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1 **Effects of flow constriction on foamed viscous shear-thinning fluids downstream**
2 **of a continuous multi rotor-stator foaming device**

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4
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12
13 **Abstract**

14
15 Foam flow through processing equipment can seriously affect the structure of the foam and its quality
16 attributes. In the design of a foam formulation and its flow system, it is therefore important to consider the
17 possible implications on the end-of-pipe structure of the foam to ensure preservation of product quality.
18 We study the flow through a straight pipe with and without the presence of a narrow orifice plate and,
19 hence, the dynamic stability of wet food relevant foams of fine texture and high static stability generated
20 from complex formulations of viscous shear-thinning fluids in a continuous multi rotor-stator device. The
21 effects of fluid formulation, gas-liquid ratio, rotor speed and constriction aperture size are investigated.
22 Constricted foam flow can cause important transformations in the foam due to significant bubble
23 coalescence and loss of air volume resulting in much coarser and much less stable foam. Increased
24 surfactant content, liquid viscosity and rotor speed reduce bubble coalescence and help preserve foam
25 structure.

26
27 **Keywords:** foam flow; flow constriction; foam dynamic stability; pressure drop; wet foam; non-
28 Newtonian liquid.

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37 1. Introduction

38 Foams are complex multi-component structures which enjoy many applications in a wide range of
39 industries including food, pharmaceuticals, mineral transport, oil and gas. Dry foams are structured two-
40 phase fluids in which polyhedral gas bubbles are separated by interconnecting thin liquid films and Plateau
41 borders which denote the regions of intersection of the thin films, whilst wet foams including food foams
42 tend to be bubbly liquids with round bubbles. Foams represent an important class of structured fluids
43 possessing a complex rheology and flow behaviour strongly dependent upon local structure and chemical
44 composition. The nature of the foam, i.e. its texture and stability, and its overall rheological and flow
45 properties can determine both the economic and technical successes of the industrial process concerned.
46 For example, some aerated products possessing a smaller bubble size and a uniform bubble size distribution
47 have a much longer shelf-life and better consumer perception because of their better creaminess (Müller-
48 Fischer and Windhab, 2005, Müller-Fischer, Suppiger and Windhab, 2007b). Information on both the static
49 as well as dynamic behaviour of foams is of direct value to the manufacture of a wide range of foods. Foam
50 flow through processing equipment usually affects the structure of the foam and its properties. In the design
51 of a food foam formulation and its flow system, it is therefore important to consider the possible effects on
52 the end-of-pipe structure and, hence, quality attributes of the foam. These effects may have serious practical
53 implications and have to be carefully considered as preservation of product structure and quality during
54 processing is important.

55
56 Effective stabilisation of a food foam is critical since bubble coalescence can lead to a loss of
57 microstructure and hence a deterioration of foam organoleptic properties such as texture and taste. Food
58 foams are often stabilised with protein molecules (β -lactoglobulin, casein, albumin and whey protein
59 isolate) commonly derived from milk and egg (Zayas, 1997). Protein molecules drastically alter the
60 interfacial rheological properties providing a strong mechanical barrier against bubble coalescence
61 (Murray *et al.*, 2006). More recently, however, non-ionic surfactants such as polyglycerol fatty acid
62 ester, PGE 55, hydrophobins and food-grade particles (agar gel particles) have attracted considerable
63 attention (Curschellas *et al.*, 2013, Cox, Aldred and Russell, 2009, Ellis *et al.*, 2017, Dickinson, 2010),
64 as they have been shown to have excellent foam stabilisation properties (Duerr-Auster *et al.*, 2007,
65 Duerr-Auster *et al.*, 2008, Curschellas *et al.*, 2013b). The irreversible adsorption of PGE 55, once
66 exposed to heat above its Kraft temperature (58 °C), can significantly reduce the rate of coalescence. In
67 addition, the presence of multilamellar vesicles, formed as a result of its very low critical aggregation
68 concentration (c_{ac}), in films and Plateau borders greatly improves stabilisation against drainage
69 (Curschellas *et al.*, 2013). Likewise, the addition of food hydrocolloids such as guar gum, xanthan gum
70 and low-molecular weight viscosity-enhancing sucrose can drastically reduce foam drainage. Inclusion
71 of hydrocolloids tends to also improve foam texture and smoothness in products such as ice cream
72 (Murray *et al.*, 2006). In the case of proteins, inclusion of these viscosity modifying ingredients may
73 lead to synergistic interaction, however, but this is not the case with PGE 55.

