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# Energy Conversion and Management

## Evaluation of the property methods for pure and mixture of CO<sub>2</sub> for power cycles analysis

--Manuscript Draft--

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<b>Abstract:</b>	<p>The use of a binary cycle coupled to the complete reinjection of non-condensable gases could provide a valid answer to the improvement of the sustainability of geothermal plants. In recent years, the interest in the use of CO<sub>2</sub> as a working fluid in transcritical cycles has increased. However, the low critical temperature of carbon dioxide (<math>\approx 30^\circ\text{C}</math>) requires the cooling cycle, temperatures below <math>15^\circ\text{C}</math>, which are not always available. In this work, to overcome this limitation and obtain a higher critical temperature and a lower maximum pressure for more flexible applications of transcritical binary cycles, the possibility of using a second component, mixed with CO<sub>2</sub>, has been evaluated. For this purpose, the following fluids have been proposed: R1234yf, R1234ze(E), n-butane, n-hexane, n-pentane and propane, with a minimum considered carbon dioxide molar content of 60%. To carry out a cycle analysis, the knowledge of the thermodynamic properties of CO<sub>2</sub>-mixtures is fundamental; however, suitable equations of state under the appropriate conditions for these blends have not been clearly defined yet. Therefore, in the first part of this paper, different EoS for predicting thermodynamic properties of pure CO<sub>2</sub> and CO<sub>2</sub>-based mixtures are analysed and compared with reference data obtained from works published in the literature. However, because of the lack of experimental data of the selected blends, the values of density, enthalpy and entropy, obtained with the selected EoS are compared with NIST REFPROP results. The EoS involved in the evaluation are cubic-type (PR, PR-Twu, PRSV, RK, SRK, GCEOS), Virial-type (LKP, BWRS), Helmholtz-type (SW) and SAFT-type (PC-SAFT). In a power cycle, the fluid works under different conditions, involving several possible states across the components. So the influence of the different EoS on each power cycle's key component for pure CO<sub>2</sub> and two selected CO<sub>2</sub>-based mixtures has been assessed. The thermodynamic results show that the CO<sub>2</sub>-based mixtures, in a transcritical configuration, can achieve efficiencies higher than the sCO<sub>2</sub> power cycle.</p>

# Evaluation of the property methods for pure and mixture of CO<sub>2</sub> for power cycles analysis

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## 1. Abstract

The use of a binary cycle coupled to the complete reinjection of non-condensable gases could provide a valid answer to the improvement of the sustainability of geothermal plants. In recent years, the interest in the use of CO<sub>2</sub> as a working fluid in transcritical cycles has increased. However, the low critical temperature of carbon dioxide ( $\approx 30^\circ\text{C}$ ) requires the cooling cycle, temperatures below  $15^\circ\text{C}$ , which are not always available. In this work, to overcome this limitation and obtain a higher critical temperature and a lower maximum pressure for more flexible applications of transcritical binary cycles, the possibility of using a second component, mixed with CO<sub>2</sub>, has been evaluated. For this purpose, the following fluids have been proposed: R1234yf, R1234ze(E), n-butane, n-hexane, n-pentane, and propane, with a minimum considered carbon dioxide molar content of 60%. To carry out a cycle analysis, the knowledge of the thermodynamic properties of CO<sub>2</sub>-mixtures is fundamental; however, suitable equations of state under the appropriate conditions for these blends have not been clearly defined yet. Therefore, in the first part of this paper, different EoS for predicting thermodynamic properties of pure CO<sub>2</sub> and CO<sub>2</sub>-based mixtures are analyzed and compared with reference data obtained from works published in the literature. However, because of the lack of experimental data of the selected blends, the values of density, enthalpy and entropy, obtained with the selected EoS, are compared with NIST REFPROP results. The EoS involved in the evaluation are cubic-type (PR, PR-Twu, PRSV, RK, SRK, GCEOS), Virial-type (LKP, BWRS), Helmholtz-type (SW), and SAFT-type (PC-SAFT). In a power cycle, the fluid works under different conditions, involving several possible states across the components. So the influence of the different EoS on each power cycle's key component for pure CO<sub>2</sub> and two selected CO<sub>2</sub>-based mixtures has been investigated. Finally, a qualitative study of the flammability of the new blends is carried out. The thermodynamic results show that the CO<sub>2</sub>-based mixtures, in a transcritical configuration, can achieve efficiencies higher than the sCO<sub>2</sub> power cycle.

**Keywords:** CO<sub>2</sub>, CO<sub>2</sub>-based mixtures, equation of state, low-temperature application, power cycle analysis.

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## 2. Introduction

Improving sCO<sub>2</sub> cycle performance always remains an interesting topic for researchers, even further revamped in recent years. In these cycles, maintaining the compressor inlet condition near the CO<sub>2</sub> critical condition is essential to benefit from the low compression efficiency. Several studies discussed the cycle configurations and proposed new schemes, while others attempted to evaluate the cycle performance by alternative working fluids. Utilizing sCO<sub>2</sub>-based mixtures as a working fluid increases the degree of freedom and makes the possibility of adjusting the critical point of CO<sub>2</sub> by adding various fluids. The magnitude of decrease or increase of the critical point depends on the mixture composition and properties of the added components. The desired mixture, with a modified critical point, manipulates the restriction of low heat rejection temperatures and the power cycle can be extended to higher heat rejection temperatures, which contributes to higher efficiency [1], while allowing transcritical cycles with condensation in the medium and high-temperature climatic areas. Moreover, the new working fluid mixtures could bring new flammability and toxicity level with different environmental impacts, costs, and operational safety concerns, which should be considered in the overall evaluation [2]. Also, the prediction of the solubility and thermal stability of fluids are factors largely discussed in the literature [3] [4] and it is worth mentioning them, anyway, they are not detailed in this paper.

The studies related to CO<sub>2</sub>-based mixtures are listed in Table 1, where researchers adopted several gas mixtures as working fluids candidates in the sCO<sub>2</sub> cycles, in which CO<sub>2</sub> is mixed with other gases. The majority of the studies are referred to the binary mixture of CO<sub>2</sub> and noble gases. Several studies investigated the binary mixtures of CO<sub>2</sub> with hydrocarbons, and some are related to performing analysis on zeotropic and azeotropic mixtures.

Due to the crucial role of the intermolecular forces under supercritical conditions, a real gas model is required to estimate the properties of either the pure fluids or the mixture. Therefore, according to the conditions and the components of the fluid mixture, the most appropriate EoS should be chosen. As listed in Table 1, several EoS and database types are investigated in the literature for the fluid property estimation to be used for the design and performance analysis of CO<sub>2</sub>-based supercritical cycles and mixtures. The EoS can be classified into four categories: Cubic-based equations, Virial-based equations, Helmholtz function, and the Statistical Associating Fluid Theory (SAFT). Based on the literature, other types of EoS are out of discussion for the sCO<sub>2</sub>-related case studies.

**Table 1 – Literature review of working fluids and thermodynamic references used for CO<sub>2</sub> power cycle analysis**

Author and Year	Fluid and Mixture type	Reference Models /software
Maczek et al., 1997 [5]	CO <sub>2</sub> -R32, R134a	REFPROP V5.0
Kim et al., 2002 [6]	CO <sub>2</sub> -R134a CO <sub>2</sub> -R290	REFPROP V6.0
Sarkar et al. 2009 [7]	CO <sub>2</sub> -R600 CO <sub>2</sub> -R600a	REFPROP CO2PROP [8]
Wright et al., 2011 [9]	CO <sub>2</sub> -SF <sub>6</sub> , CO <sub>2</sub> -Butane	REFPROP V9.0
Wright, et al., 2011 [1]	Pure CO <sub>2</sub> , Two-phase CO <sub>2</sub>	REFPROP V8.0
Lewis et al., 2011 [10]	SF <sub>6</sub> - CO <sub>2</sub> , C4- CO <sub>2</sub>	REFPROP, PR
Jeong et al., 2011 [11]	CO <sub>2</sub> + (H <sub>2</sub> , N <sub>2</sub> , O <sub>2</sub> , He, Ar, Kr,)	REFPROP V8.0
Conboy et al., 2012 [12]	CO <sub>2</sub> -He, CO <sub>2</sub> -Ne, CO <sub>2</sub> -CH <sub>4</sub> CO <sub>2</sub> -nC <sub>4</sub> , CO <sub>2</sub> -SF <sub>6</sub>	REFPROP V9.0
Jeong et al., 2013 [13]	CO <sub>2</sub> -H <sub>2</sub> S, CO <sub>2</sub> -cyclohexane	REFPROP V8.0

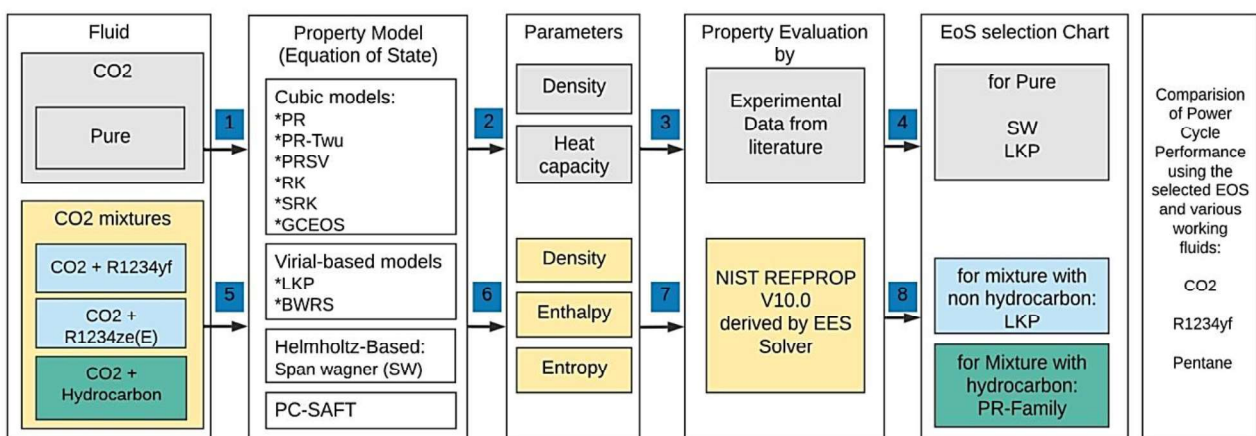
<b>Yin et al., 2013 [14]</b>	CO <sub>2</sub> -SF <sub>6</sub>	REFPROP V8.0
<b>NETL guideline 2014 [15]</b>	-	LK-PLOCK
<b>Hakkaki-Fard et al., 2014 &amp; 2015 [16] [17]</b>	zeotropic mixture R32-CO <sub>2</sub>	REFPROP V9.0
<b>Hu et al., 2015 [18]</b>	CO <sub>2</sub> -Ar, CO <sub>2</sub> -O <sub>2</sub> , CO <sub>2</sub> -He, CO <sub>2</sub> -Xe, CO <sub>2</sub> -Kr, CO <sub>2</sub> -Butane, CO <sub>2</sub> - cyclohexane	REFPROP V9.0
<b>Mecheri et al. 2016 [19]</b>	CO <sub>2</sub>	REFPROP, PENG-ROB PR-BM (PR- Boston Mathias), RK-SOAVE, SRK (Redlich- Kwong-Soave) BWRS (Benedict-Webb-Rubin- Starling) LK-PLOCK (Lee-Kesler-Plocker)
<b>Weiland et al., 2016 [20]</b>	CO <sub>2</sub> -HCL-NH <sub>3</sub>	Peng-Robinson-Boston-Mathias (PR-BM) in Aspen Plus
<b>Vesely et al., 2016 [21]</b>	CO <sub>2</sub> -He, CO <sub>2</sub> -CO, CO <sub>2</sub> -O <sub>2</sub> CO <sub>2</sub> -N <sub>2</sub> , CO <sub>2</sub> -Ar, CO <sub>2</sub> -Xe	REFPROP V9.1
<b>Manikantachari et al. 2017 [22]</b>	CO <sub>2</sub>	RK, SRK, PRS, REFPROP V7.0
<b>Ma et al., 2018 [23]</b>	CO <sub>2</sub> -Kr	REFPROP V9.0
<b>Manikantachari et al., 2018 [22]</b>	CH <sub>4</sub> -O <sub>2</sub> -CO <sub>2</sub> , H <sub>2</sub> -O <sub>2</sub> -CO <sub>2</sub>	SRK in CHEMKIN-RG Exp. (Ignition Delay Times)
<b>Baik et al., 2018 [24]</b>	SF <sub>6</sub> -CO <sub>2</sub> , CO <sub>2</sub> -R123, CO <sub>2</sub> -R134a CO <sub>2</sub> -R32, CO <sub>2</sub> -R22	REFPROP Exp.
<b>White et al., 2018 [25]</b>	CO <sub>2</sub> -H <sub>2</sub> O	REFPROP (2007), PR-BM, LK-PLOCK PC-SAFT, BWRS, BWRS-LS SRK, SR-POLAR, GRAYSON
<b>Guo et al., 2019 [26]</b>	CO <sub>2</sub> -Xenon, CO <sub>2</sub> -Butane	REFPROP
<b>Vesely et al., 2019 [27]</b>	CO <sub>2</sub> -He, CO <sub>2</sub> -CO, CO <sub>2</sub> -O <sub>2</sub> , CO <sub>2</sub> -N <sub>2</sub> , CO <sub>2</sub> -Ar, CO <sub>2</sub> -C1, CO <sub>2</sub> -H <sub>2</sub> S	REFPROP V9.1 & COOLPROP in PYTHON TREND 2.0 [28]
<b>Liu et al., 2019 [29]</b>	CO <sub>2</sub> -cyclohexane, CO <sub>2</sub> -butane, CO <sub>2</sub> -isobutane, CO <sub>2</sub> -propane, CO <sub>2</sub> - H <sub>2</sub> S	LK-PLOCK property Aspen Plus (2010)
<b>Manzolini, Invernizzi et al., 2019 [30]</b>	CO <sub>2</sub> -N <sub>2</sub> O <sub>4</sub> , CO <sub>2</sub> -TiCl <sub>4</sub>	REFPROP, Peng-Robinson EOS
<b>Yu et al., 2020 [31]</b>	CO <sub>2</sub> -Xe, CO <sub>2</sub> -Kr, CO <sub>2</sub> -O <sub>2</sub> , CO <sub>2</sub> -Ar, CO <sub>2</sub> -N <sub>2</sub> , CO <sub>2</sub> -Ne, CO <sub>2</sub> -He	REFPROP V10.0, MATLAB
<b>Barak et al., 2020 [32]</b>	CH <sub>4</sub> -O <sub>2</sub> -CO <sub>2</sub> -N <sub>2</sub>	Exp. (Ignition Delay Times)
<b>Saengsikhiao et al., 2020 [33]</b>	Azeotropic Mixtures: R463A (R32-R125-R134a-R1234yf- CO <sub>2</sub> ) R445A (R1234z3-R134-CO <sub>2</sub> ) R455A (R1234yf-R32-CO <sub>2</sub> )	REFPROP CYLCE_D-HX [34]
<b>Bonalumi, Lasala, Macchi, 2020 [35]</b>	CO <sub>2</sub> -TiCl <sub>4</sub>	Peng-Robinson EOS

