2 [\log(\Delta\sigma_{N^*}) - \log(\Delta\sigma)] \tag{6}$$

where  $\Delta\sigma$  is the stress range of the prestressing steel;  $\Delta\sigma_{N^*}$  is the stress range at  $N^*$  cycles;  $k_1, k_2$  are the stress exponents. Table 2 illustrates the parameters of prestressing steel S–N curve.

Table 2. Parameters of S–N curve for prestressing steel [31].

S–N Curve of Prestressing Steel Used for	Stress Exponent			$\Delta\sigma_{N^*}$ at $N^*$ Cycles (MPa)
	$N^*$	$k_1$	$k_2$	
Pre-Tensioning	$10^6$	5	9	185

### 2.3. Fatigue Life Assessment

In fatigue life assessment, there are two steps: cracking load calculation and fatigue life calculation. Initially, the stress range at the bottom fiber needs to be analyzed by:

$$\sigma_{cF}^b = \frac{nA_{ps}\sigma_{se}}{A_t} + \frac{nA_{ps}\sigma_{se}e}{I_t}y_t \quad (7)$$

where  $\sigma_{se}$  is the effective stress at each prestressing steel;  $A_{ps}$  is the cross-section area of a prestressing steel;  $e$  is the eccentricity;  $A_t$  is the transformed area of the sleeper;  $I_t$  is the inertia moment of transformed section before cracking;  $y_t$  is the distance of the centroidal axis of the transformed area from the soffit.

The cracking moment is calculated by:

$$M_{cr} = I_t \frac{\sigma_{cF}^b + f_{cf}}{y_t} \quad (8)$$

where  $f_{cf}$  is the tensile strength.

The neutral axis of the cross-section of the sleeper starts changing when the cracking propagates. Therefore, the distance from the center of gravity of the effective transformed area to the top of the compressed area can be calculated by:

$$y_{CG} = \text{root}[[S_{pcII} - n_e A'_{p3}(h - y_{cg} - d_3) - n_e A'_{p2}(h - y_{cg} - d_2) - n_e A'_{p1}(h - y_{cg} - d_1)], y_{cg}] \quad (9)$$

where the  $S_{pcII}$  is the first moment at the bottom fiber after cracking;  $A'_{pi}$  is the total area of the prestressed steel at layer  $i$ ;  $d_i$  is the distance from the prestressed steel at layer  $i$  to the bottom of the steel area; and  $n_e$  is the modular ratio.

The effective transformed section can be estimated using the transformed area of the sleeper cross-section  $A_{cII}$ :

$$A_{tII} = A_{cII} + n_e A_p \quad (10)$$

The moment of inertia of the cracking section is presented by:

$$I_{cr} = I_{ccr} + n_e A'_{p3}(h - y_{cg} - d_3)^2 + n_e A'_{p2}(h - y_{cg} - d_2)^2 + n_e A'_{p1}(h - y_{cg} - d_1)^2 \quad (11)$$

The effective inertia moment in the lifetime is given by:

$$I_{ef} = I_{cr} + (I_t - I_{cr}) \left( \frac{M_{cr}}{M_{max}} \right)^3 \quad (12)$$

where  $I_t$  is the inertia moment of transformed section before cracking;  $M_{cr}$  is the cracking moment;  $M_{max}$  is the maximum bending moment at the section under cyclic loads:

$$\Delta\sigma_{pt1} = n_e \frac{M_{max} - M_{min}}{I_{ef}} (h - y_{cg} - d_1) \quad (13)$$

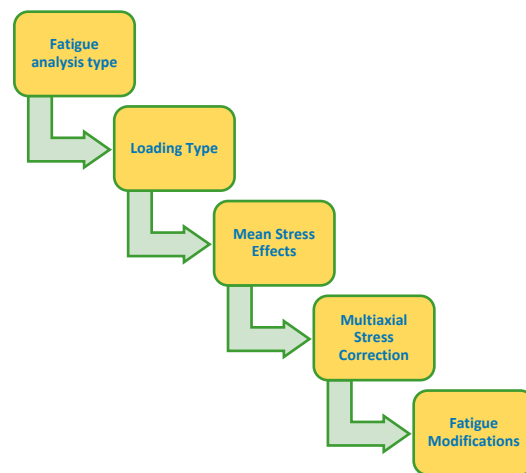
where  $M_{min}$  is the minimum bending moment at the section under cyclic loads.

Using the output value of  $\Delta\sigma_{pt1}$ , the failure cycles of the prestressing steel under constant cyclic loading can be estimated by Equations (5) or (6).

## 3. Numerical Life-Cycle Assessment Method of Prestressed Concrete Sleepers

### 3.1. Fatigue Analysis Decisions

Numerical fatigue analysis can be divided into five common stages listed in Figure 3. This figure illustrates the general flow of decisions required to perform a fatigue analysis.



**Figure 3.** Flowchart for fatigue analysis decision tree.

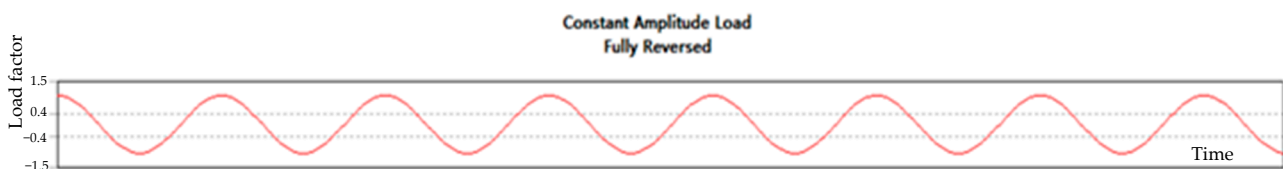
Fatigue analysis consists of ascertaining the stress life and strain life. Stress life is based on empirical S–N curves and then modified by a variety of factors. Strain life is based on the strain-life relation equation. The strain-life method is concerned with crack initiation and usually deals with relatively low cycles (less than  $10^5$  cycles). In this study, the stress-life method is used for life-cycle simulation of the railway sleeper. The stress-life method focuses on total fatigue life, which doesn't distinguish between cracking initiation and progression. The stress-life method is also suitable for simulation of relatively high cycles (more than  $10^5$  cycles) [32]. Normally, railway sleepers experience millions of cyclic loads during service life.

### 3.2. Types of Cyclic Loading

There are four types of fatigue loading in the simulation:

- Constant amplitude, proportional loading;
- Constant amplitude, non-proportional loading;
- Non-constant amplitude, proportional loading;
- Non-constant amplitude, non-proportional loading.

Each passed wheel is assumed as a single cycle with constant amplitude. The principal stress axes do not change over time [32]. Therefore, constant amplitude with proportional loading is used for fatigue-life simulation of the railway sleeper. Figure 4 shows the types of loading used in the simulation.



**Figure 4.** Cyclic loading type for life-cycle simulation of the railway sleeper.

### 3.3. Fatigue Life Results

In the fatigue analysis, the typical stress analysis can be used to determine the fatigue life of the prestressed concrete sleeper when it is subject to cyclic loads. This method is based on the S–N curve as part of the material definition of railway sleepers. The S–N curve is cyclic stress (S) against the logarithmic scale of cycles to failure (N). In the stress-life method, the alternating stress vs. the number of cycles to failure data are needed to put into the model [32]. It should be noted that the fatigue-life results using the stress-life method represent the available life for the given fatigue analysis without considering crack propagation and factors such as bond-slip, environmental conditions, etc.



#### 4. Prestressed Concrete Sleeper Modelling

##### 4.1. Properties of the Railway Sleeper

This project is a collaborative study between the University of Birmingham and the China Academy of Railway Sciences (CARS). CARS has commissioned full-scale experimental studies to support this collaboration. In this study, the 2600-mm long Chinese Type III prestressed concrete sleeper (Figure 5) was originally designed for high-speed railways, with the properties shown in Table 3. The dimension of the sleeper is approximately 2600 mm × 320 mm × 260 mm including 10 prestressing tendons with 7 mm diameters. The sleeper will be assessed using the numerical and theoretical approaches to calculate the life-cycle.