74

75 Any process where significant deformation of the air-water interface is likely to occur may lead to
76 bubble coalescence. Such processes include the flow of aerated products through nozzles, pipes, pipe
77 fittings and pumps. In addition, in the food industry, aeration is predominantly performed under
78 pressurised conditions (typically, 2–3 bar) to reduce the effective air volume fraction inside the mixing-
79 head chamber of the foam generator and, hence, diminish the probability of bubble collision and
80 re-coalescence during foam generation. Once the foam is discharged to atmosphere, bubbles expand as
81 a result of the pressure drop, but an over-beating phenomenon can take place as a result of increased
82 residence time because of the reduced gas volume fraction inside the mixing-head chamber.

83

84 Operations involving rapid pressure drop (e.g. flow from a nozzle), steady and elongation shear (e.g.
85 flow through a pipe) can lead to a severe loss of foam attributes. Much of the current understanding of
86 these effects stems from the engineering literature. Calvert and co-workers were the first to examine the
87 effects of geometric constrictions (commercial diaphragm, globe and ball valves) on fire-fighting
88 foams. It was found that a flow constriction (globe valve) with an intricate flow path (high shear rates)
89 and a high residence time led to foam breakdown in contrast to a diaphragm or ball valve (Calvert and
90 Nezhati, 1987, Calvert, 1988). Deshpande and Barigou (2000, 2001a, 2001b) examined the flow of dry
91 and wet detergent-stabilised foams in straight pipes fitted with a variety of flow constrictions
92 (expansion, contraction, orifice plate, perforated plate, bend, elbow). They found that foam flow
93 through pipe fittings is characterised by complex phenomena which influence foam structure, liquid
94 holdup and flow regime. In general, the liquid holdup decreases substantially downstream of a fitting,
95 which results in intense recirculation flow patterns upstream and a much drier foam downstream. A
96 sudden expansion can lead to a complete breakdown of the foam (Deshpande and Barigou, 2001a).
97 Thus, pipe fittings can have serious effects on the end-of-pipe structure of a foam, hence, resulting in
98 important practical implications for the preservation of product structure. Similar but more detailed
99 work has been recently reported on the flow of monolayer foams through narrow 2D channels with
100 constrictions (Badve and Barigou, 2020). However, little is known about the flow behaviour of food
101 foams which have a more complex composition and, thus, a more complex rheology.

102

103 Dickinson and coworkers developed an apparatus for the direct visualisation of foam microstructure
104 under rapid pressure drop. One major finding from their study was that foam made from gelatine was
105 less likely to undergo coalescence when exposed to rapid pressure drop (Dickinson *et al.*, 2002, Murray
106 *et al.*, 2006). Similarly, Heuer *et al.* (2007) reported the effects observed on the microstructure of a
107 model food foam, using a Linkam pressure cell to pressurise the foam to different levels from
108 atmospheric pressure up to 11 bar and then releasing the pressure at varying rates. The setup was also
109 used to study the effects of disproportionation and single and multiple pressure cycles on the resultant
110 foam. Significant pressure drops were quite destructive, with most coalescence observed from 2 bar

111 down to 1 bar absolute. Surprisingly, however, no coalescence was observed from 11 bar, the starting
112 pressure, down to 2 bar absolute. Significant effects were seen when the pressure release rates were
113 varied. Slow pressure release rates (2 min per bar released) had the effect of causing increased
114 coalescence events, when compared to very quick release rates (Heuer *et al.*, 2007). Other studies on
115 continuous foaming of Newtonian and non-Newtonian model liquid food formulations using a rotor-
116 stator device all agree on the fact that an increase in rotor speed leads to a significant reduction in bubble
117 size (Müller-Fischer, Suppiger and Windhab, 2007b, Jabarkhyl *et al.*, 2020a, Mary *et al.*, 2013).
118 However, there are conflicting reports on the effects of static pressure and residence time which hitherto
119 remain unclear and hence need further investigation (Mary *et al.*, 2013, Balerin *et al.*, 2007, Müller-
120 Fischer and Windhab, 2005)

121

122 Recently, we investigated the continuous foaming of viscous non-Newtonian shear-thinning model food
123 liquids in a pilot-scale multi rotor-stator high-shear device (Jabarkhyl *et al.*, 2020a), and studied the
124 effects of processing parameters including rotor speed, gas-liquid ratio, surfactant and xanthan gum
125 concentration. Furthermore, we studied the steady-shear as well as viscoelastic rheological properties
126 of the various wet foams thus generated (Jabarkhyl *et al.*, 2020b). The foams exhibited high static
127 stability and resistance to steady shear with no bubble breakage observed when the foams were sheared
128 between parallel-plates on a rheometer. In this paper, we study the flow of these wet model food foams
129 and their dynamic stability as they flow through a straight pipe and interact with a narrow orifice plate
130 constriction. Narrow orifices of different aperture sizes are used to generate significant pressure drops on
131 a lab scale which would mimic the flow of such foams through nozzles and pipe fittings in industrial setups.
132 The effects of fluid formulation, gas-liquid ratio, rotor speed and orifice aperture size, are investigated.