On the other hand, one of the most common databases used by the NIST database [36] is REFPROP, which provides the fluid's properties based on either the related experimental data or the proven models from the literature. Most of these experimental data belong to pure fluids, like the one for pure CO<sub>2</sub> derived from the research of Span Wagner [37]. As listed in Table 1, several studies on the sCO<sub>2</sub> power cycles are carried out basing on this database, with different versions during the

years. In the prediction of mixtures property, the REFPROP performance depends on the availability of specific models and experimental data for the required binary or multi-component mixtures, which are incorporated within the database. In some cases, due to the temperature limits, computations fail for property predictions by the database [25]. Other databases are COOLPROP [38], an open-source program able to determine the property of pure and pseudo-pure fluids; CO2PROP, which is a subroutine, developed based on Helmholtz free energy function and AIChE's "DIPPR 801", which is a source of critically evaluated thermophysical properties by American Institute of Chemical Engineers (AIChE) [39]. There is also a generated data developed by Aspen Technology based on the most well-known EoS widely used in the literature. National Energy Technology Laboratory (NETL) already evaluated the data available on the Aspen properties database, including NIST REFPROP, Peng-Robinson (PR) variants [40], PR-Twu [41], PR-BM (PR-Boston Mathias) [42], RK (Redlich-Kwong) [43], SRK (Redlich-Kwong-Soave) [44], BWRS (Benedict-Webb-Rubin-Starling) [45], and LKP (Lee-Kesler-Plocker) [46]. Both PR variants and LKP have the best prediction near the critical point compared to REFPROP, while the LKP has superior performance at high pressure and temperature. The LKP is also recommended by the NETL, due to higher consistency in the critical region [15].

The software packages are Honeywell UniSim Design [47] [48], DWSIM [49], Aspen HYSYS [50], and similar solvers that, in some cases, introduce some improvements and modifications of the basic EoS when treating mixtures. These modifications are mainly related to the mixing rules, binary interactions, and solubility. The various numerical solvers provide only marginally different results even for pure fluids [19].

Most of the case studies discussed in the literature are related to specific thermodynamic applications rather than analytic thermodynamic property evaluation. Their focus is on power cycles, alternative configurations, and various applications. In most of those, the new mixtures are limited to the extraction of data from the common database. As shown in Figure 1, the present study fills in the thermodynamic evaluation gap and provides a cross-check between the available models and experimental data for the pure CO<sub>2</sub> and CO<sub>2</sub>-based mixtures (blank box).



**Figure 1 – Research outline for property model evaluation**

### 3. Methods and implementation

#### 3.1. Pure CO<sub>2</sub>

##### Available experimental data and Gaps regarding pure CO<sub>2</sub>

In order to provide a reliable power cycle simulation, using accurate working fluid's thermodynamics properties is fundamental. Since the 1950s, increasingly accurate experiments have been conducted for pure CO<sub>2</sub> properties. In this work, to verify the reliability of calculation models and equations of state, more than 880 experimental measurements of density and specific heat capacity of pure CO<sub>2</sub> are collected from the literature. Among all the available publications, only the experimental data included in a temperature and pressure range of 303-615 K and 7-35.5 MPa, respectively, were selected because typical of sCO<sub>2</sub> geothermal power plants. The references used for pure CO<sub>2</sub> are shown in Table 2 and Table 3.

*Table 2 – Literature references on experimental measurements of the density of pure CO<sub>2</sub>*

Reference for CO <sub>2</sub>	Year	T range (K)	P range (MPa)	N° points
Kennedy [51]	1954	313.15 - 615	7.50 - 35.00	176
Langenfeld et al. [52]	1992	313.15 - 423.15	8.21 - 29.90	17
Knetz [53]	1995	333.15 - 373.15	10.00 - 30.00	28
Fenghour et al. [54]	1995	330 - 613	7.2 - 34	29
Seitz [55]	1996	323.15 - 573.15	9.94 - 29.93	17
Pohler and Kiran [56]	1996	323.00 - 423.00	15.46 - 30.78	27
Van der Gulik [57]	1997	303.05	7.23 - 35.31	33
Tomoya Tsuji et al [58]	1998	304, 310, 320	7 - 10	67
Ferri et al. [59]	2004	353.20 - 393.20	16.00 - 30.00	17
Garmroodi et al. [60]	2004	308.00 - 348.00	12.20 - 35.50	40
Skerget et al. [61]	2005	313.20 - 353.20	7.83 - 30.37	55
Pečar and Doleček [62]	2007	308.15 - 333.15	10.00 - 35.00	10
Liu et al. [63]	2007	320, 355, 369	13 - 34	8
Pensado et al. [64]	2008	303 - 353	10 - 35	57
Mantilla et al. [65]	2010	310 - 450	10 - 35	26
Laura Gil [66]	2010	304.21 - 308.15	7.01 - 20	103
Kodama et al. [67]	2013	313.15	7 - 10	4

*Table 3 – Literature references on experimental measurements of the specific heat of pure CO<sub>2</sub>*

Reference for CO <sub>2</sub>	Year	T range (K)	P range (Mpa)	N° points
Lowell [68]	1960	304 - 322	7.2 - 8.7	38
Dordain And Coxam [69]	1995	327 - 416	7.3 - 25.8	100
Ishmael [70]	2016	333 - 423	10 - 30	28

### 3.2. CO<sub>2</sub>-based mixtures

#### Correlation of thermodynamic models with VLE data

Typically, to define the Binary Interaction Parameters (BIP) of a mixture, the VLE points are used as data regression. The Nishiumi et al. [71] binary interaction coefficients are used in the present study (Table 4), which are also of the UniSim library. The PR-mod is a modified Peng-Robinson version, with the coefficients suggested by UniSim, available only for CO<sub>2</sub>+HC. The coefficients of Helmholtz type equations are those implemented in REFPROP 10.0 version. The charts below show the equilibrium points obtained from experimental campaigns on the VLE, already existing in literature for the selected mixtures, compared to those estimated with the most promising EoS, chosen from the ones previously tested for pure CO<sub>2</sub>. For this study, the potential of UniSim and DWSIM is exploited. Similarly, by using REFPROP 10.0 libraries [36] through EES (Engineering Equation Solver) [72] the accuracy of the models implemented in the program was estimated. In Table 5, the publications of the VLE experimental measurements used in the present study are reported.

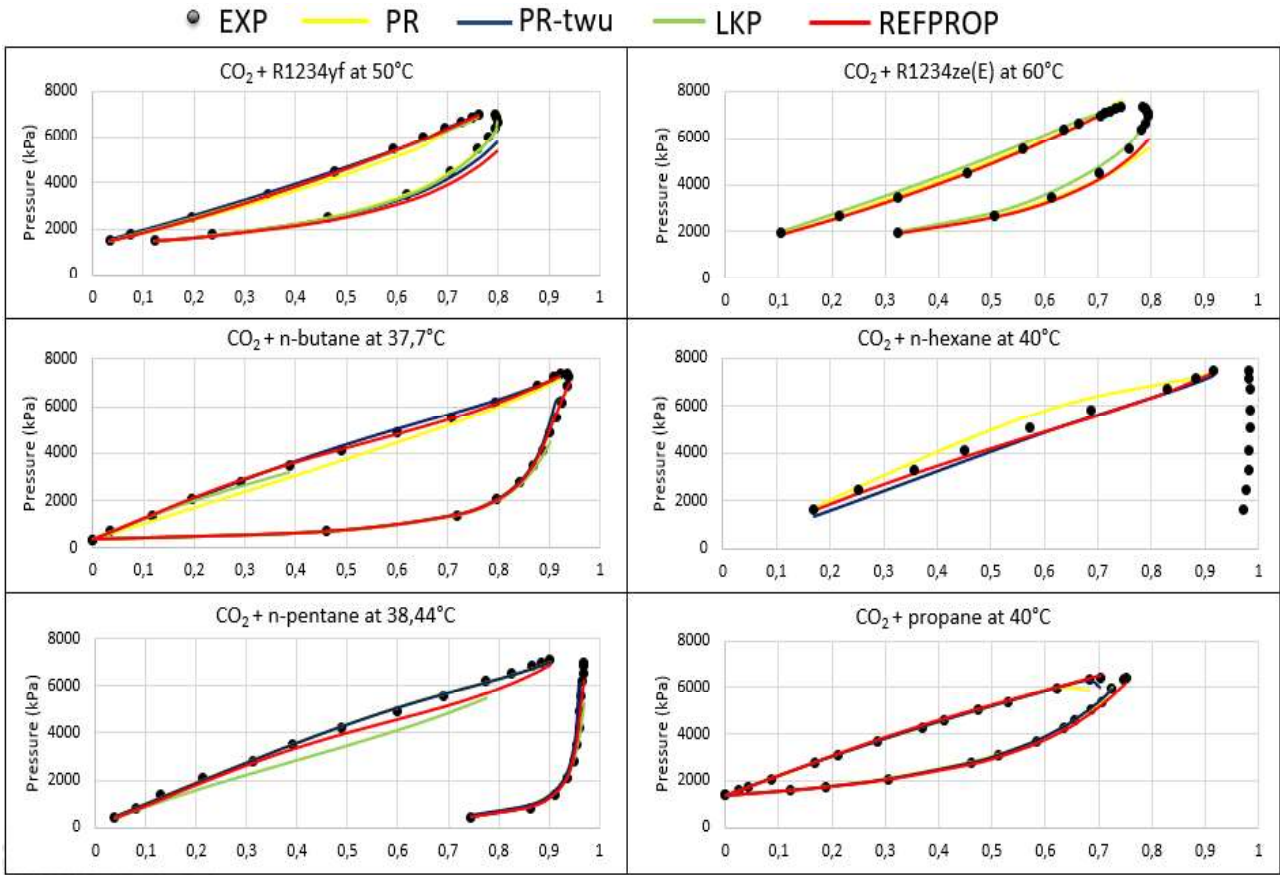
*Table 4 – Binary Interaction Parameters of the selected mixtures for each EoS [71]*

	PR	PR mod	PR-Twu	LKP	GCEOS
CO <sub>2</sub> + R1234yf	0.1113	-	0.101	0	-
CO <sub>2</sub> + R1234ze(E)	0.11129	-	0.101	0	-
CO <sub>2</sub> + n-butane	0.1298	0.06374	0.1298	0.9456	0.13
CO <sub>2</sub> + n-hexane	0.125	0.04971	0.125	1.0196	0.125
CO <sub>2</sub> + n-pentane	0.125	0.05672	0.125	0.9833	0.125
CO <sub>2</sub> + propane	0.135	0.07075	0.135	0.9211	0.135

*Table 5 – CO<sub>2</sub>-based mixtures and VLE references*

Fluids	VLE reference
CO <sub>2</sub> + R1234yf	Juntarachat et al. [73] G. Di Nicola et al. [74]
CO <sub>2</sub> + R1234ze(E)	Juntarachat et al. [73]
CO <sub>2</sub> + n-butane	Shlbata et al. [75]
CO <sub>2</sub> + n-hexane	Ying-Hsiao Li et al. [76]
CO <sub>2</sub> + n-pentane	Huazhe Cheng et al. [77]
CO <sub>2</sub> + propane	Ju Hyok-Kim et al. [78] J. C. Acosta [79]





**Figure 2 – VLE isotherms for carbon dioxide-based mixtures from the models, compared with the experimental data shown in Table 5**

The comparison, shown in Figure 2, clarifies the models' prediction level compared to the reference of NIST REFPROP. The LKP, imported by DWSIM for the VLE analysis, seems the best for the simulation of the binary equilibrium of CO<sub>2</sub> - refrigerants mixtures. On the other hand, the Peng-Robison EoS demonstrates an acceptable regression of the experimental points for mixtures with hydrocarbons.