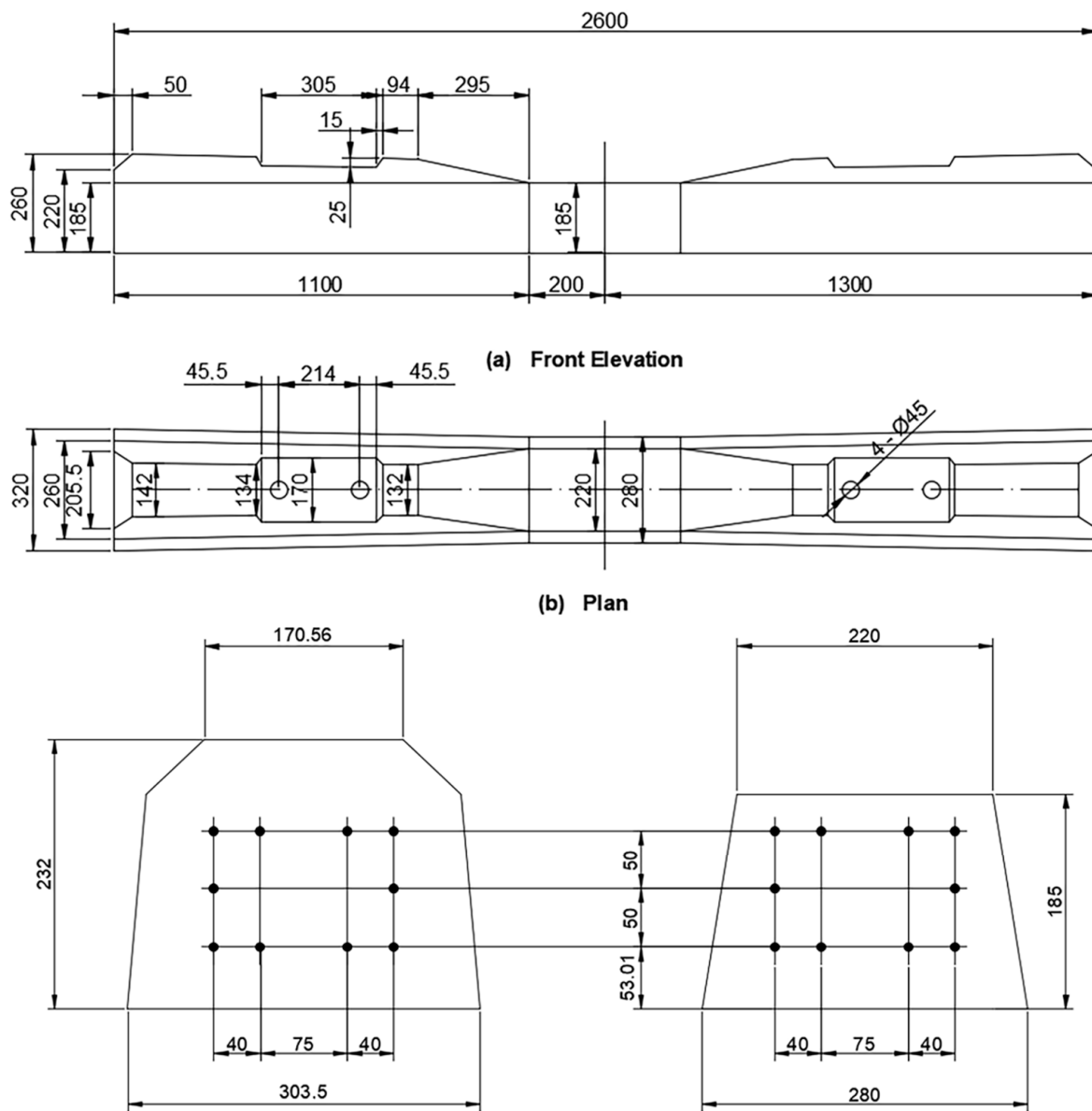


Figure 5. Chinese Type III prestressed concrete sleeper.

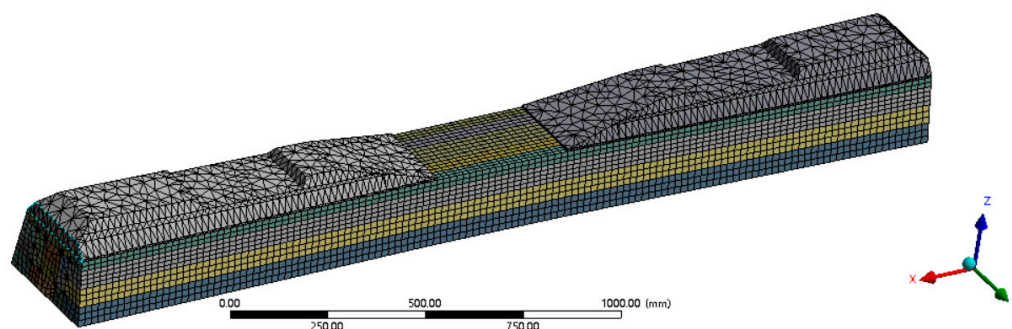


**Table 3.** Material properties of Chinese Type III prestressed concrete sleeper.

Material Properties	Basic Variables	Value
Concrete	• Mean compressive strength	65 MPa
	• Modulus of elasticity	33 GPa
	• Yield strength	1570 MPa
Prestressed wire	• Modulus of elasticity	200 GPa
	• Prestressing force	420 kN

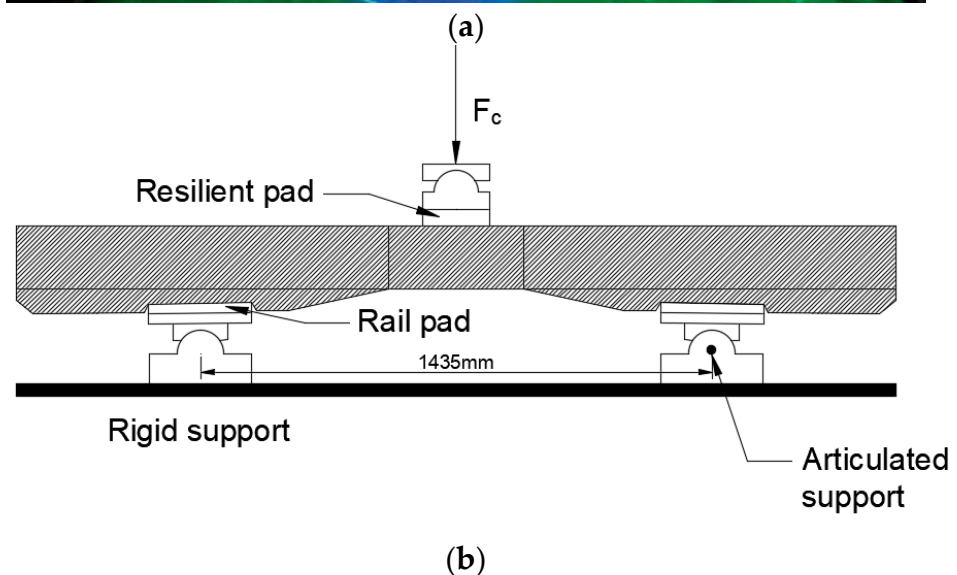
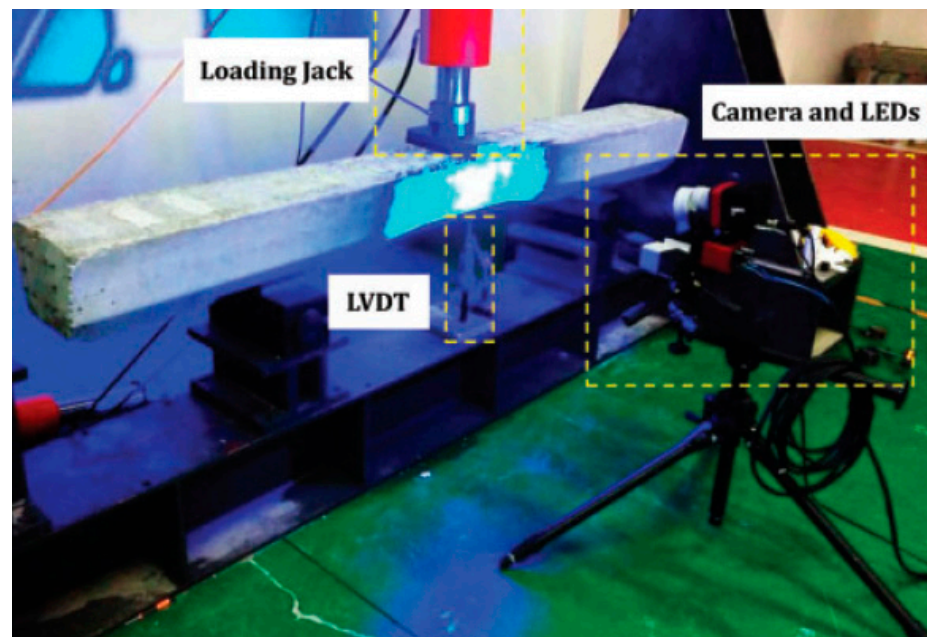
#### 4.2. Finite Element Model