133

134 **2. Materials and methods**

135 **2.1 Model fluids and foam generation**

136 The materials and methods used are based on our recent related work which studied the continuous
137 production of foams from complex viscous shear-thinning fluids in a multi rotor-stator device and their
138 rheological properties (Jabarkhyl *et al.*, 2020a, Jabarkhyl *et al.*, 2020b). We used five model complex
139 non-Newtonian fluid formulations of shear-thinning rheology consisting of a mixture of polyglycerol
140 fatty acid ester (PGE 55), xanthan gum (XG), caster sugar and sodium azide, denoted MF1, MF2, MF3,
141 MF4 and MF5, whose composition and physical properties are summarised in Table 1. Foams were
142 generated by aerating the model fluids in a pilot-scale continuous multi rotor-stator unit (Megatron FM
143 12- 50/2 HR) depicted in Fig. 1. The geometrical dimensions of the 12 rotor-stator pairs positioned in
144 series inside the foam generator are provided in Table 2. A Julabo F-25 cooling system enabled the
145 foam temperature at the outlet of the foaming unit to be kept approximately equal to the inlet feed
146 temperature (20 °C). Foams of different textures were obtained by using combinations of liquid and air
147 flowrates within the range 2.5 – 5.0 L h⁻¹ and 0.1 – 12.5 L hr⁻¹, respectively. Further details of the

148 protocols adopted for the preparation of the model fluids and foams can be found in our previous work
149 (Jabarkhyl *et al.*, 2020a, Jabarkhyl *et al.*, 2020b).

150

151 **2.2 Foam characterisation**

152 The foams produced were characterised by determining their air volume fraction, their bubble size
153 distribution and their rheological properties.

154

155 *2.2.1 Air volume fraction*

156 The foam air fraction (ϕ_e) was experimentally determined by collecting foam samples of known volume
157 at the outlet of the foam generator and measuring the mass of liquid within. The foaming process aims
158 to maximise ϕ_e and achieve the maximum theoretical value $\phi_{th}^{(P)}$, defined in terms of the pressure-
159 dependent volumetric air flowrate $Q_G^{(P)}$ and liquid volumetric flowrate Q_L , as:

160

$$161 \quad \phi_{th}^{(P)} = \frac{Q_G^{(P)}}{Q_G^{(P)} + Q_L} \quad (1)$$

162

163 The effects of pressure are taken into account through the ideal gas law, thus:

164

$$165 \quad F_E = \phi_{th}^{(Patm)} \left(\frac{P_{atm}}{P} \right) \quad (2)$$

166

167 where F_E is the foam expansion ratio dependent on pressure, air and liquid flowrate in the mixing-head
168 chamber and $\phi_{th}^{(Patm)}$ is the equivalent air volume fraction at atmospheric pressure P_{atm} .

169

170 Another important parameter is the average residence time, τ , inside the mixing-head chamber of the
171 foam generator (Fig. 1) which can be estimated using the foam volumetric flowrate (V_{foam}) and the
172 volume of the mixing-head chamber ($V = 85$ mL), thus:

173

$$174 \quad \tau = \frac{V}{V_{foam}} = \frac{V}{Q_L + Q_G^{(P)}} \quad (3)$$

175

176 *2.2.2 Foam bubble size distribution*

177 A foam sample of about 5 ml was carefully placed inside a plastic drinking straw using a pipette and
178 sealed prior to scanning. X-ray micro-Computed Tomography measurements were performed on a
179 Skyscan instrument (Skyscan 1172, Bruker, Belgium) operating at a source voltage of 80 kV and current
180 of 98 μ A, with an image resolution of $3.78 \mu\text{m pixel}^{-1} \times 5.78 \mu\text{m pixel}^{-1}$. No filter was used since foam
181 has a low density and a low attenuation coefficient. Each sample was scanned over 180 degrees in