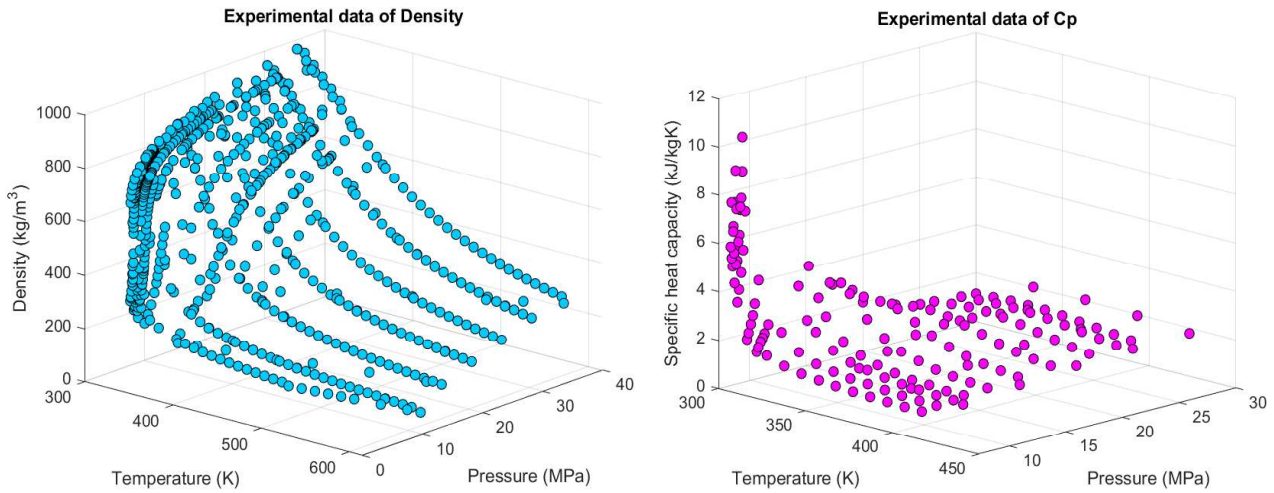
## 4. Results and discussion

### 4.1. Pure CO<sub>2</sub>

The experimental data, reported in Figure 3, were compared with the values of density and specific heat calculated by different EoS, included in the UniSim database. Two dimensionless parameters were adopted to compare the various models: the absolute average deviation (AAD), and the root mean square error (RMSE).

$$AAD = \frac{1}{n} \sum_{i=1}^n \left| \frac{\rho_{exp,i} - \rho_{calc,i}}{\rho_{exp,i}} \right| \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (\rho_{exp,i} - \rho_{calc,i})^2}{n}}$$

Where  $\rho_{calc}$  is the calculated density by EOS,  $\rho_{exp}$  is the experimental density and  $n$  is the number of experimental data.



**Figure 3 - Reference experimental data for density (left) and heat capacity,  $C_p$  (right)**

The results of the comparison are shown in Table 6. It is evident that the use of the Helmholtz-type Span-Wagner equation [37], implemented in the REFPROP software, provides the best matching with the experimental data in the whole range. The related AAD and RMSE of density and  $C_p$  are the lowest compared to the other EoS. In particular, the calculated  $\rho$ -RMSE is more than three times lower than the second-best equation. The SW model implemented in the open-source COOLPROP software was also tested, with very similar results to the REFPROP version. Looking at the equations of state implemented in UniSim software, the LKP seems to provide reasonable accuracy. Alternatively, the DWSIM version of the Lee-Kesler-Plöcker (LKP) EoS was also employed with significant improvements. The GCEOS and PR-family equations are acceptable at a moderate extent, with  $\rho$ -AAD and  $C_p$ -AAD about 3.3% and 7%, respectively. On the contrary, the worst prediction of density in the analyzed region is achieved by the SRK, BWRS, and PC-SAFT equations, with an average deviation of around 10%. According to the present work, the temperature increase contributes to a decrease in the deviation for a fixed pressure. The here achieved results agree with those of other studies [80].

**Table 6 - Comparison of property estimation by EoS compared with REFPROP as the reference**

EOS	Density (AAD)	Density (RMSE)	$C_p$ (AAD)	$C_p$ (RMSE)
PR	3.949%	33.98	6.724%	0.536
PR-Twu	3.348%	30.54	6.916%	0.479
PRSV	3.481%	35.54	7.571%	0.483
LKP	2.544%	24.55	3.584%	0.388
LKP (DWSIM)	1.478%	10.39	2.925%	0.342
SRK	9.878%	74.72	5.789%	0.492
SRK-Twu	11.034%	82.03	5.587%	0.474
BWRS	5.612%	69.43	11.208%	1.069
GCEOS	3.272%	31.06	7.570%	0.483
PC-SAFT	4.810%	49.62	10.513%	1.174
SW (REFPROP)	0.479%	7.11	2.471%	0.227

<b>SW (COOLPROP)</b>	0.471%	7.32	2.472%	0.227
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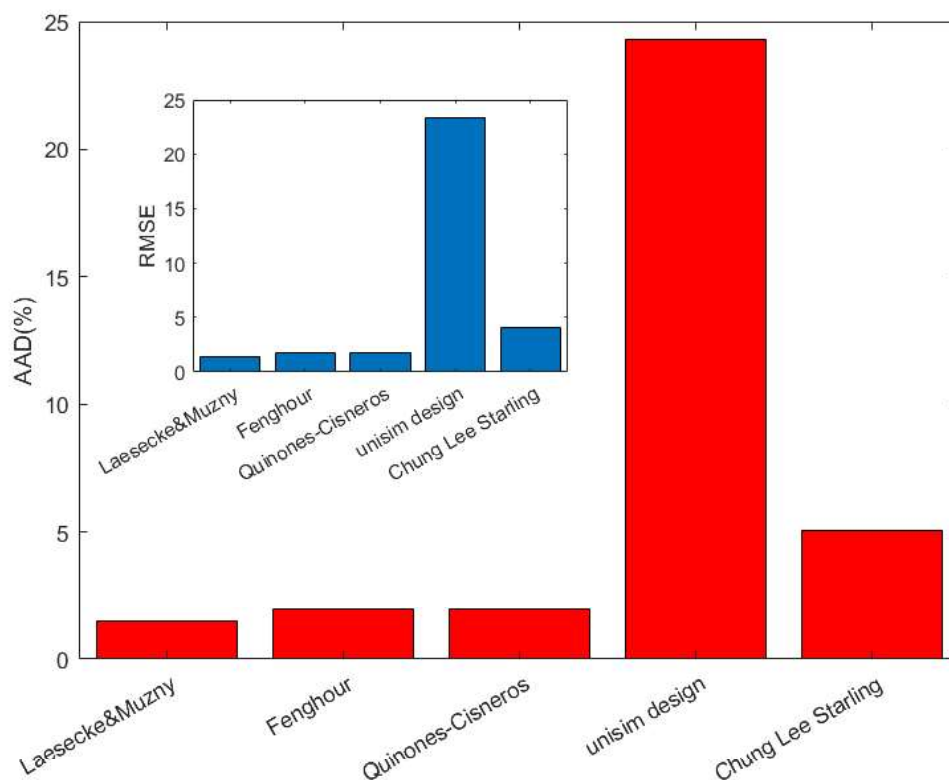
### Analysis of the viscosity model

The viscosity describes a fluid's resistance to flow, and it is one of the most critical transport properties. For this reason, an accurate model for its representation in thermo-fluid dynamic problems is often necessary. The results of available viscosity models are evaluated with related experimental data (Table 7). REFPROP solver comprises Fenghour model [54] and Quinones-Cisneros model [81]; the UniSim solver includes the Chung Lee Starling viscosity model and a dedicated database which is based on external property dataset of DIPPR® 801 [39]. Also, an additional model of Laesecke and Muzny [82] out of those solvers is taken into account for the viscosity evaluation. These models are independent of the EoS.

*Table 7 – Available references for the viscosity of pure CO<sub>2</sub>*

Reference for CO <sub>2</sub>	Year	T range (K)	P range (MPa)	N°points
<b>Van Der Gulik [57]</b>	1997	308.15	8.61 - 35.50	16
<b>Liu et al. [83]</b>	2007	320 - 355 - 369	13 - 34	8
<b>Pensado [64]</b>	2008	303 - 353	10 - 60	32

The results of the comparison are shown in Figure 4. Among the selected models, Laesecke and Muzny Model [82] gives the best result. Also, both the Fenghour and Quinones models give accurate predictions with AAD of about 1%, and both are available as REFPROP sub-model for the viscosity. The Chung Lee Starling model is the next-ranked model, which is also available in the UniSim solver. The internal database of UniSim design gives the worst performance compared to experimental data, with an absolute error higher than 24%.



**Figure 4 – Comparison of viscosity achieved by the EoS implemented on different models and software packages**

## 4.2. CO<sub>2</sub>-based mixture

### EoS comparison with REFPROP

There are no available experimental data of density, nor other thermodynamic properties, of the selected CO<sub>2</sub>-based mixtures from the literature. A comparison with REFPROP data was determined to validate the results of the different EoS for each blend. Considering that the present study aims to evaluate CO<sub>2</sub>-based binary fluids, the upper concentration of the second component was limited at 40%. Table 8 shows the pressure and temperature ranges for which the analysis of the mixtures was carried out. The equations inside the open-source software COOLPROP were also included in comparison with REFPROP. The Fluids R1234yf and R1234ze(E) are not included in the UniSim library; therefore, it was necessary to import the properties of the fluid from the external module of DWSIM and to set up manually the critical properties (Table 9).