In this study, the finite element method (FEM) is used to analyze the life-cycle of prestressed concrete sleepers with surface abrasion. The prestressed concrete sleeper is modelled in ANSYS Workbench (shown in Figure 6). The finite element model is composed of concrete and prestressed tendons. The Solid65 element is used to model the concrete material. In the model, thermal condition is used to simulate the characteristics of prestressing tendons. The support condition is modelled as fixed support. In the model, the contact condition No Separation is used between concrete and prestressing tendons. Therefore, the concrete and prestressing tendons are considered as being well adhered, while the bond slip and bursting are ignored. The material properties of the FE sleeper model are shown in Table 3. The modelling is performed with the minimum difference from the real sleeper.

**Figure 6.** FE sleeper model.

#### 4.3. Experimental Program

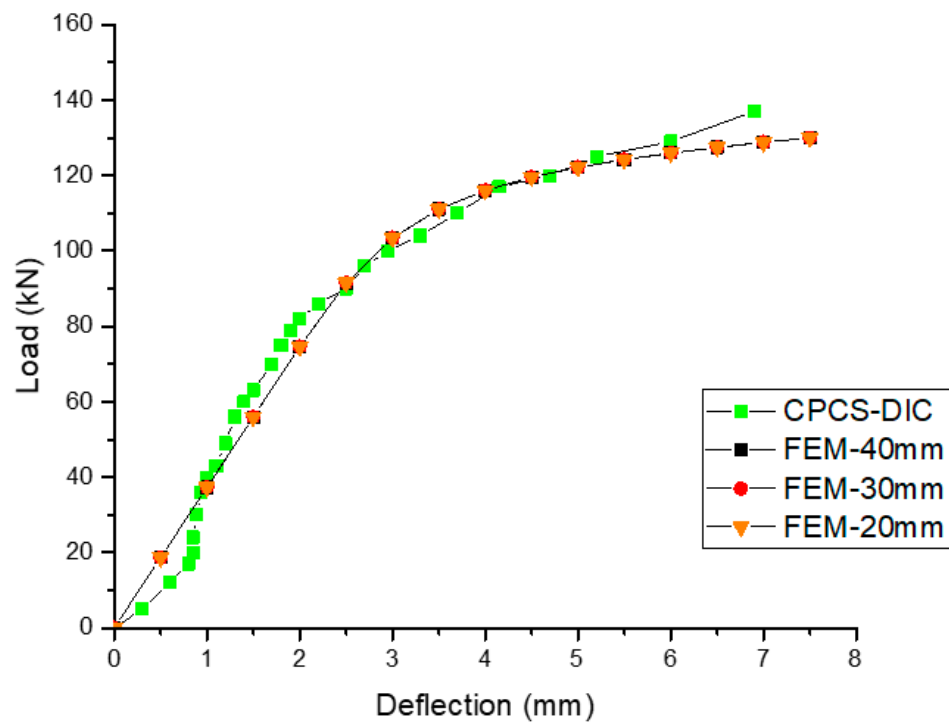
The bending moment test at the midspan of the full-scale prestressed concrete sleeper using the digital image correlation method (DIC) conducted by Jing et al. [33], as part of CARS's commissioned tests, is used for the FE model validation. This experiment presented the nonlinear structural performance of Chinese Type III prestressed concrete sleeper. The arrangement for the test follows EN13230-2 shown in Figure 7 [33]. The loading surface was placed at the bottom midspan of the sleeper with a resilient pad. Two rail pads were placed between the rail-seat area and each support. Sadeghi and Barati stated that the normal failure load of concrete sleepers is 140 kN [34], thus the applied load range was between 0 to 140 kN. The speed of loading was no more than 120 kN/min. The experimental load–deflection results in terms of the DIC will be compared with the numerical results for the sleeper model validation.



**Figure 7.** Arrangement for the bending moment test at midspan of the prestressed concrete sleeper [33,35]. (a) Experimental apparatus of the bending moment test. (b) Setup for the bending moment test.

#### 4.4. FE Sleeper Model Validation

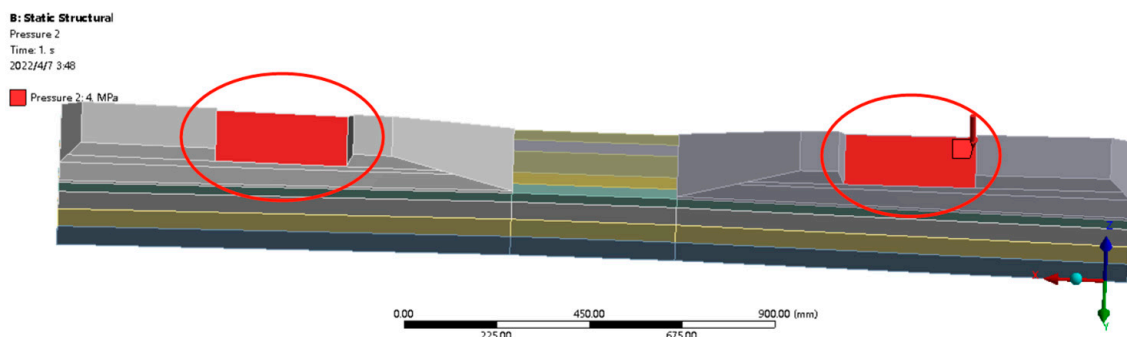
The material and structural performance of the FE sleeper model needs to be validated for further simulation. Previous research has presented the validation of the FE sleeper model in reference [23]. The mesh study of the FE sleeper model is also carried out for the models with 20 mm, 30 mm, and 40 mm mesh size. Figure 8 illustrates the load–deflection responses of the experimental and numerical results. The mesh study shows slight differences between the mesh size 20 mm, 30 mm, and 40 mm. Therefore, the closest results of mesh size 30 mm are selected (with 5.99% max error calculated from the deviation of the experimental and FEM results). The numerical performance indicates a good agreement with the experimental results.



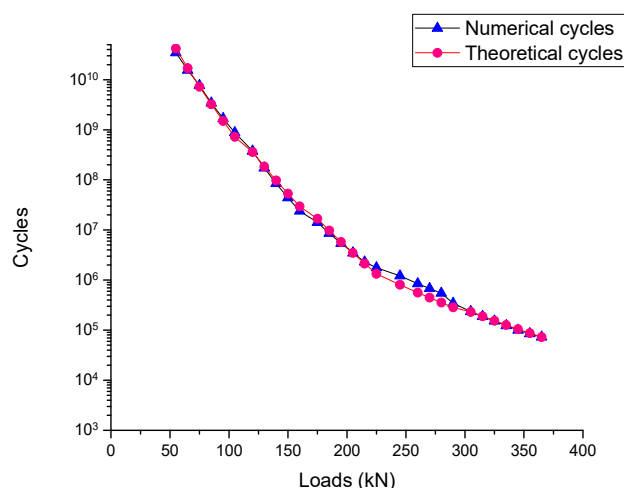
**Figure 8.** Load–deflection responses of experimental and numerical results.

#### 4.5. Fatigue Model Validation

The life-cycle is evaluated by numerical and theoretical approaches with the cyclic loads between 55 kN and 365 kN. Each cyclic load (constant) can only calculate one fatigue life for both the theoretical and numerical methods. These results present the available life of the prestressed concrete sleepers for the fatigue analysis. The cyclic load is applied at the rail-seat area shown in Figure 9. Note that the static and fatigue tests are in a different test set up. The negative bending test was performed for the static tests (in accordance with EN 13230), whilst the positive rail-seat tests were considered for the fatigue tests. The theoretical results of the life-cycle were according to the damage accumulation method. The calculation details were presented in reference [29]. The results of the numerical and theoretical calculation are demonstrated in Figure 10. Life cycles are inversely proportional with the constant cyclic loads for both the numerical and theoretical results. In comparison between numerical and theoretical results, the average error is only 13.03%.