182 discrete steps of 0.4 degree with a frame averaging of 4 to acquire up to 1200 radiographic images of
183 1048×2000 pixels. The scan duration was limited to less than 20 min to avoid any significant effects
184 arising from gravity drainage of the foam. A computer recorded the images for subsequent
185 reconstruction using NRecon software (Bruker micro-CT, Belgium), based on the principle of filtered
186 back-projection utilising the method of cone-beam reconstruction. At least three samples of the same
187 foam were scanned to obtain statistically significant results. Depending on the scanning parameters
188 implemented, the reconstruction procedure took approximately 5 – 10 min. Finally, the projection
189 images were uploaded to a CTan software (Bruker micro-CT, Belgium) for detailed image analysis.
190 The technique provides non-invasively a high-resolution 3D model of the microstructure of a stable
191 foam, from which the bubble size distribution and various descriptive statistics are derived including
192 the Sauter mean bubble diameter (D_{32}) defined as:

193

$$194 \quad D_{32} = \frac{\sum n_i d_i^3}{\sum n_i d_i^2} \quad (4)$$

195

196 where n is the number of bubbles of diameter d in class size i . The technique and its protocol have been
197 described in more detail in our previous works (Lim and Barigou, 2004, Barigou and Douaire, 2013,
198 Jabarkhyl *et al.*, 2020a).

199

200 2.2.3 Rheological properties of model fluids and foams

201 The oscillatory rheology of the foams studied was characterised at 25 °C using a 40 mm parallel-plate
202 geometry with a gap of 2.0 mm fitted on a controlled stress/strain rheometer (Discovery HR-2, Hybrid
203 Rheometer, TA, USA). Amplitude sweep tests with % strain varying in the range 0.01 to 1000% were
204 conducted at 1 Hz frequency to determine the viscoelastic moduli (G' , G''). The use of roughened plates
205 (58 μm equivalent grit size) enabled the elimination of slip. Measurements were repeated at least three
206 times using fresh samples and an average obtained. The measurement time was kept short to avoid
207 foam drainage effects. More details on the rheometry procedures adopted can be found in our previous
208 work (Jabarkhyl *et al.*, 2020b).

209

210 2.3 Foam flow through an orifice constriction

211 The foam flow rig consisted of two lengths of acrylic pipe of 30 mm diameter and 0.5 m length
212 connected by bolted flanges, as schematically represented in Fig. 2. Digital pressure transducers
213 (Druck, UK) connected to a computer via a data logger (PicoLog 1000 Series), were installed along the
214 flow pipe including at the inlet and at the exit of the constriction for pressure drop measurements. A
215 thin stainless-steel orifice plate (1.5 mm thick) was inserted between the two flanges to act as a
216 constriction to the foam flow. The orifice sizes investigated were: $D_o = 0.4, 0.5, 0.6, 0.8$ and 1.8 mm

217 diameter corresponding, respectively, to orifice-pipe area ratios of $A_o/A = 0.00020$; 0.00032 ; 0.00046 ;
218 0.00082 ; 0.00413). A foam sampling point was fitted at the exit of the constriction.

219

220 In a typical experiment, foam generated by the continuous rotor-stator device is fed directly into the
221 flow pipe. Foam samples are collected at the exit of the constriction for off-line analysis using an X-
222 ray micro-CT technique to determine the bubble size distribution. At this point, the foam pressure
223 would have dropped to nearly atmospheric and sampling at the wall does not introduce any significant
224 effects on the foam microstructure. Upstream of the constriction, however, the foam pressure is high
225 and wall sampling would cause expansion of the foam. Hence, the foam is photographed in-situ at the
226 pipe wall using a digital camera fitted onto a Leica microscope with a variable zoom lens, and the
227 bubble size distribution determined via image analysis using ImageJ software. Typically, a sample of
228 at least 500 bubbles is used and only bubbles in the centre of an image are analysed to avoid curvature
229 effects. It should be pointed out, however, that imaging at the wall does not yield accurate information
230 on the full 3D microstructure of the foam and is only used as a rough indication of the bubble size when
231 other means of visualisation are not possible (Deshpande and Barigou, 2000, Deshpande and Barigou,
232 2001a, Deshpande and Barigou, 2001b). Before taking measurements, the foam is allowed to flow
233 through the constricted pipe for up to 20 min until steady state conditions are reached, i.e. when pressure
234 readings and volume fraction of the foam collected at the exit of the pipe stabilise.