**Table 8 – Temperature and Pressure ranges selected for thermodynamic analysis of mixtures of CO<sub>2</sub> and the following fluids**

	R1234yf	R1234ze(E)	n-butane	n-pentane	n-hexane	propane
<b>T range (°C)</b>	30 - 240	30 - 240	30 - 240	30 - 240	30 - 240	30 - 240
<b>P range (MPa)</b>	3 - 30	3 - 30	1 - 20	0.6 - 20	0.6 - 20	1 - 20

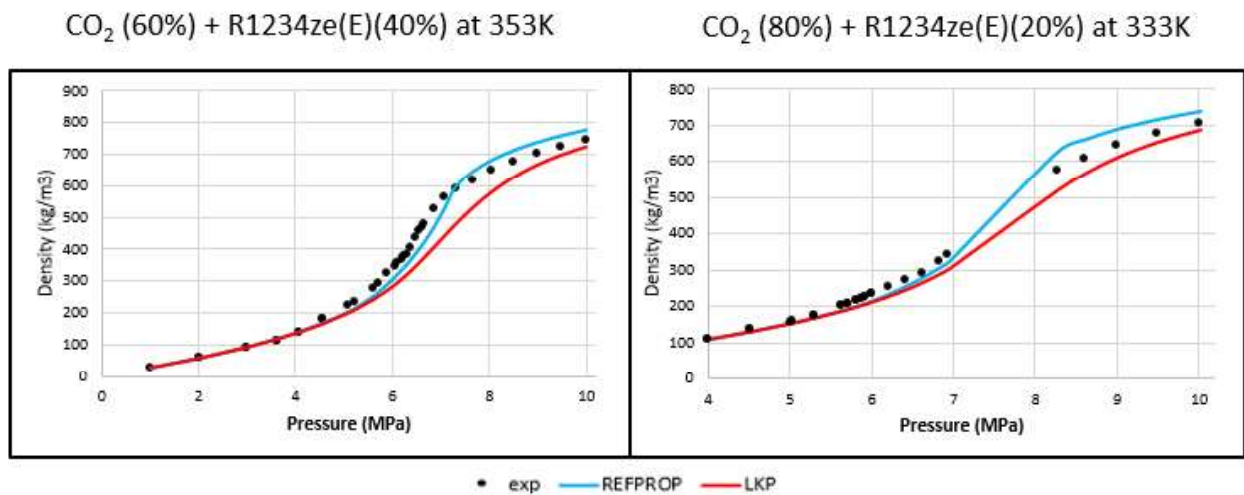
**Table 9 – Basic and critical properties of fluids that are necessary to set up in UniSim [36], [38]**

Fluid	T <sub>c</sub> (°C)	P <sub>c</sub> (kPa)	Ideal Liq. Density (kg/m <sup>3</sup> )	Critical Volume (m <sup>3</sup> /kmol)	MM (kg/kmol)	NBP (°C)	Acentricity (-)
<b>R1234yf</b>	94.7	3382	1100	0.2398	114.04	-30	0.2760
<b>R1234ze(E)</b>	109	3636	1293	0.2331	114.04	-19	0.3131

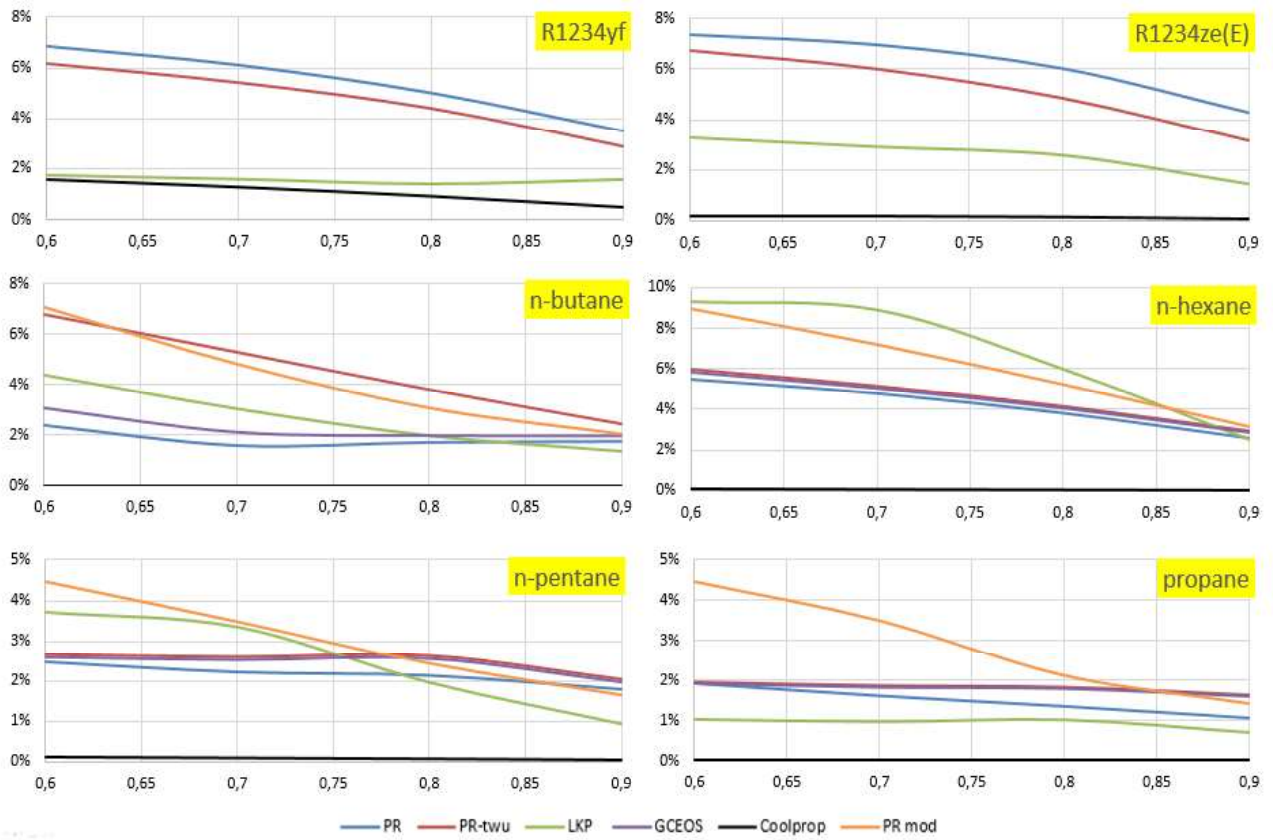
The thermodynamic properties tested for this comparison were the density, enthalpy, and entropy difference. Figures 6, 7, and 8 report the calculated average absolute error of each EoS tested for the y-axis and the variation of the molar concentration of CO<sub>2</sub> for the x-axis. Generally, the AAD referred to the REFPROP database is about 5-6% for the three selected properties, with some peaks over 10%. The behaviour of the curves for enthalpy and entropy is very similar, while there are more significant differences with the density.

For refrigerants, the Lee-Kesler-Plöcker equation allows for density errors of less than 2% for R1234yf and less than 4% for R1234ze (E). The error for  $\Delta H$  and  $\Delta S$  is higher but never exceeds 6% compared to Peng-Robinson and PR-Twu. Although there are limited references for the evaluation of the results, the experimental data of the mixture of CO<sub>2</sub>-R1234ze(E) in supercritical conditions at 333K and 353K [84] are considered, and the accuracy of LKP and REFPROP has been verified in Figure 7. The Twu modification of PR is recommended by the UniSim software manual [85] because its  $\alpha$ -function has an exponential term that provides smooth transition through the critical conditions; therefore, they are more practical for process simulation.

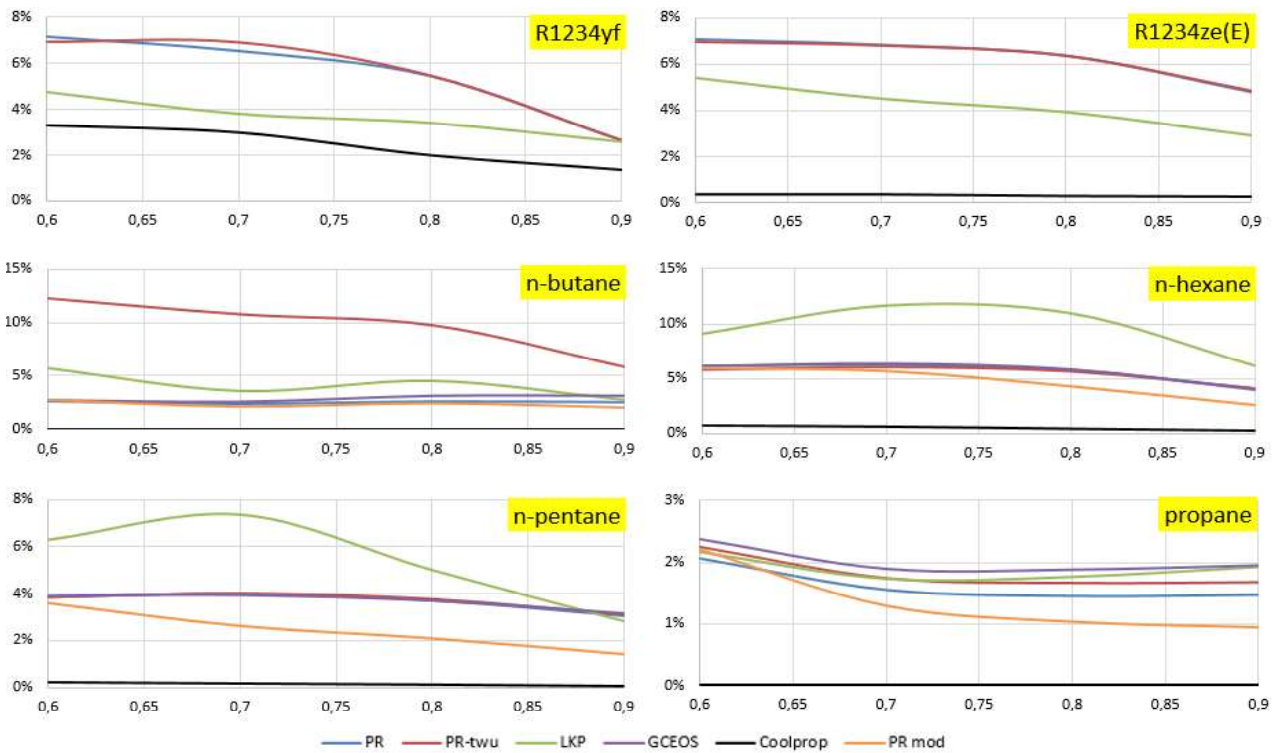
For hydrocarbons, the PR family proves to be the most effective and reliable one. The PR is the equation that is widely used to predict the thermodynamic properties of pure hydrocarbons. In principle, PR-Two gives similar results compared to simple PR except for the mixture with n-butane. The best performance of PR is for the mixture of n-butane and propane with the lowest errors. Therefore,  $\rho$ -AAD,  $\Delta H$ -AAD, and  $\Delta S$ -AAD are consistently under 3% in the molar content range. The worst performance of PR is for n-hexane with a  $\rho$ -AAD of around 4%,  $\Delta H$ -AAD, and  $\Delta S$ -AAD around 5%. The corrective coefficients proposed by UniSim show an improvement in the results of  $\Delta H$ -AAD and  $\Delta S$ -AAD, especially for n-pentane and propane, but also an increase of the density deviation with the decrease of the CO<sub>2</sub> concentration in the mixture. Therefore, it may be interesting to consider a compromise between the two versions of PR depending on the molar concentration of carbon dioxide for each blend. The molecular weights of propane and carbon dioxide are 44.09 g/mol and 44.01 g/mol, respectively. Therefore, the performance of LKP, as a virial-type EoS, for the case study of propane-blend is because of the similarity of mixture components molecules. Finally, the results obtained with COOLPROP deserve consideration, showing the reliability of this open-source database.