**Figure 9.** Setup for boundary conditions in the fatigue life simulation. The sleepers in the model are fully supported by ballast and substructure.



**Figure 10.** Comparison between numerical and theoretical fatigue-life results.

The experiments conducted by Parvez and Foster investigated failure cycles of prestressed concrete sleepers under cyclic loads [16,36,37]. Two specimens were selected from their experiments in order to validate the numerical fatigue model. The average of the failure cycles of the specimens are calculated and presented in Table 4. Table 5 shows the comparison between the experimental, theoretical, and numerical results.

**Table 4.** Experimental failure cycle of prestressed concrete sleepers [29].

Specimen ID	Failure Cycles	Average	Standard Deviation
SF2-a	773,793	896,290	173,236
SF3-a	1,018,787		

**Table 5.** Comparison between experimental, theoretical, and numerical results.

Experimental Result	Failure Cycles			Numerical Result	Deviation Ratio%
	Theoretical Result	Deviation Ratio%			
896,290	889,577	0.75	849,000	5.28	

From Figure 10 and Table 5, it is seen that the numerical results have a good correlation with the experimental and theoretical results, which provides a reliable method for the life-cycle in the surface abrasion study.

## 5. Influence of Surface Abrasions on Fatigue Life

In reality, railway sleepers experience aggressive dynamic loading, especially in sharp curves and high gradients, which causes rail-seat abrasion. The ballast angularity also results in differential abrasion on the soffit abrasion. The most common surface abrasions of railway sleepers are the rail-seat abrasion, the soffit abrasion at rail-seat, and the soffit abrasion at midspan [10]. Figure 11 shows the typical abrasions of a railway sleeper. This section investigates the life-cycle of the railway sleeper with each typical surface abrasion pattern using the numerical fatigue-life model. In the simulation, abrasions are applied in the FE sleeper model by changing the geometry of the rail-seat area and bottom surface at midspan. It is clear that the life-cycle can be affected by the surface abrasions.

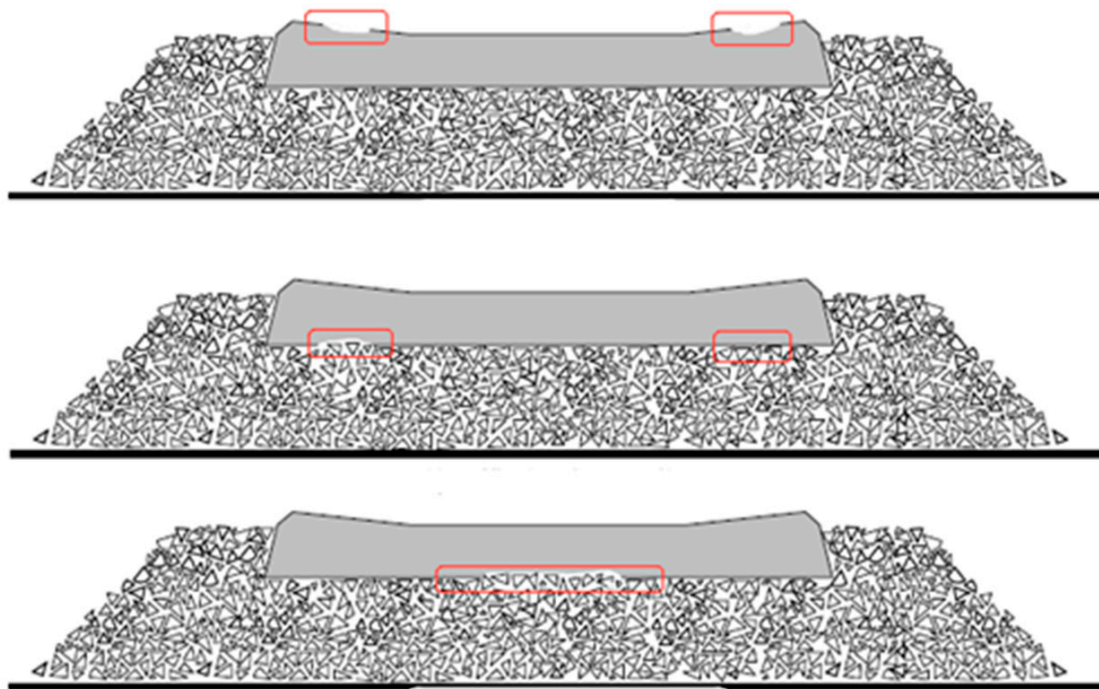


Figure 11. Typical surface abrasions of railway sleepers [10].

5.1. Rail-Seat Abrasion Results

Figure 12 shows the location of the rail-seat abrasion of the railway sleeper model. The depths of the rail-seat abrasions are chosen as 5 mm, 15 mm, and 30 mm to analyze the effect of the life-cycle on the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 6 and Figure 13 indicate the results of the life-cycle with rail-seat abrasion.

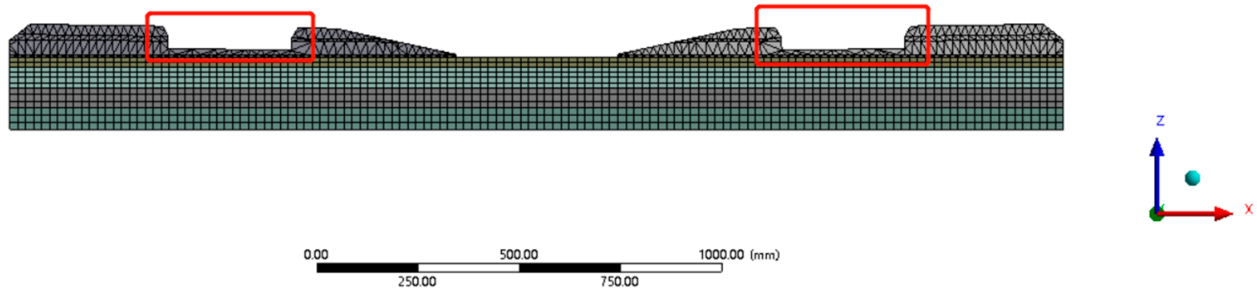


Figure 12. Rail-seat abrasion of the railway sleeper model.

Table 6. Life-cycle results of the railway sleeper with rail-seat abrasion.

Load (kN)	No Abrasion	5 mm Rail-Seat Abrasion	15 mm Rail-Seat Abrasion	30 mm Rail-Seat Abrasion
55	$3.47 \times 10^{10}$	$2.12 \times 10^{10}$	$1.75 \times 10^{10}$	$4.15 \times 10^9$
105	$8.79 \times 10^8$	$3.27 \times 10^8$	$2.23 \times 10^8$	$1.83 \times 10^7$
160	$2.39 \times 10^7$	$9.68 \times 10^6$	$6.81 \times 10^6$	$1.01 \times 10^6$
215	$2.30 \times 10^6$	$1.25 \times 10^6$	$9.90 \times 10^5$	$1.23 \times 10^5$
270	$6.79 \times 10^5$	$2.38 \times 10^5$	$1.82 \times 10^5$	36,627
325	$1.52 \times 10^5$	78,521	62,593	14,068



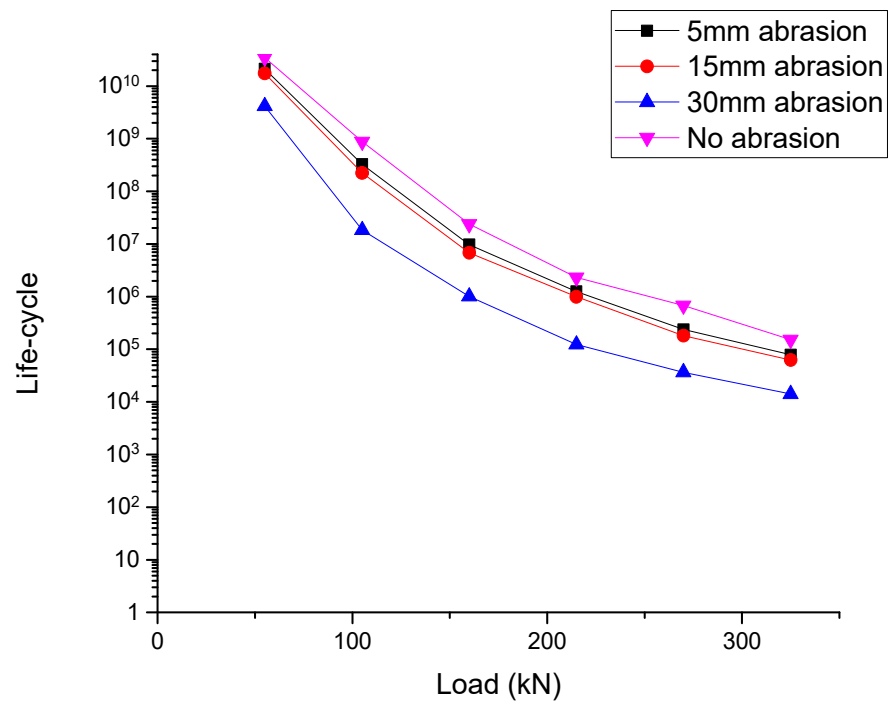


Figure 13. Comparison of life-cycle results with rail-seat abrasion.