235

236 **2.4 Foam static stability**

237 Foam static stability was determined by monitoring, at a constant temperature of 50°C over a period of
238 several weeks, liquid drainage in 50 mL samples collected at relevant points of the flow system. Thus,
239 transients of drained liquid were obtained for all experimental conditions investigated. In each case,
240 three samples were analysed and an average obtained.

241

242 **2.5 Statistical analysis**

243 All measurements were performed in triplicate. A one-way analysis of variance (ANOVA) was
244 conducted using the well-known Minitab statistical software, and a Tukey's pairwise comparison test
245 was performed to find statistically significant results (i.e. $p < 0.05$). Results are reported as mean values
246 \pm standard deviation in Tables 3 – 6.

247

248 **3. Results and discussion**

249 **3.1 Aeration efficiency**

250 Aeration efficiency ($\eta = \phi_e/\phi_{th}$) is an important feature of the foam generation process which indicates
251 the ability to incorporate all of the available gas into the foaming liquid to make a homogeneous foam.
252 Thus, optimum aeration is achieved when the theoretical and experimental values of volume gas

253 fraction are equal (Eq. (1)). At atmospheric pressure, i.e. when the foam flow rig is not connected to
254 the rotor-stator device and the generated foam is simply discharged to atmosphere, maximum aeration
255 efficiency was achieved for all model fluids at most rotor speeds when the G/L ratio (ratio of air to
256 liquid volumetric flowrate) was set to 1.0, 1.5 and 2.0, corresponding respectively to $\phi_{th}^{(Patm)} =$
257 0.50, 0.60 and 0.67. These conditions were also achieved when the foam flow rig was connected to
258 the foam generator unit and flow took place through the short straight pipe without a constriction; in
259 this case the pressure inside the mixing-head chamber was close to atmospheric given that the linear
260 pressure drop in the pipe was small (~ 0.1 bar), as shown in Table 3. Such a low pressure drop along
261 the pipe did not have any significant effects on the microstructure of the flowing foam including bubble
262 size and gas holdup.

263

264 In the presence of a flow constriction, maximum aeration efficiency was only achieved when the
265 pressure drop ΔP_c across the constriction was below 1.0 bar, independent of the G/L ratio used (Table
266 3). The reduction in aeration efficiency with increasing pressure drop may be attributed to the relatively
267 large increase in bubble size across the constriction caused by bubble coalescence - note that bubble
268 expansion through the constriction accounts for only a relatively small part ($\sim 20\%$) of this increase in
269 bubble size.

270

271 **3.2 Effects of processing parameters on bubble size distribution**

272 *3.2.1 Effects of residence time*

273 Whilst it is well known that increasing the rotor speed reduces bubble size (Jabarkhyl *et al.*, 2020a,
274 Mary *et al.*, 2013, Müller-Fischer, Suppiger and Windhab, 2007b), the effects of residence time and G/L
275 ratio are not always clearly identified. For example, Muller-Fischer, Suppiger & Windhab (2007b)
276 reported that a longer residence time led to a smaller bubble size, whereas Mary *et al.* did not observe
277 a clear trend. Such conflicting reports may be due to differences in foaming solutions (Newtonian, non-
278 Newtonian), processing parameters and hydrodynamic conditions (rotor speed, pressure and G/L ratio,
279 laminar flow, turbulent flow), imaging procedures (online, off-line) and different rotor-stator
280 geometries; in addition, the cross-influence of residence time and dispersion viscosity is not taken into
281 account in most cases (Müller-Fischer, Suppiger and Windhab, 2007b, Mary *et al.*, 2013).

282

283 In this study, for a fixed G/L ratio, doubling the residence time led to a significant reduction in bubble
284 size, as shown in Fig. 3, the extent of reduction being a function of G/L ratio and N . The smaller the
285 G/L ratio, the greater the influence of residence time on the bubble size distribution (BSD) and, hence,
286 on D_{32} . Increasing the G/L ratio (i.e. increasing ϕ_e) and τ leads to a narrower, more uniform BSD; the
287 effects of τ reduce as the G/L ratio and N increase. These observations can be explained in terms of
288 bubble breakage and coalescence frequency inside the mixing-head chamber. At smaller G/L ratios,

289 the probability of bubble coalescence is low and bubble breakage is predominant and, hence, a longer
290 residence time results in a smaller bubble size. At higher G/L ratios, the larger bubble number density
291 leads to an equilibrium between bubble breakage and coalescence, which reduces the effect of τ . Under
292 all conditions, the effect of τ diminishes with increasing N . It should also be pointed out that substantial
293 variations in τ are required to generate any noticeable effects on bubble size.