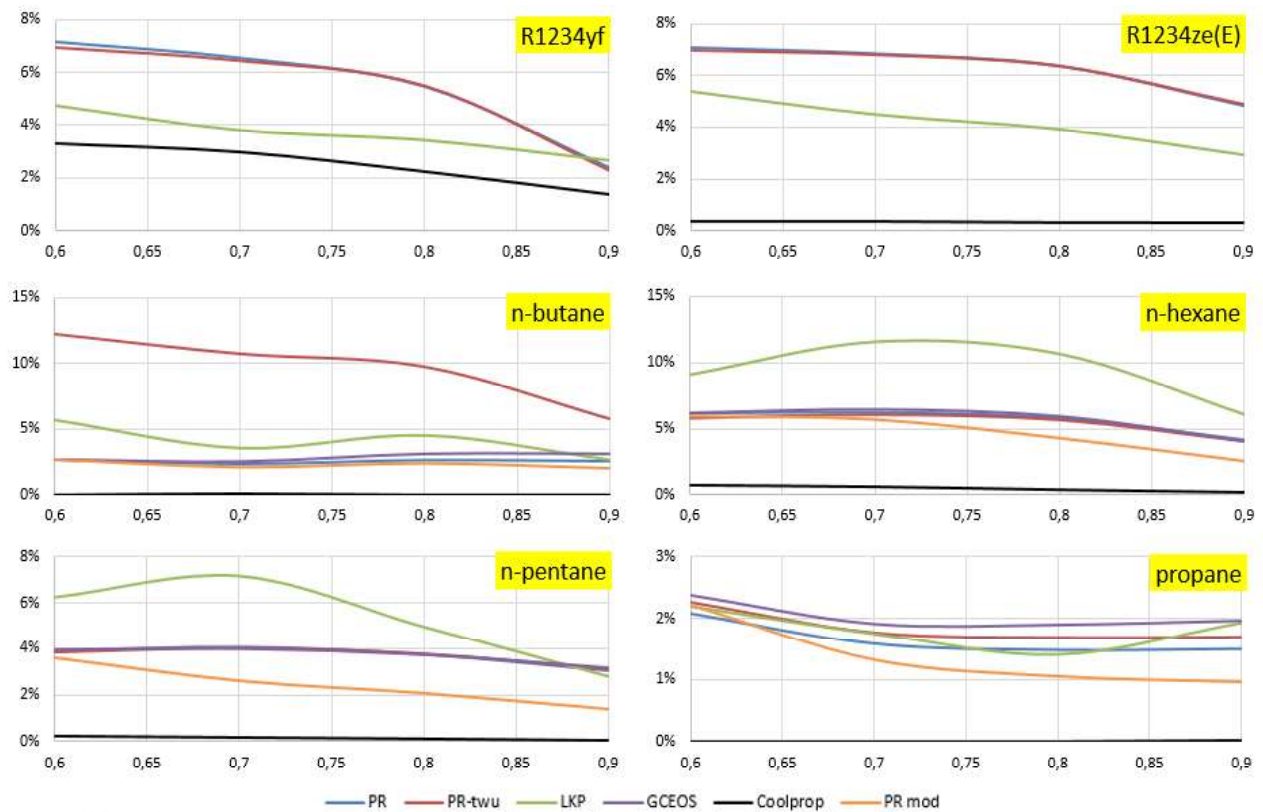
**Figure 5 – The LKP and REFPROP accuracy to fit the supercritical experimental data [84] of CO<sub>2</sub> and R1234ze(E) mixture**



**Figure 6 – AAD of density comparing EoS and REFPROP model with the variation of the molar concentration of CO<sub>2</sub> in the mixture**



**Figure 7 – AAD of the enthalpy difference comparing EoS and REFPROP model with the variation of the molar concentration of CO<sub>2</sub> in the mixture**

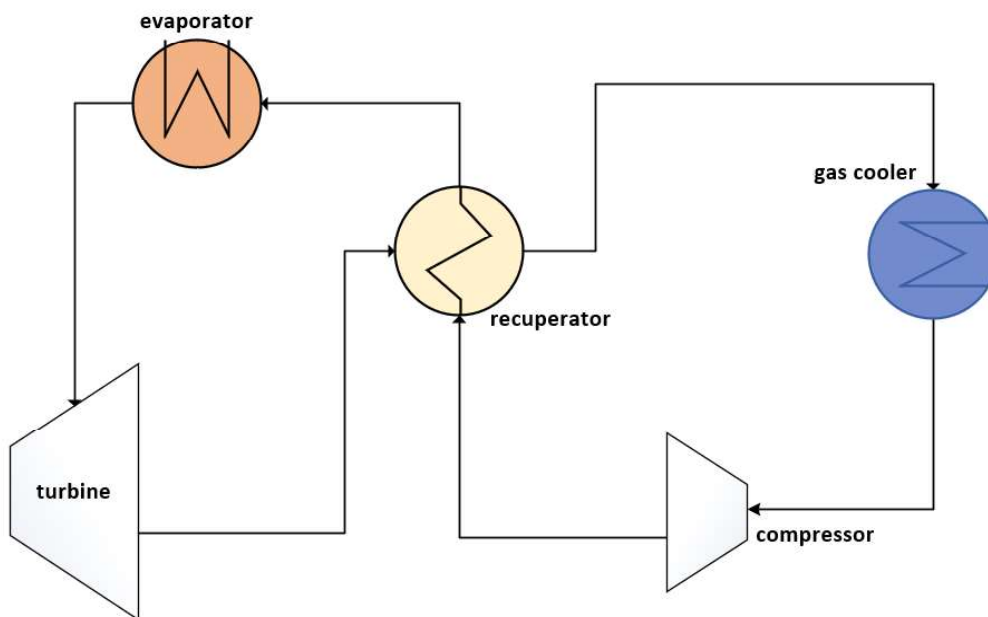


**Figure 8 – AAD of the entropy difference comparing EoS and REFPROP model with the variation of the molar concentration of CO<sub>2</sub> in the mixture**

## 5. The power cycle

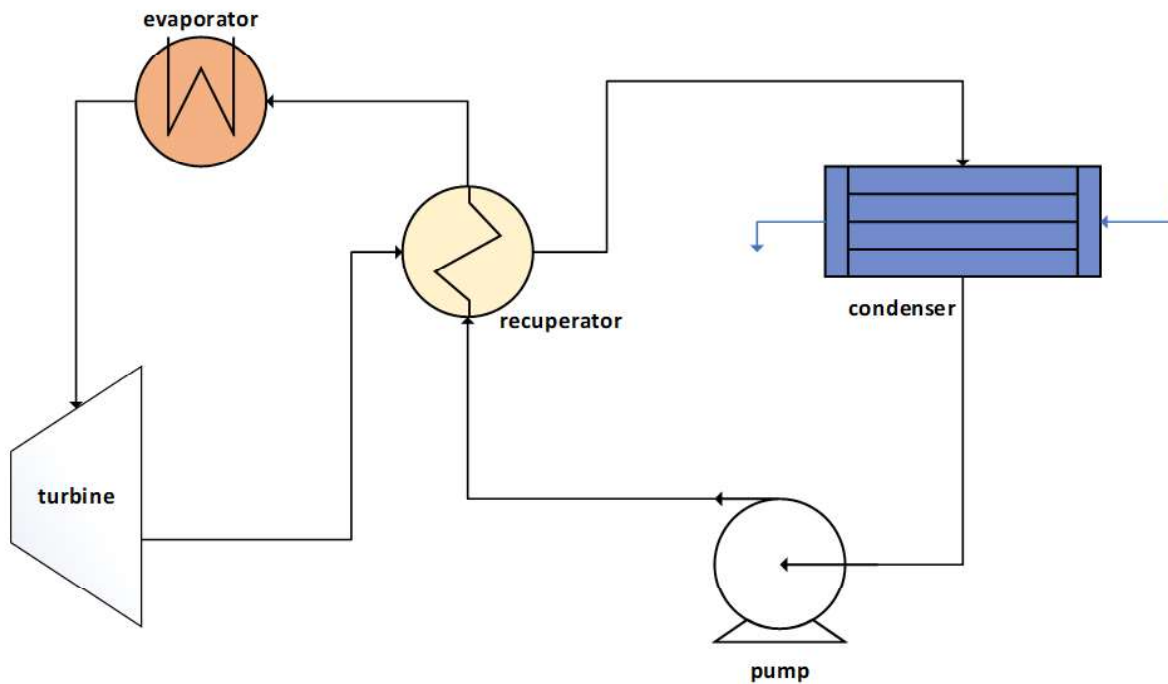
As previously discussed, using sCO<sub>2</sub>-based mixtures as a working fluid increases the degrees of freedom and makes possible the modification of the critical point of CO<sub>2</sub> by adding various fluids and manipulating the constraint of low heat rejection temperatures. So, the power cycle can be extended to higher heat rejection temperatures with the possibility of realizing a transcritical cycle configuration, which contributes to higher efficiency. Moreover, the new working fluid mixtures could lead to reducing the maximum pressure of the cycle with different equipment costs and operational safety concerns. The main objective of this chapter is to investigate the influence on the accuracy of the results of the different discussed EoS when applied to the analysis of power cycles working with CO<sub>2</sub> based mixtures. Such a comprehensive analysis is very useful to the designers and researchers of energy systems to address the uncertainty of thermodynamic cycles results when working with novel mixtures, not currently available in literature so far.

The layouts of the power cycle simulated with pure CO<sub>2</sub> and with the selected blends are shown in Figures 9 and 10, respectively. The first is a supercritical Brayton power cycle with recuperation; the second is a recuperative closed-loop Rankine cycle. The working fluid is indirectly heated by a low–medium temperature hot source (e.g. solar, geothermal, waste heat, biomass, etc.) through a heat exchanger up to 230°C. The fluid at the output of the cold side of the recuperator is then cooled down to 30°C, corresponding to the value at the compressor inlet or pump inlet. For a mixture, differently from a pure fluid, in the case of the transcritical cycle, it is not possible to set a defined pinch point because of the non-isothermobaric condensation line. Therefore, to avoid a large heat transfer area, a control function of the minimum temperature difference of each heat exchanger was implemented. The temperature limit at the condenser and recuperator pinch point was assumed within the range of 5°C to 10°C. Also, the approach point at the evaporator was assumed as 10°C. Finally, the adiabatic efficiency of the pump and the turbine was taken equal to 90%. The simulations have been carried out in an EES environment using the procedure to access the REFPROP database, furthermore, the energy and mass balances are reported in Appendix A.



*Figure 9 – Supercritical recuperative closed-loop Brayton cycle*





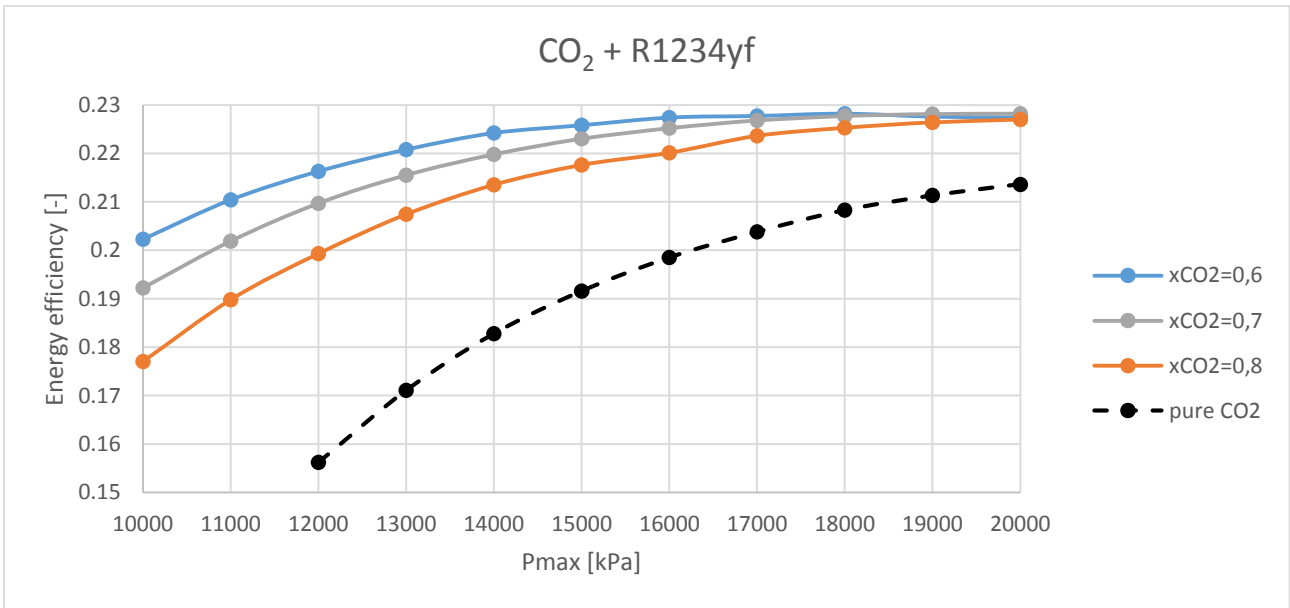
**Figure 10 – Recuperative closed-loop Rankine cycle**

To make a comparison with pure sCO<sub>2</sub>, in terms of thermodynamic performance and energy efficiency of the cycle, the influence of the selected mixture composition and the maximum pressure of the cycle has been investigated.