5.2. Soffit Abrasion at Rail-Seat Results

Figure 14 shows the location of the soffit abrasion at the rail seat of the railway sleeper model. The depths of the soffit abrasions at the rail seat are chosen as 5 mm, 15 mm, and 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 7 and Figure 15 indicate the results on the life-cycle with the soffit abrasion at the rail seat.

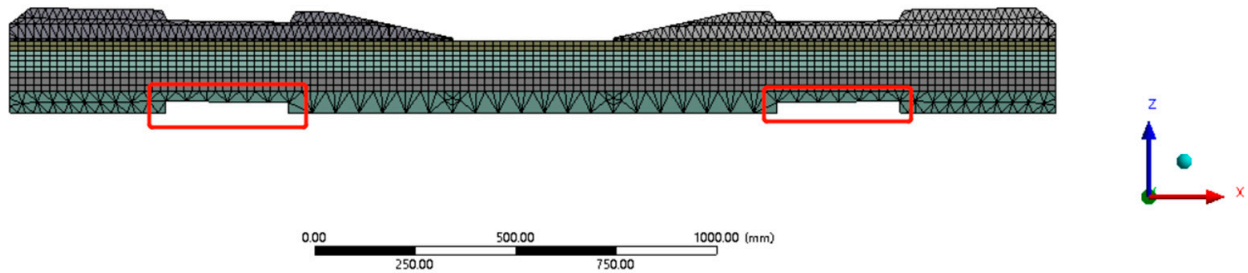


Figure 14. Soffit abrasion at rail seat of the railway sleeper model.

Table 7. Life-cycle results of the railway sleeper with soffit abrasion at rail seat.

Load (kN)	No Abrasion	5 mm Soffit Abrasion at Rail Seat	15 mm Soffit Abrasion at Rail Seat	30 mm Soffit Abrasion at Rail Seat
55	$3.47 \times 10^{10}$	$2.85 \times 10^9$	$1.08 \times 10^9$	$5.04 \times 10^8$
105	$8.79 \times 10^8$	$1.10 \times 10^7$	$2.99 \times 10^6$	$1.63 \times 10^6$
160	$2.39 \times 10^7$	$7.19 \times 10^5$	$1.87 \times 10^5$	$1.02 \times 10^5$
215	$2.30 \times 10^6$	85,372	36,816	22,380
270	$6.79 \times 10^5$	26,466	11,413	4527
325	$1.52 \times 10^5$	10,165	1673	936

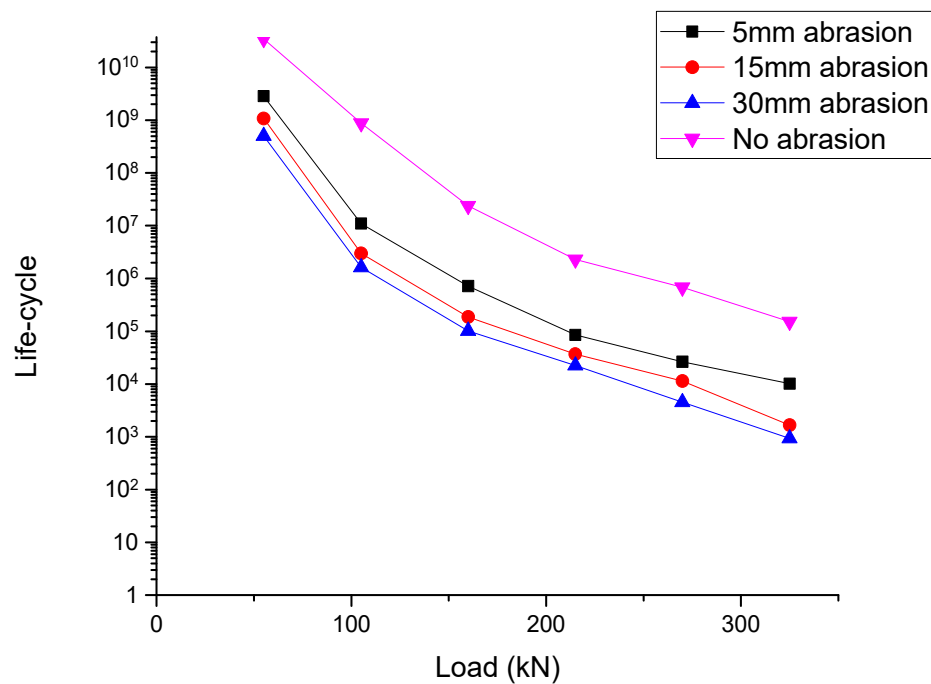


Figure 15. Comparison of life-cycle results with soffit abrasion at rail seat.

5.3. Soffit Abrasion at Midspan Results

Figure 16 shows the location of the soffit abrasion at the midspan of the railway sleeper model. The depths of the soffit abrasion at midspan are chosen as 5 mm, 15 mm, and 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 8 and Figure 17 indicate the results on the life-cycle with the soffit abrasion at midspan.

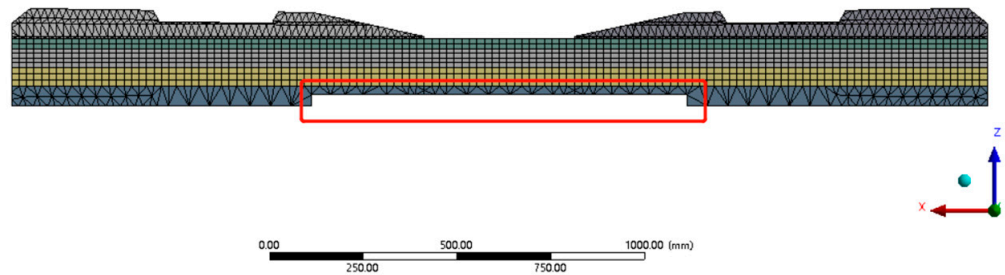


Figure 16. Soffit abrasion at midspan of the railway sleeper model.

Table 8. Life-cycle results of the railway sleeper with soffit abrasion at midspan.

Load (kN)	No Abrasion	5 mm Soffit Abrasion at Midspan	15 mm Soffit Abrasion at Midspan	30 mm Soffit Abrasion at Midspan
55	$3.47 \times 10^{10}$	$4.59 \times 10^9$	$3.04 \times 10^9$	$1.54 \times 10^9$
105	$8.79 \times 10^8$	$2.09 \times 10^7$	$1.20 \times 10^7$	$4.81 \times 10^6$
160	$2.39 \times 10^7$	$1.10 \times 10^6$	$7.61 \times 10^5$	$2.68 \times 10^5$
215	$2.30 \times 10^6$	$1.37 \times 10^5$	90,168	50,015
270	$6.79 \times 10^5$	39,963	27,953	15,505
325	$1.52 \times 10^5$	15,349	10,736	3250