294

295 3.2.2 Effects of air volume fraction

296 Typical results depicting the effects of air volume fraction on bubble size for a fixed residence time (τ
297 = 40 s) are shown in Fig. 4. The BSD is more or less the same for $G/L \leq 1.0$, however, the BSD
298 becomes much narrower and more uniform for $G/L \geq 1.5$. The data fall into two distinct regions: (i) a
299 region of constant D_{32} corresponding to low and medium ϕ_e values; and (ii) a region of sharp decline in
300 D_{32} at higher gas volume fractions. Müller-Fischer, Suppiger and Windhab (2007b) using a similar
301 rotor-stator device, but a different non-Newtonian fluid formulation and operating at much higher rotor
302 speeds and a much shorter residence time, reported the same plateau region beyond which, however, D_{32}
303 increases sharply as a function of ϕ_e . The rise in bubble size was attributed to the increased coalescence
304 rate because of the higher rotor speeds and the higher ϕ_e values they used as well as the significant time
305 lag between foam sampling and bubble size measurement using a light microscope (Müller-
306 Fischer, Suppiger and Windhab, 2007b). The latter effect was obviated here because of the high stability
307 of the foams (Jabarkhyl *et al.*, 2020a) and the use of fast X-ray micro-CT analysis. There is no
308 significant effect on BSD for $G/L < 1.0$, however, the BSD becomes much more uniform for $G/L \geq 1.5$.

309

310 3.3 Foam flow through a short straight pipe

311 Initial foam flow experiments were conducted through a short straight pipe without constriction. Using
312 foams generated from the different model fluids (Table 1), varying the foam flowrate in the range 7.5
313 – 16.0 L hr⁻¹ by varying the G/L ratio from 0.5 to 2.0, engendered a maximum pressure drop along the
314 pipe of about 0.1 bar. Such a pressure drop was too low to cause any significant effects on the foam
315 microstructure and texture along the pipe. These foams exhibit high static and quasi-static stability
316 (Jabarkhyl *et al.*, 2020a).

317

318 3.4 Foam flow through a straight pipe with an orifice constriction

319 3.4.1 Effects of G/L ratio

320 The diameter of the orifice constriction was varied in the range 0.5 – 1.8 mm to achieve different
321 pressure drops in the foam flow (Table 3). X-ray micro-CT images showing the microstructure of foams
322 generated from MF2 flowing with and without a flow constriction are depicted in Fig. 5a. In the absence
323 of a flow constriction, the foams exhibit a fine texture characterised by a narrow BSD with a peak at
324 100 μm and the vast majority of bubbles being less than 200 μm . In contrast, in the presence of a flow

325 constriction the BSD is much wider and the foam texture much coarser with bubble sizes up to 600 μm
326 being observed. Though the relative frequency of the larger bubbles is small, they do contribute
327 significantly to the Sauter mean diameter, as shown in Fig. 6.

328

329 Over the range of conditions investigated, the mean bubble size measured at the exit of the constriction
330 increased approximately linearly as a function of ΔP_c , as shown in Fig. 6. In a short straight pipe (data
331 points corresponding to approximately zero pressure drop), the G/L ratio has a relatively small effect
332 on D_{32} . Upstream of the constriction, the mean bubble size is independent, within experimental error,
333 of the orifice size used, as revealed by the data presented in Table 3. A reduction in orifice size
334 corresponds to an increase in pressure inside the mixing-head chamber, the effect of which seems to be
335 cancelled by a longer residence time leading to a constant mean bubble size. An identical maximum
336 bubble size is expected, provided the air volume fraction and the residence time are kept constant inside
337 the mixing-head chamber, independent of the applied static pressure, since the critical Weber number
338 is independent of pressure (Müller-Fischer, Suppiger and Windhab, 2007b).

339

340 A higher G/L ratio, i.e. a higher gas holdup, causes a significantly larger increase in D_{32} , reflected in a
341 greater slope of the linear trend. Qualitatively similar findings were reported by Müller-Fischer and
342 coworkers for different foam formulations and flow conditions (Müller-Fischer, Suppiger and Windhab,
343 2007b, Müller-Fischer and Windhab, 2005). The results appear to suggest that at low pressure drops,
344 the foam is able to squeeze through the constriction without incurring significant structural damage. As
345 ΔP_c increases, the foam texture becomes coarser due to increased bubble coalescence. This effect seems
346 to be even more significant for dryer foams probably because of the higher bubble density and thinner
347 liquid films. To illustrate the severity of the foam degradation that can occur, flow experiments were
348 conducted through an even narrower 0.4 mm orifice creating a much higher pressure drop of 2.5 bar,
349 and the results are depicted in Fig. 7. The BSD becomes much wider and positively skewed. In this
350 case, there was an almost 5 fold increase in the D_{32} from ~ 130 to ~ 600 μm .