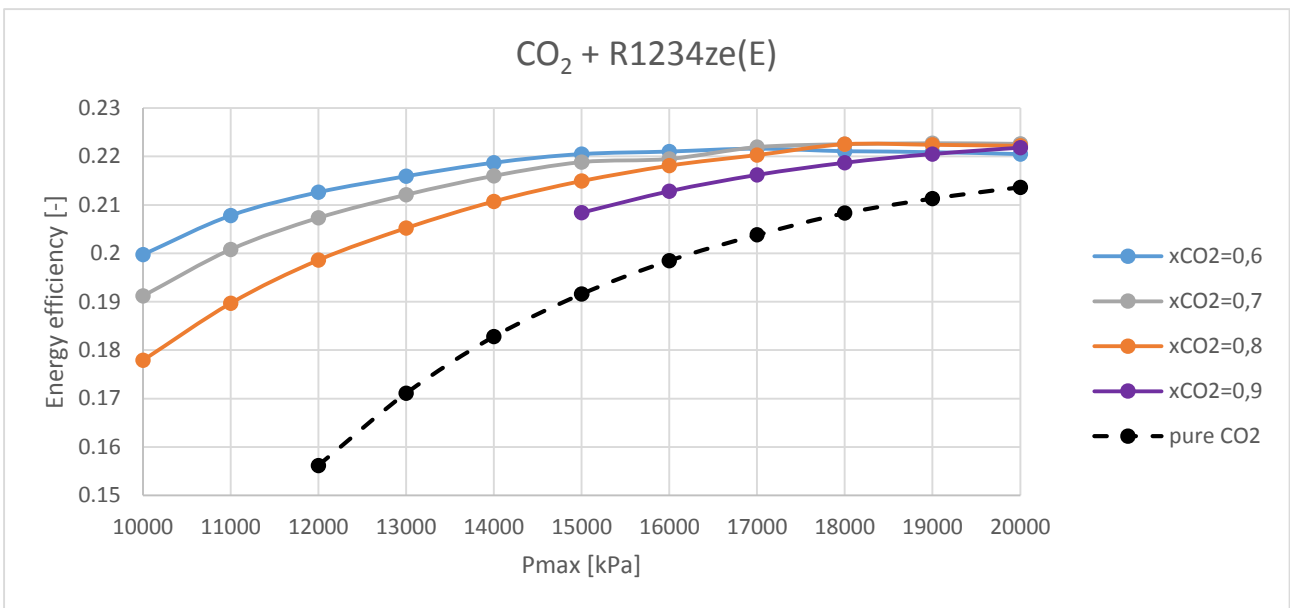
$$\eta = \frac{W_t - W_p}{Q_{in}}$$

With  $W_t$  the work produced by the turbine,  $W_p$  the work absorbed by the pump or the compressor and  $Q_{in}$  the total heat energy input entering the system by the evaporative heat exchanger.

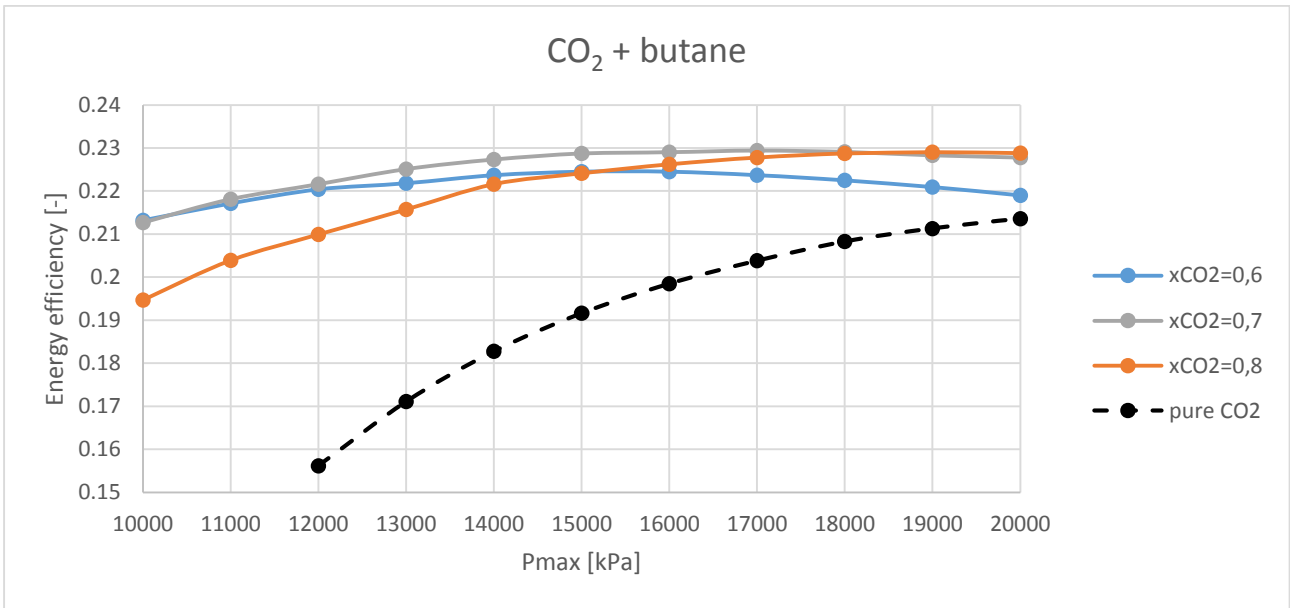
Where possible and respecting the previously defined pinch point of the heat exchangers, the molar fraction of CO<sub>2</sub> has been ranged from 90% to 60%, and the maximum pressure range was set between 200 and 100 bar. The results presented in Figure 11 to Figure 16 highlight the benefits of the new mixtures compared to pure CO<sub>2</sub>, enhancing thermodynamic efficiency up to more than 23%. The efficiency of the power cycle decreases with the reduction of the maximum pressure for most of the fluids, except for the mixture with pentane and hexane, however remaining higher than the sCO<sub>2</sub> cycle efficiency. Moreover, the lower the maximum pressure, the higher the efficiency improvement. In the case of mixing carbon dioxide with R1234yf, R1234ze(E), or propane, the reduction of CO<sub>2</sub> molar concentration allows better performance. On the other hand, the highest efficiency of the cycle mixing carbon dioxide with butane, hexane, and pentane is achieved with a CO<sub>2</sub> molar content of 70%, 80%, and 80%, respectively.



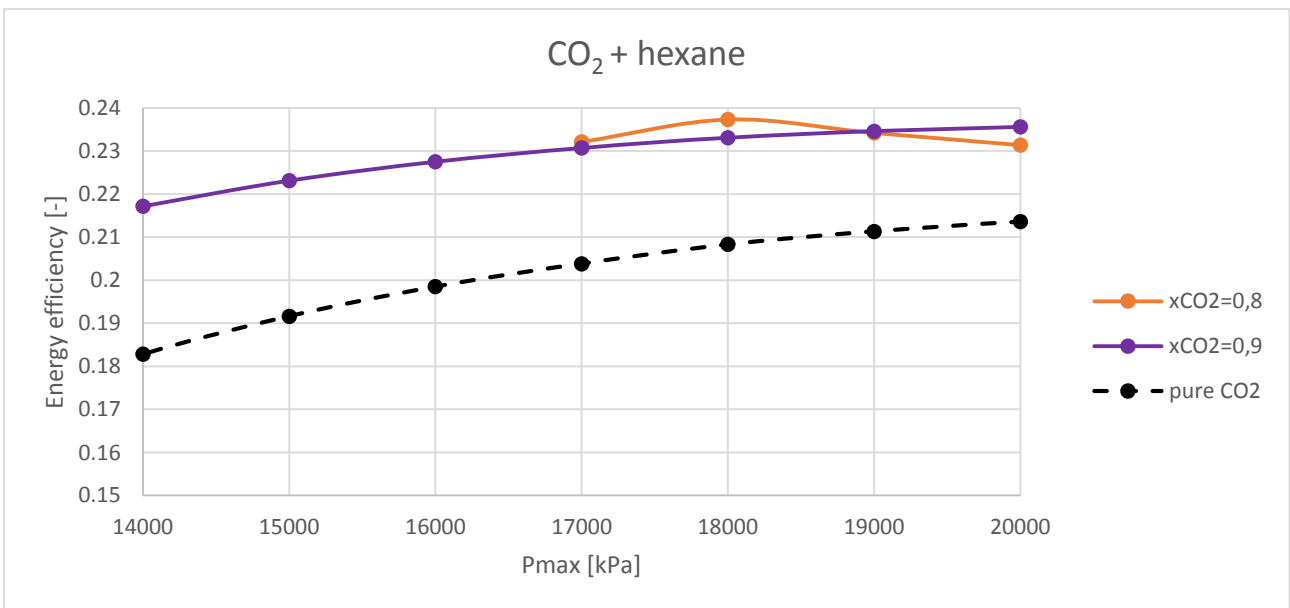
**Figure 11 – Energy efficiency of the power cycle vs. maximum pressure of the cycle, at a variable molar concentration of CO<sub>2</sub> in the mixture, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+R1234yf**



**Figure 12 – Energy efficiency of the power cycle vs. maximum pressure of the cycle, at a variable CO<sub>2</sub> in the mixture, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+R1234ze(E)**



**Figure 13 – Energy efficiency of the power cycle vs. maximum pressure of the cycle, at a variable molar concentration of CO<sub>2</sub>, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+butane**



**Figure 14 – Energy efficiency of the power cycle vs. maximum pressure of the cycle, at a variable molar concentration of CO<sub>2</sub> in the mixture, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+hexane**

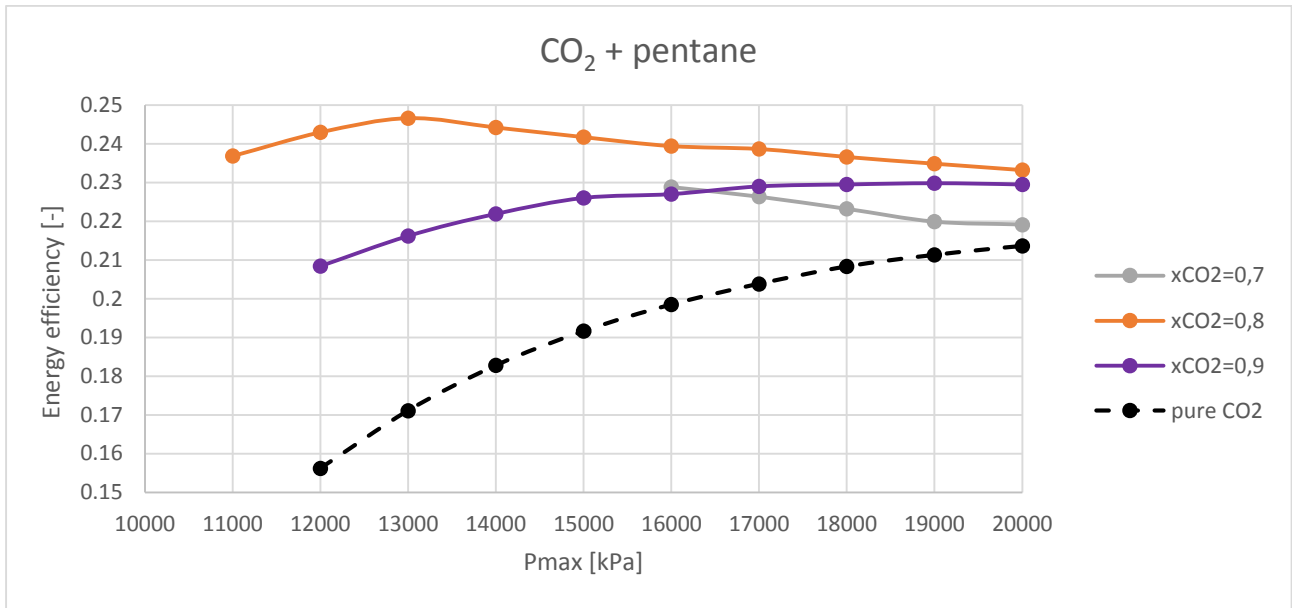


Figure 15 – Energy efficiency of the power cycle vs. maximum pressure of the cycle, at a variable molar concentration of CO<sub>2</sub> in the mixture, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+pentane