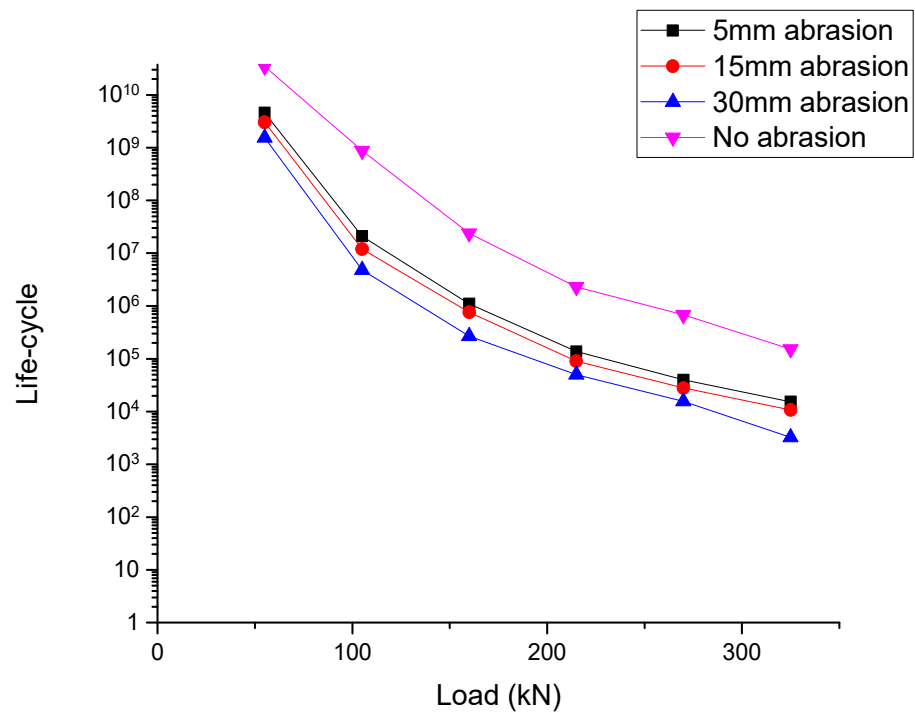


Figure 17. Comparison of life-cycle results with soffit abrasion at midspan.

5.4. Rail-Seat Abrasion and Soffit Abrasion at Rail Seat Results

Figure 18 shows the location of the rail-seat abrasion and the soffit abrasion at the rail seat of the railway sleeper model. The depths of the abrasions are chosen as 5 mm & 5 mm, 15 mm & 15 mm, and 30 mm & 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 9 and Figure 19 indicate the results on the life-cycle with the rail-seat abrasion and soffit abrasion at the rail seat.

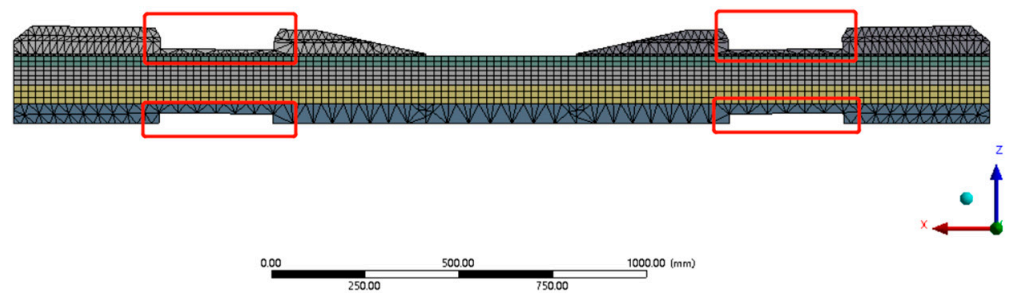


Figure 18. Rail-seat abrasion and soffit abrasion at rail seat of the railway sleeper model.

Table 9. Life-cycle results of the railway sleeper with rail-seat abrasion and soffit abrasion at rail seat.

Load (kN)	No Abrasion	5 mm & 5 mm	15 mm & 15 mm	30 mm & 30 mm
55	$3.47 \times 10^{10}$	$2.25 \times 10^9$	$3.12 \times 10^8$	$3.25 \times 10^7$
105	$8.79 \times 10^8$	$8.01 \times 10^6$	$1.22 \times 10^6$	$1.90 \times 10^5$
160	$2.39 \times 10^7$	$5.80 \times 10^5$	76,391	20,139
215	$2.30 \times 10^6$	69,485	16,878	1728
270	$6.79 \times 10^5$	21,541	2455	792
325	$1.52 \times 10^5$	6630	871	621

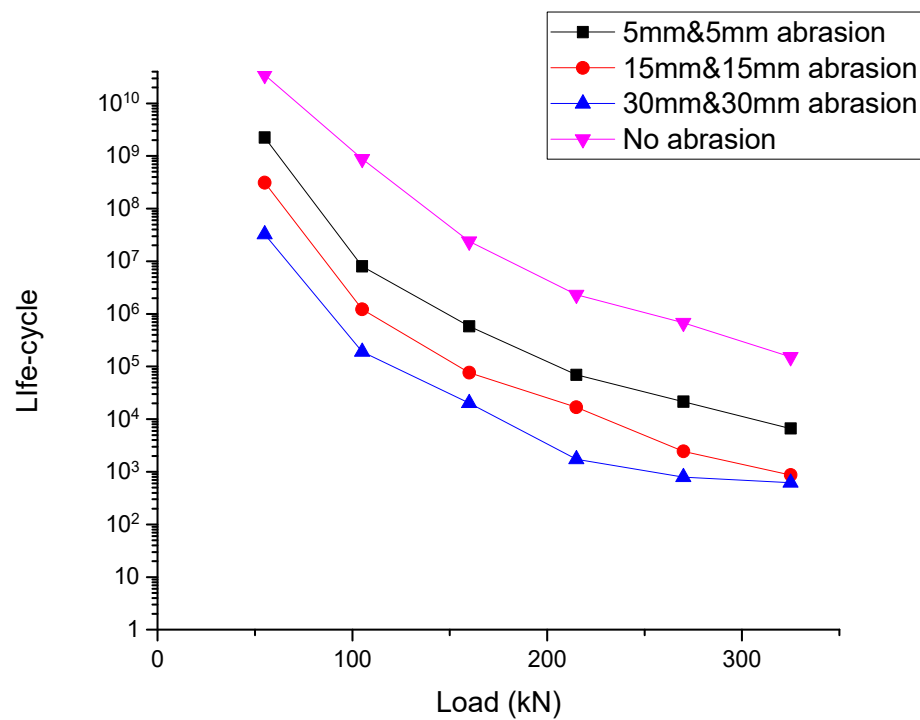


Figure 19. Comparison of life-cycle results with rail-seat abrasion and soffit abrasion at rail seat.

5.5. Rail-Seat Abrasion and Soffit Abrasion at Midspan Results

Figure 20 shows the location of the rail-seat abrasion and the soffit abrasion at midspan of the railway sleeper model. The depths of the abrasions are chosen as 5 mm & 5 mm, 15 mm & 15 mm, and 30 mm & 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 10 and Figure 21 indicate the results on the life-cycle with the rail-seat abrasion and soffit abrasion at midspan.

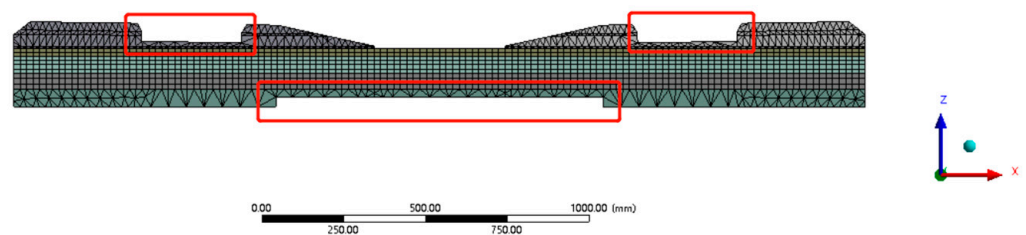


Figure 20. Rail-seat abrasion and soffit abrasion at midspan of the railway sleeper model.

Table 10. Life-cycle results of the railway sleeper with rail-seat abrasion and soffit abrasion at midspan.