351

352 These results serve to demonstrate that even such statically highly stable foams, do incur significant
353 structural transformations as a result of dynamic interactions with processing equipment. Hence, the
354 transport and processing of these structured fluids should avoid high pressure drops and should be
355 conducted as far as possible under conditions of pressure close to atmospheric.

356

357 3.4.2 Effects of PGE 55 surfactant concentration

358 Flow experiments were conducted through a short straight pipe first without and then with a constriction
359 (0.8 mm orifice plate) at G/L = 1.5, using foams generated from fluids MF1, MF2 and MF3 containing
360 respectively, 0.2, 0.5 and 1.0 wt% PGE 55 surfactant, but the same XG concentration (0.5 wt%). It
361 should be pointed out that the cac (critical aggregation concentration) of PGE 55 is very low (0.00001

362 wt%), such that the concentrations used here are orders of magnitude higher (Gupta *et al.*, 2016). In
363 this case, maximum aeration efficiency was achieved under all conditions, as shown in Table 4. Whilst
364 the pressure drop across the constriction is, within experimental error, the same for the three fluids, the
365 relative increase in mean bubble size is greatest for fluid MF1 with the lowest PGE 55 content and
366 reduces as the PGE 55 concentration increases for MF2 and MF3, as shown in Fig. 8.

367

368 Foams generated in the absence of a flow constriction have a relatively narrow BSD and have a peak at
369 around 100 μm . Flow through the constriction, however, leads in all cases to a much broader positively
370 skewed BSD. The effects are considerably more severe for fluid MF1 than MF2 and MF3. A possible
371 reason for this may be due to the excess PGE 55 multilamellar vesicles available at higher
372 concentrations to stabilise gas-liquid interfaces, clog plateau borders and thin films and, thus, slow
373 down liquid drainage and inhibit film rupture and bubble coalescence (Jabarkhyl *et al.*, 2020a).

374

375 Duerr-Auster *et al.* (2008) who studied the effects of pH on the foamability of PGE 55 solutions inside
376 a kitchen mixer, found that the adsorption kinetics of PGE 55 improved leading to much enhanced
377 foamability when the pH was reduced from 7 to 3. They attributed this improvement to the partial
378 destruction of PGE 55 multilamellar vesicles, thereby exposing a higher fraction of the hydrophobic
379 bilayer core to the air-water interface. They also found that acidity increased the rate of bubble
380 coalescence under static conditions by dramatically reducing coalescence time (Duerr-Auster *et al.*,
381 2008).

382

383 In this study, foams generated from fluid MF2 at pH 3 and pH 7 and G/L ratios of 1.0, 1.5 and 2.0 were
384 allowed to flow through a short straight pipe with and without a 0.8 mm orifice plate fitted, but no
385 significant effects were observed on either pressure drop or bubble size (data not shown). In this case,
386 the improved adsorption kinetics of the PGE 55 surfactant was not sufficient to influence bubble
387 coalescence during flow. Flow through the pipe with or without the constriction is relatively very fast
388 and there is probably insufficient time for the diffusion of multilamellar vesicles of PGE 55 to have an
389 effect.

390

391 3.4.3 *Effects of xanthan gum concentration*

392 The above flow experiments were repeated at G/L = 1.5 to study the effects of varying the concentration
393 of xanthan gum using foams generated from fluids MF4, MF5 and MF2 containing respectively, 0.25,
394 0.35 and 0.50 wt% XG, but the same PGE 55 concentration (0.5 wt%). In this case, maximum aeration
395 efficiency was achieved under all conditions, as shown in Table 5. Foams generated in the absence of
396 a flow constriction have a relatively narrow BSD and have a peak at around 100 μm . Flow through the
397 constriction, however, leads in all cases to a right shift in the BSDs which become much broader and
398 positively skewed. The effects are most severe for fluid MF4. The pressure drop across the constriction

399 increases as a function of XG concentration, but the relative increase in mean bubble size is greatest for
400 fluid MF4 with the lowest XG content and reduces as the XG concentration increases for MF5 and
401 MF2, as shown in Fig. 9. The coarser foam texture at lower XG concentrations is probably due to the
402 lower liquid viscosity causing weaker foam stability because of faster drainage, shorter thin liquid
403 lifetime and higher rate of bubble coalescence.