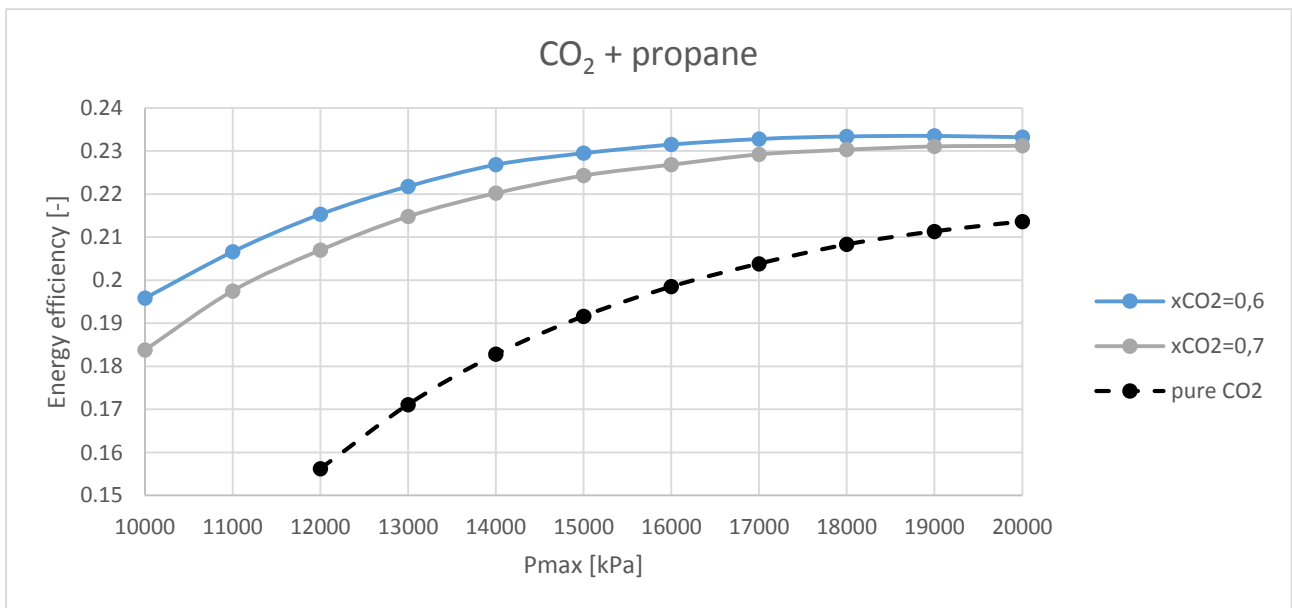


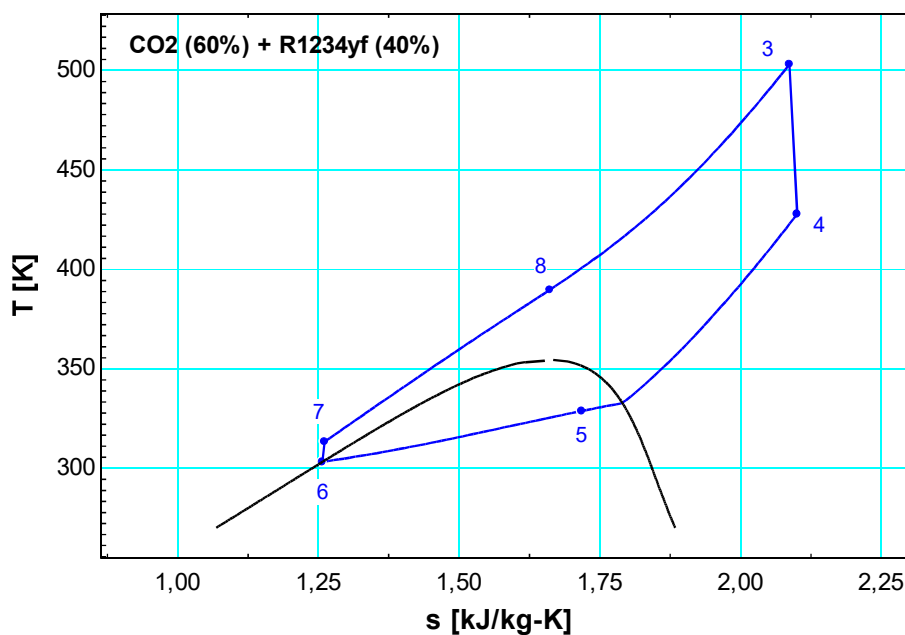
Figure 16 – Energy efficiency of the power cycle vs maximum pressure of the cycle, at a variable molar concentration of CO<sub>2</sub> in the mixture, comparing pure sCO<sub>2</sub> and CO<sub>2</sub>+propane

As above discussed, the deviation of the EoS from the actual fluid physical properties also depends on the fluid state. In a power cycle, the fluid works under different conditions, involving several possible states across the components. The influence of the different EoS in pure CO<sub>2</sub> and CO<sub>2</sub>-based mixtures when working in power cycles has been investigated. For this purpose, among the studied refrigerants and the hydrocarbons, two of the most promising and potential blends were

selected: CO<sub>2</sub>(60%)-R1234yf(40%) and CO<sub>2</sub>(80%)-pentane(20%), for which the relative main thermodynamic properties of the power cycle are collected in Table 10. The T-s diagrams of the related power cycles are shown in Figures 17 and 18: it is worth noting that the prediction of the dew and bubble curves, through the REFPROP saturation functions, is not complete near the critical point; however, it is sufficiently accurate to have effective, reliable representation of the power cycle. The outputs of some selected cycle parameters, obtained with REFPROP, were compared with those from UniSim simulations of the same power cycle. It allowed assessing the influence of the EoS on the results of each cycle key component and the overall performance (Figures 19-20-21).

**Table 10 – Main parameters of CO<sub>2</sub>-based mixtures power cycle.**

Power cycle state points	CO <sub>2</sub> (60%)-R1234yf(40%)			CO <sub>2</sub> (80%)-pentane(20%)		
	T [°C]	P [kPa]	h [kJ/kg]	T [°C]	P [kPa]	h [kJ/kg]
<b>3</b> Turbine inlet	230	14000	594,2	230	13000	659,2
<b>4</b> Turbine Outlet	154,7	3863	540,6	168,4	5089	601,6
<b>5</b> Condenser inlet	55,57	3863	399,6	50,44	5089	335,4
<b>6</b> Condenser Outlet	30	3863	254,3	30	5089	195
<b>7</b> Pump Outlet	40,17	14000	266	37,84	13000	206,8
<b>8</b> Evaporator Inlet	116,6	14000	407	135,8	13000	473
<b>Energy Efficiency</b>	<b>22,4%</b>			<b>24,6%</b>		



**Figure 17 – T-s diagram of the recuperative Rankine power cycle simulated with CO<sub>2</sub>(60%)-R1234yf(40%) as working fluid in EES environmental**

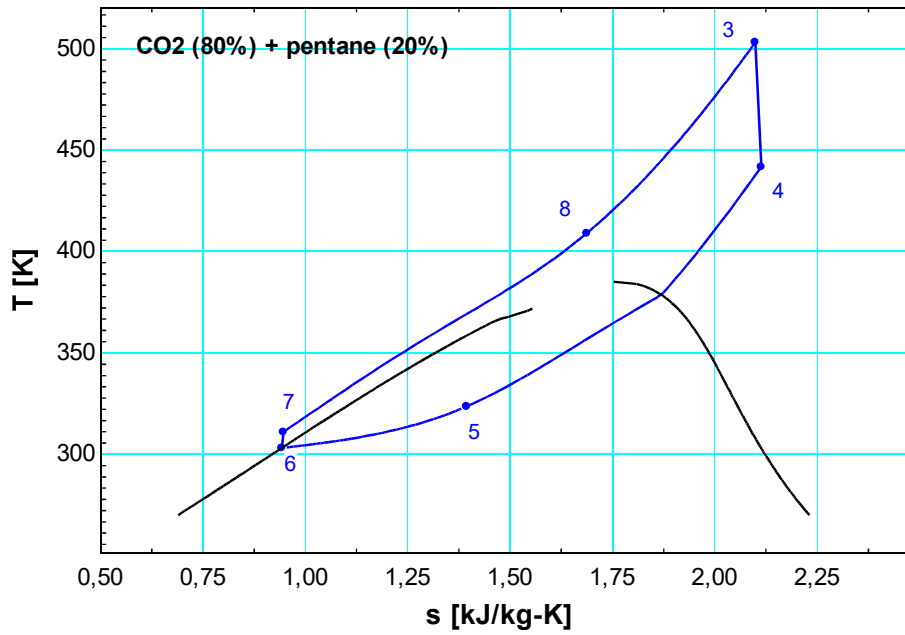


Figure 18 – T-s diagram of the recuperative Rankine power cycle simulated with CO<sub>2</sub>(80%)-pentane(20%) as working fluid in EES environmental

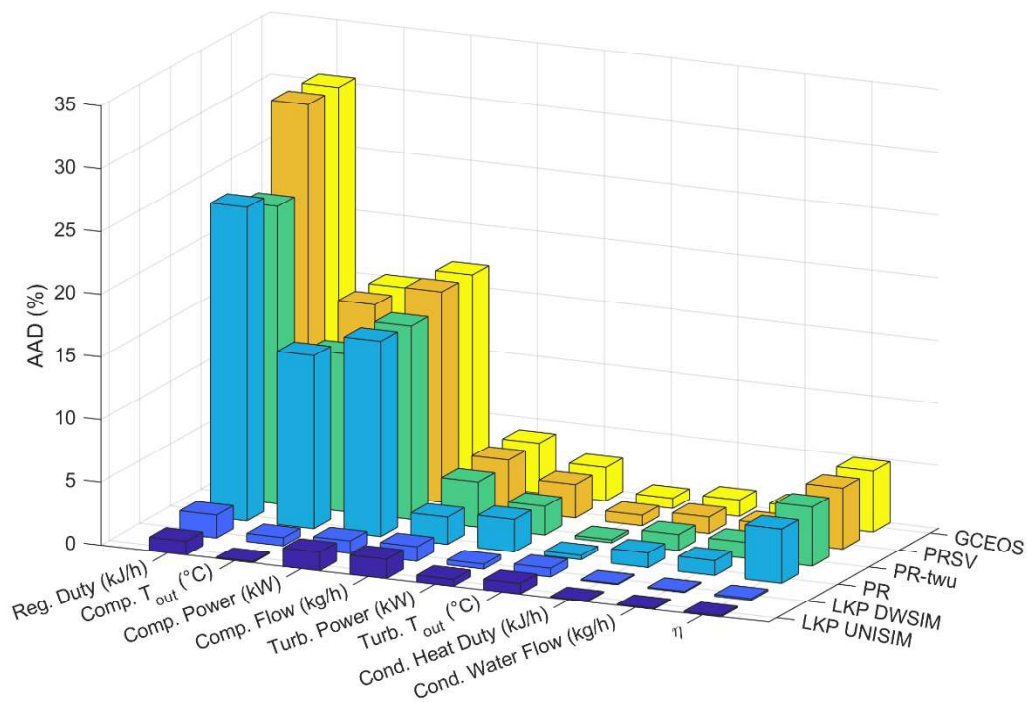
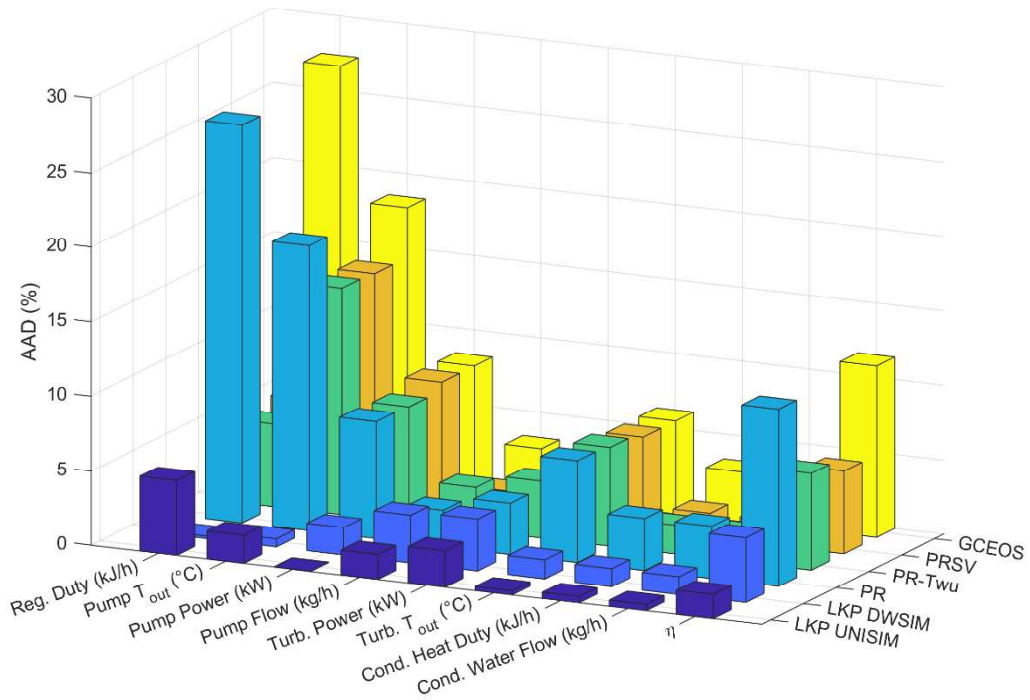
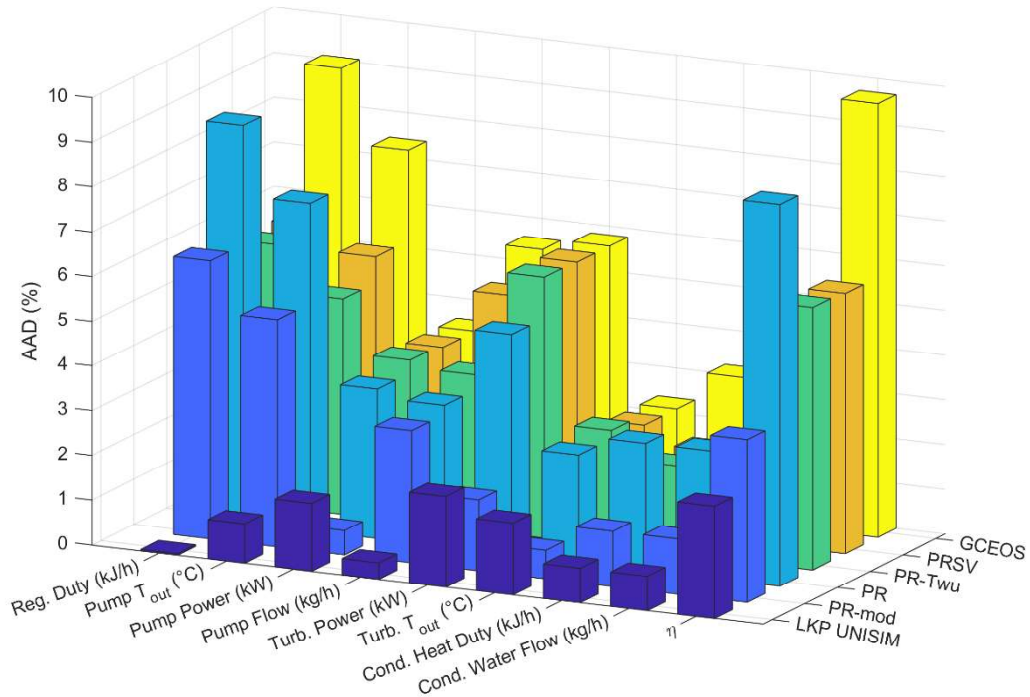