Load (kN)	No Abrasion	5 mm & 5 mm	15 mm & 15 mm	30 mm & 30 mm
55	$3.47 \times 10^{10}$	$2.73 \times 10^9$	$1.33 \times 10^9$	$7.74 \times 10^8$
105	$8.79 \times 10^8$	$1.04 \times 10^7$	$3.95 \times 10^6$	$2.12 \times 10^6$
160	$2.39 \times 10^7$	$6.91 \times 10^5$	$2.31 \times 10^5$	$1.39 \times 10^5$
215	$2.30 \times 10^6$	82,248	44,032	28,812
270	$6.79 \times 10^5$	25,498	13,650	7,828
325	$1.52 \times 10^5$	9,557	2,466	998

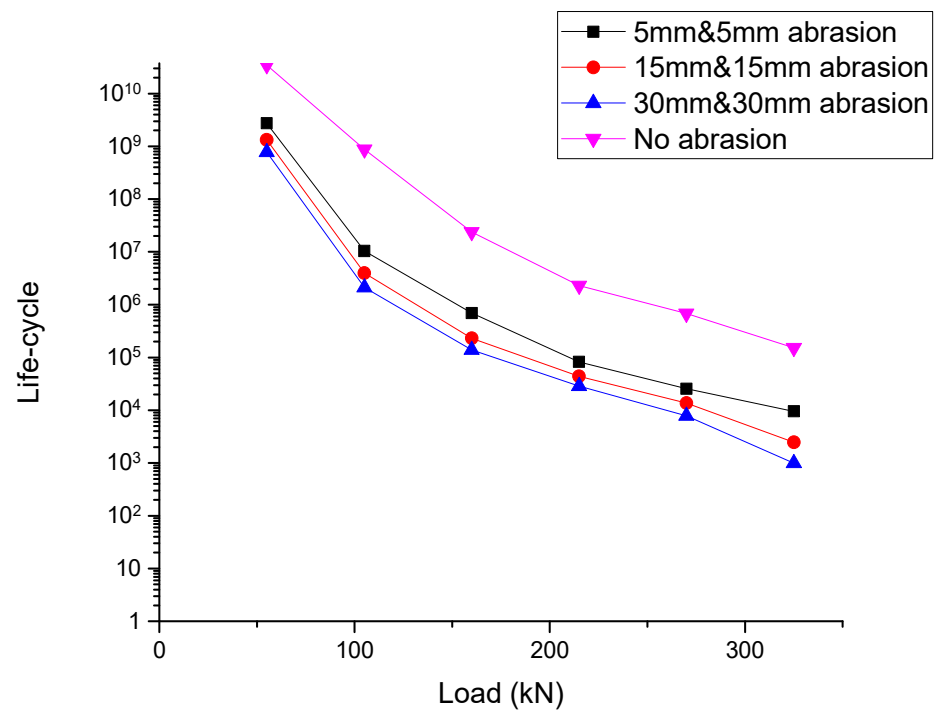


Figure 21. Comparison of life-cycle results with rail-seat abrasion and soffit abrasion at midspan.

5.6. Soffit Abrasion at Rail Seat and Soffit Abrasion at Midspan Results

Figure 22 shows the location of the soffit abrasion at the rail seat and the soffit abrasion at midspan of the railway sleeper model. The depths of the abrasions are chosen as 5 mm & 5 mm, 15 mm & 15 mm, and 30 mm & 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 11 and Figure 23 indicate the results on the life-cycle with the soffit abrasion at the rail seat and the soffit abrasion at midspan.

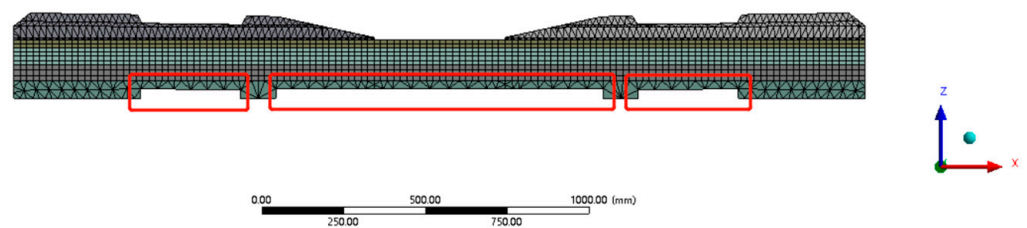


Figure 22. Soffit abrasion at rail seat and soffit abrasion at midspan of the railway sleeper model.

Table 11. Life-cycle results of the railway sleeper with soffit abrasion at rail seat and soffit abrasion at midspan.

Load (kN)	No Abrasion	5 mm & 5 mm	15 mm & 15 mm	30 mm & 30 mm
55	3.47 × 10 <sup>10</sup>	2.49 × 10 <sup>9</sup>	6.26 × 10 <sup>8</sup>	3.37 × 10 <sup>8</sup>
105	8.79 × 10 <sup>8</sup>	9.23 × 10 <sup>6</sup>	1.86 × 10 <sup>6</sup>	1.28 × 10 <sup>6</sup>
160	2.39 × 10 <sup>7</sup>	6.38 × 10 <sup>5</sup>	1.19 × 10 <sup>5</sup>	79,896
215	2.30 × 10 <sup>6</sup>	76,113	25,415	17,652
270	6.79 × 10 <sup>5</sup>	23,596	5963	2706
325	1.52 × 10 <sup>5</sup>	8078	966	881

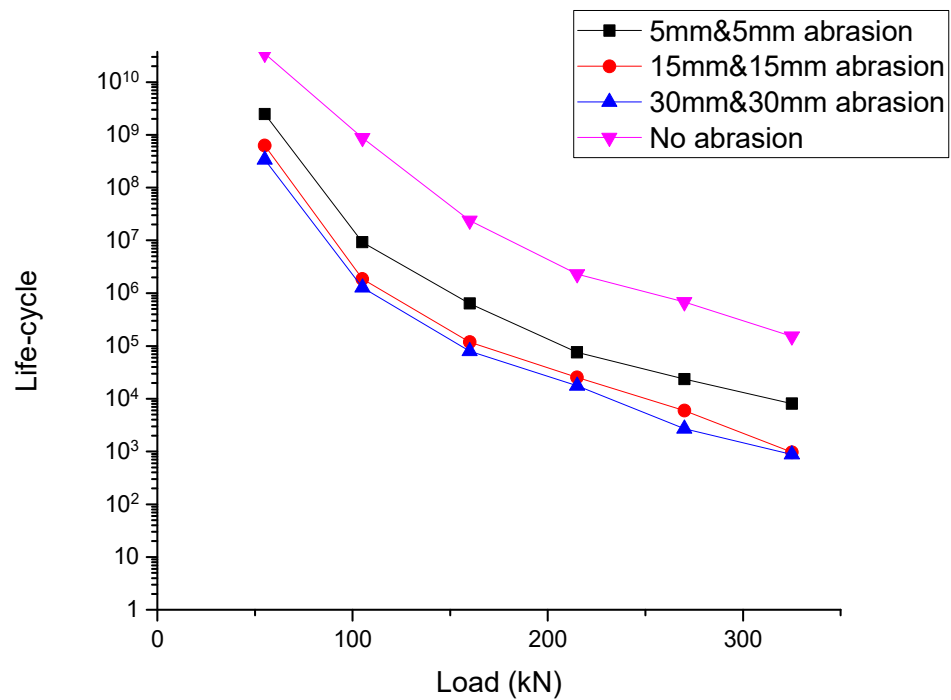


Figure 23. Comparison of life-cycle results with soffit abrasion at rail seat and soffit abrasion at midspan.

5.7. Rail-Seat Abrasion, Soffit Abrasion at Rail Seat, and Soffit Abrasion at Midspan Results

Figure 24 shows the location of the rail-seat abrasion, the soffit abrasion at rail seat, and the soffit abrasion at midspan of the railway sleeper model. The depths of the abrasions are chosen as 5 mm & 5 mm & 5 mm, 15 mm & 15 mm & 15 mm, and 30 mm & 30 mm & 30 mm to analyze the effect on the life-cycle of the railway sleeper. Loads of between 55 kN to 325 kN are applied in the simulation. Table 12 and Figure 25 indicate the results on the life-cycle with the rail-seat abrasion, the soffit abrasion at rail seat, and the soffit abrasion at midspan.

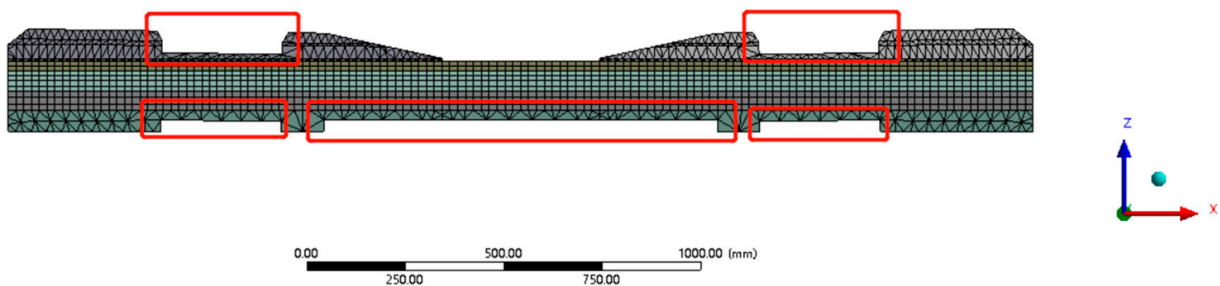
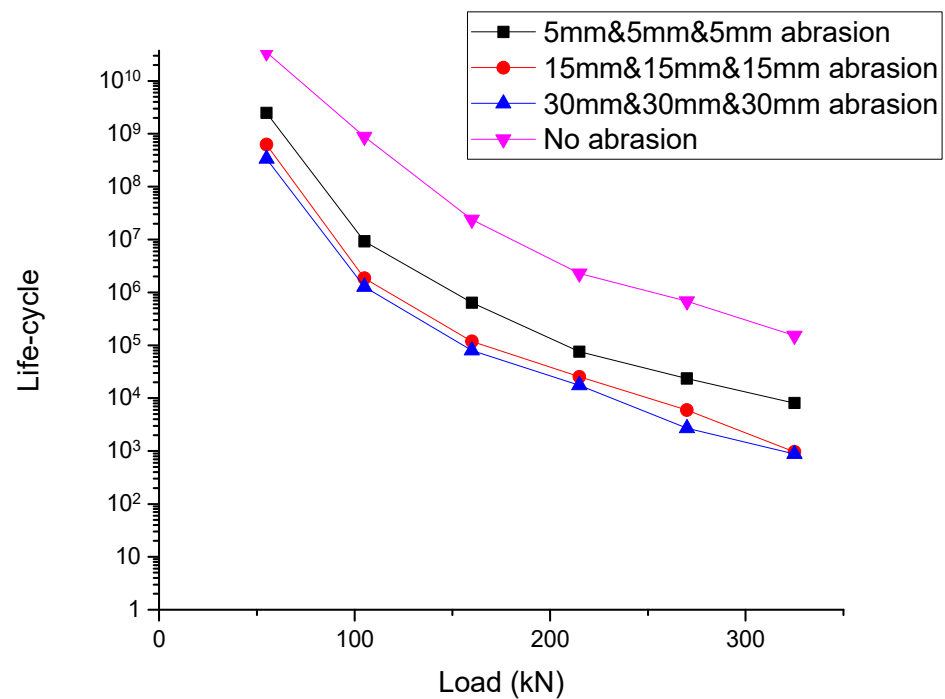


Figure 24. Rail-seat abrasion, soffit abrasion at rail seat and soffit abrasion at midspan of the railway sleeper model.

Table 12. Life-cycle results of the railway sleeper with rail-seat abrasion, soffit abrasion at rail seat and soffit abrasion at midspan.

Load (kN)	No Abrasion	5 mm & 5 mm & 5 mm	15 mm & 15 mm & 15 mm	30 mm & 30 mm & 30 mm
55	$3.47 \times 10^{10}$	$2.49 \times 10^9$	$6.26 \times 10^8$	$3.37 \times 10^8$
105	$8.79 \times 10^8$	$9.23 \times 10^6$	$1.86 \times 10^6$	$1.28 \times 10^6$
160	$2.39 \times 10^7$	$6.38 \times 10^5$	$1.19 \times 10^5$	79,896
215	$2.30 \times 10^6$	76,113	25,415	17,652
270	$6.79 \times 10^5$	23,596	5963	2706
325	$1.52 \times 10^5$	8078	966	881



**Figure 25.** Comparison of life-cycle results with rail-seat abrasion, soffit abrasion at rail seat and soffit abrasion at midspan.

### 5.8. Discussions

Sections 5.1–5.3 demonstrate the life-cycle results with the single abrasion pattern of the railway sleeper. Sections 5.4–5.7 present the life-cycle results with the combination of the different abrasion patterns of the railway sleeper. The abrasion depth of the prestressed concrete sleeper is reduced by 5 mm, 15 mm, and 30 mm, respectively. In general, the life-cycle of the worn railway sleeper is less than an undamaged sleeper. The life-cycle decreases with an increase in abrasion, especially large depth abrasion (30 mm). Higher dynamic loads result in a reduction in the life-cycle. However, at the same abrasion depth, the performance of the sleeper varies with different abrasion patterns.

On comparison with each single abrasion patterns, the effect of the soffit abrasion at rail seat on the railway sleeper is the most significant. The soffit abrasion at midspan also has a very significant influence on the sleeper. For both of the soffit abrasion patterns, the life-cycle falls by more than 90%. The change of the life-cycle due to rail-seat abrasion is relatively low, with only a 53.32% change in comparison with an undamaged sleeper. However, when the rail-seat abrasion rises to 30 mm, the life-cycle also reduces by up to 93.63%.

Sections 5.4–5.7 show that the combination of the different abrasion patterns affects the life-cycle of the prestressed concrete sleeper. The results demonstrate more than one abrasion pattern occurring in the sleeper, and the life-cycle decreases sharply. There are four groups of multi-abrasion patterns analyzed. The triple abrasion (combination of rail-seat abrasion, soffit abrasion at rail seat, and soffit abrasion at midspan) is the most critically damaging. With a 5 mm abrasion for each position, the life-cycle falls by 97.16%. The worst case in this study is the triple abrasion with 30 mm depth, where the life-cycle undergoes a 99.88% change. For the double abrasion patterns (rail-seat abrasion/soffit abrasion at rail seat, rail-seat abrasion/soffit abrasion at midspan, and soffit abrasion at rail seat/soffit abrasion at midspan), the results are not very different. The combination of soffit abrasion at rail seat and soffit abrasion at midspan pattern is relatively worse than the other two double abrasion patterns, which reduces the life-cycle by up to 96.16%.

## 6. Conclusions

In this research, 3D finite element models were developed to investigate the fatigue behavior of the prestressed concrete sleeper considering surface abrasion. The theoretical life-cycle assessment method based on the damage accumulation concept was also demonstrated. The fatigue behavior of the prestressed concrete sleepers with surface abrasions were assessed by a numerical fatigue model. Seven cases of surface abrasion pattern were considered in this study. For each case analysis, a series of abrasion depths and dynamic loads were applied in numerical model in order to investigate the performance of the prestressed concrete sleeper. Based on the obtained results of this study, the key findings are revealed as follows:

- Surface abrasion significantly influences the structural performance of prestressed concrete sleepers. From the results, undamaged sleepers have much more service life than worn sleepers. Therefore, track maintenance should be carried out regularly to prevent loss of life-cycle from surface abrasion;
- Rail-seat abrasion has a relatively low influence on railway sleepers in comparison with soffit abrasion. Soffit abrasion at the rail seat can critically reduce the life-cycle;
- The risk of more than one abrasion pattern happening in the railway sleeper is far greater than a single abrasion pattern;
- In this study, the life-cycle was found to largely depend on the magnitude of the dynamic load and abrasion depth. Both large dynamic loads and abrasion depths can result in serious decreases in life-cycle.

This study is the first to present a finite element modelling for determining the life-cycle of the prestressed concrete sleepers with surface abrasion. The numerical fatigue model was validated using the theoretical life-cycle assessment method. The FE sleeper model was also validated by comprehensive experimental data. It should be noted that, in general, the lifespan of prestressed concrete sleepers can also be affected by factors such as bond slip, environmental conditions, chemical attack, etc. For example, the bond between the strand and the concrete is a factor which can directly or indirectly influence the lifespan of prestressed concrete sleepers. Therefore, more factors affecting the fatigue life of prestressed concrete sleepers are suggested for investigation in future research.

This paper confirms that inspection of railway sleepers is essential and even small abrasions that occur in critical positions can still affect the performance of railway sleepers. It is obvious that surface abrasions can result in a significant reduction in the life-cycle. Hence, it is important to reduce the impact loading to prevent railway sleepers from failing. From this study, the railway concrete sleepers should be inspected regularly, for example, every 10 to 15 years (or around 300 to 450 MGT or million gross tons). The outcomes of this study lead to a better insight into the effects of surface abrasion on prestressed concrete sleepers. This insight will enhance the inspection criteria of railway sleepers and track maintenance.

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