Figure 19 – Influence of the EoS on the AAD of each sCO<sub>2</sub> cycle key component



**Figure 20 – Influence of the EoS on the AAD of each cycle key component with CO<sub>2</sub>(60%)-R1234yf(40%) mixture as working fluid**



**Figure 21 – Influence of the EoS on the AAD of each cycle key component with CO<sub>2</sub>(80%)-pentane(20%) mixture as working fluid**

The results summarized in Figures 19, 20, and 21 confirm the relevance of the current investigation, revealing the significant influence of the selected EoS in the analysis of power cycles working with sCO<sub>2</sub> and CO<sub>2</sub> based novel mixtures. Specifically, the higher reliability of LKP is confirmed, as well as the larger deviation achieved when using other EoS (particularly cubic PR and GCEOS), especially when working with mixtures. It effectively points out, in a quantitative manner, the importance of the selected EoS when dealing with these problems.

## 6. Conclusions

In the present study, most of the EoS available in the literature for calculating the properties of pure-CO<sub>2</sub> and CO<sub>2</sub>-based mixtures under different thermodynamic conditions when working into sCO<sub>2</sub> cycles are discussed and compared, also with the support of available experimental data. Such a comparison is essential to assess the reliability of the EoS adopted for the simulation of the sCO<sub>2</sub> power cycle. It is even more important when dealing with power cycles working with CO<sub>2</sub>-based mixtures, designed to better adapt the CO<sub>2</sub> properties to different possible heat source behaviour and/or to raise the critical temperature at suitable environmental levels to allow transcritical configurations. This kind of critical review and validation, especially for mixtures, is currently not retrievable in the literature of energy systems, where often the EoS available into the specifically used thermodynamic tools are adopted without a critical approach, sometimes resulting in questionable comparisons of different cycles configurations and working conditions.

The first significant outcome of the present research is that it is practically impossible addressing a specific EoS or an EoS-based database as the most reliable one. Moreover, based on the type of the fluid and the thermodynamic zone on the fluid phase envelope, the most suitable EoS family may be selected to improve the reliability of the results. On the whole, the following relevant conclusions may be outlined from this research:

- I. REFPROP is a stand-alone program, generally based on the most advanced EoS often validated against available experimental literature data. It is accurate for single-component fluids, mentioned by several studies, and, in most cases, it is considered a benchmark for several, even new, approaches and EoS. However, it evidenced some limits on the temperature/pressure range and/or against experimental data of new CO<sub>2</sub>-based mixtures. The accuracy may vary from the released version.
- II. Other alternative EoS, built with specific mixing rules, may be adopted for common and novel CO<sub>2</sub>-based mixtures (e.g. CO<sub>2</sub>+R1234yf and CO<sub>2</sub>+R1234ze(E)) under a wider range of conditions. Among the discussed EoS, the LKP showed to be the most reliable one for the property estimation of pure CO<sub>2</sub>. If possible, the use of EoS available in DWSIM is recommended.
- III. When dealing with CO<sub>2</sub>-based mixtures, the results showed that the Lee-Kesler-Plocker equation, with BIP set at zero, is also reliable for mixtures of CO<sub>2</sub> and HFOs (e.g. R1234yf and R1234ze(E)). The suggested model for CO<sub>2</sub>-hydrocarbons mixtures is not a single one, but it is determined as a table covering various fluids and mixture compositions [84]. Hence, as a relevant part of the conclusions, a summary table with our recommendations is reported hereafter:

**Table 11 – EoS recommended for the analysed mixtures**



Mixtures	LKP	PR	PR mod
CO <sub>2</sub> + R1234yf	0.6 < xCO <sub>2</sub> < 1		
CO <sub>2</sub> + R1234ze(E)	0.6 < xCO <sub>2</sub> < 1		
CO <sub>2</sub> + n-butane		0.6 < xCO <sub>2</sub> < 1	
CO <sub>2</sub> + n-hexane		xCO <sub>2</sub> < 0.7	xCO <sub>2</sub> > 0.7
CO <sub>2</sub> + n-pentane			0.6 < xCO <sub>2</sub> < 1
CO <sub>2</sub> + propane		0.6 < xCO <sub>2</sub> < 1	

- IV. For both blends of refrigerants and hydrocarbons, a general increase of the mean absolute error with the increasing molar concentration of the second component was found. Therefore, the EoS-based approaches are generally more accurate at lower concentrations of the non-CO<sub>2</sub> component.
- V. The thermodynamic results show that the CO<sub>2</sub>-based mixtures, in a transcritical configuration, can achieve efficiencies higher than the sCO<sub>2</sub> power cycle. Generally, the lower the maximum pressure, the higher the efficiency improvement. In the case of mixing carbon dioxide with R1234yf, R1234ze(E), or propane, the reduction of CO<sub>2</sub> molar concentration drives better performance. On the other hand, the highest efficiency of the cycle mixing carbon dioxide with butane, hexane, and pentane is achieved with an intermediate CO<sub>2</sub> molar content. These considerations are summarized in Table 12.

**Table 12 – CO<sub>2</sub> molar content for each mixture which leads to the best thermodynamic efficiencies**

Mixture	Best CO <sub>2</sub> molar content
CO <sub>2</sub> + R1234yf	60%
CO <sub>2</sub> + R1234ze(E)	60%
CO <sub>2</sub> + n-butane	70%
CO <sub>2</sub> + n-hexane	80%
CO <sub>2</sub> + n-pentane	80%
CO <sub>2</sub> + propane	60%

- VI. The reliability performance indicators, applied to various CO<sub>2</sub> mixtures and pure sCO<sub>2</sub> cycle processes, were estimated for several property methods (EoS) and compared to REFPROP. For example, when dealing with the recuperative sCO<sub>2</sub> cycle, the Recuperator Heat Duty was the most significantly affected parameter, and the results showed that LK-PLOCK performs most similarly to REFPROP under the analysed cycle conditions. Looking at the analyzed mixtures, for CO<sub>2</sub>(60%)-R1234yf(40%), as widely expected, LKP confirms to be the most reliable EoS to predict the several states of the working fluid across the cycle components. For CO<sub>2</sub>(80%)-pentane(20%) PR-mod demonstrates more suitability than PR and the other Cubic-equations of state. However, the Lee-Kesler-Plocker model seems to be the most accurate, especially close to the pump operating points thanks to the good prediction of mixtures' density (Figure 6); but, according to Figure 7 and Figure 8, it is reasonable to expect a worsening of the thermodynamic prediction with reducing the CO<sub>2</sub> molar content in the fluid.

Overall, the most relevant outcome of the present study is helping and addressing the property methods selection in the design and analysis of CO<sub>2</sub> and CO<sub>2</sub>-based mixture power cycles, which is

a fundamental step to realize reliable simulation procedures of power cycles working with novel CO<sub>2</sub> mixtures. The here proposed accurate investigation is a valuable contribution to a current lack in the literature dealing with power cycles working with sCO<sub>2</sub> and CO<sub>2</sub> mixtures.

## 7. Appendix A

Based on the first law of thermodynamic, the main thermodynamic relations and the energy balance equations of the regenerated Rankine cycle, used for the simulations in EES environmental, are shown in the following section.

- **Turbine (3-4)**

Turbine inlet temperature:  $T_3 = T_1 - \Delta T_{approach}$  (Eq.A1)

Turbine work:  $W_t = m_{wf}(h_3 - h_4)$  (Eq.A2)

Isentropic turbine efficiency:  $\eta_{t;is} = \frac{h_3 - h_4}{h_3 - h_{4;is}}$  (Eq.A3)

- **Recuperator (4-5 / 7-8)**

Recuperator energy balance:  $Q_{REC} = m_{wf}(h_4 - h_5) = m_{wf}(h_8 - h_7)$  (Eq.A4)

- **Condenser (5-6 / 9-10)**

Condenser outlet temperature:  $T_6 = T_{10} - \Delta T_{pinch\ point}$  (Eq.A5)

Condenser energy balance:  $Q_{COND} = m_{water}(h_{10} - h_9) = m_{wf}(h_5 - h_6)$  (Eq.A6)

- **Pump (6-7)**

Pump work:  $W_p = m_{wf}(h_7 - h_6)$  (Eq.A7)

Isentropic pump efficiency:  $\eta_{p;is} = \frac{h_7 - h_6}{h_{7;is} - h_6}$  (Eq.A8)

- **Evaporator (8-3 / 1-2)**

Evaporator energy balance:  $Q_{EVA} = m_{hot\ source}(h_1 - h_2) = m_{wf}(h_3 - h_8)$  (Eq.A9)

- **Cycle parameters**

Net power output:  $W_{net} = W_t - W_p$  (Eq.A10)

Power cycle energy efficiency:  $\eta_{cycle} = \frac{W_{net}}{Q_{EVA}}$  (Eq.A11)

## 8. Nomenclature

$\mu$	Viscosity
AAD	Average Absolute Deviation
AIChE	American Institute of Chemical Engineers
BWRS	Benedict Webb Rubin Starling equation
COMP	Compressor
COND	Condenser
Cp	Specific heat capacity

EES	Engineering Equation Solver
EOS	Equation of State
GCEOS	Generalized Cubic Equation of State
h	Enthalpy
HC	Hydrocarbon
LFL	Low Flammability Level
LKP	Lee-Kesler-Plocker equation
LK-PLOCK	Lee-Kesler-Plocker property method
$m_{hot\ source}$	Hot source flow rate
$m_{water}$	Cooling water flow rate
$m_{wf}$	Working fluid flow rate
PR	Peng-Robinson equation
PR-BM	Peng-Robinson-Boston-Matias equation
PR-mod	Peng-Robinson modified
PRSV	Peng–Robinson–Stryjek–Vera equation
PR-twu	Peng-Robinson Twu alpha function equation
$Q_{COND}$	Condenser heat duty
$Q_{EVA}$	Evaporator heat duty
$Q_{in}$	Heat energy input entering the system
$Q_{REC}$	Recuperator heat duty
REFPROP	Reference Fluid thermodynamic and transport Properties
REG	Regenerator
RK-SOAVE	Redlich-Kwong equation
RMSE	Root Mean Square Error
S	Entropy
sCO <sub>2</sub>	Supercritical CO <sub>2</sub>
SRK	Redlich–Kwong–Soave equation
SRK-twu	Redlich–Kwong–Soave Twu alpha function equation
SW	Span-Wagner equation
T	Temperature
TURB	Turbine
$W_{net}$	Net power output
$W_p$	Work absorbed by the pump
$W_t$	Work produced by the turbine
xCO <sub>2</sub>	Molar content of carbon dioxide
$\eta$	Energy Efficiency
$\rho$	Density

## 9. References

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