404

405 3.4.4 *Effects of rotor speed*

406 Similarly, flow experiments were again performed at $G/L = 1.5$ but varying the rotor speed, viz $N =$
407 500, 1000, 1500 and 2000 rpm, using foams generated from fluid MF2. Maximum aeration efficiency
408 was achieved at all conditions investigated as shown in Table 6. Increasing N over this range led to a
409 modest increase in pressure drop across the constriction which can be explained by the finer foams
410 generated (i.e. more complex thin liquid film network) which dissipate more energy in flow (Jabarkhyl
411 *et al.*, 2020b). Flow through the constriction causes, in all cases, a considerable rise in the mean bubble
412 size, as shown in Fig. 10. The relative increase in D_{32} , however, is lowest for $N = 2000$ rpm probably
413 because of the much finer foam texture; in general, the finer the bubble size, the less the damage incurred
414 through a constriction.

415

416 3.5 Foam elasticity and static stability

417 3.5.1 *Foam elasticity*

418 Oscillatory tests were performed in the linear viscoelastic region to probe the unperturbed foam
419 structure. The storage modulus (G') is a function of air volume fraction and bubble size distribution.
420 For very wet foams ($\phi < \sim 0.50$) bubble size distribution has negligible effects on (G') (Jabarkhyl *et*
421 *al.*, 2020b). Typical G' measurements for foams generated from fluid MF2 at $G/L = 1.5$ and $N = 1000$
422 rpm are shown in Fig. 11. G' is the highest for foam generated under ambient condition since this foam
423 has a very fine texture. In contrast, G' decreases as the pressure drop incurred across the orifice
424 constriction increases, owing to the coarser texture of the emerging foam and the loss of air at the
425 highest pressure drop shown (Table 3).

426

427 3.5.2 *Foam drainage*

428 The raw foams generated in the rotor-stator device are statically extremely stable at room temperature
429 on a timescale of months (Jabarkhyl *et al.*, 2020a). To assess the effects of the interaction with the
430 constriction on the foam static stability, 50 ml foam samples were collected at the outlet of the flow
431 pipe with and without a constriction. The sealed samples were then stored at a controlled temperature
432 of 50 °C to enhance drainage and, consequently, shorten the foam lifetime and reduce experimental
433 monitoring time. Typical foam drainage transients and foam half-life estimates for foams generated
434 from fluid MF2 at $G/L = 1.5$ and $N = 1000$ rpm are shown in Fig. 12. Foams flowing in a short straight

435 pipe without incurring a significant pressure drop have a finer texture which provides more resistance
 436 to liquid flow and, hence, they exhibit the slowest drainage time and the longest half-life. In contrast,
 437 the half-life is significantly reduced for foams having passed through the orifice constriction which have
 438 a coarser texture and may also contain less air as a result (Table 3). Results show that the higher the
 439 pressure drop incurred, the less the foam stability.

440

441 **4 Conclusions**

442 Foams generated from viscous shear-thinning fluids in a continuous multi rotor-stator device exhibit
 443 long term static stability on the order of months due to their fine texture consisting of a uniform bubble
 444 size distribution and the high viscosity of their base liquid. Flow through a short straight pipe incurs a
 445 low pressure drop and produces no tangible effects on foam structure, thus, preserving the original
 446 bubble size and static stability of the foam. At low pressure drops, foams are able to squeeze through
 447 a narrow orifice constriction without incurring significant structural transformations. At higher pressure
 448 drops, flow through the constriction causes significant bubble coalescence and, in some cases, loss of
 449 air volume leading to much coarser and much less stable foam. Increased surfactant content, liquid
 450 viscosity and rotor speed reduce bubble coalescence and help preserve foam structure during dynamic
 451 interaction with a flow constriction.

452

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456

457

458 **Notation**

459	d	bubble diameter (m)
460	D_0	orifice plate diameter (m)
461	D_{32}	Sauter mean diameter (m)
462	$D_{32}^{(P_{atm})}$	Sauter mean diameter at atmospheric pressure (m)
463	$D_{32}^{(P)}$	Sauter mean diameter at pressure P (m)
464	F_{rel}	relative frequency (%)
465	G'	storage modulus (Pa)
466	G/L	ratio of volumetric flowrate of air to liquid (-)
467	MF1	model fluid 1
468	MF2	model fluid 2
469	MF3	model fluid 3
470	MF4	model fluid 4

471	MF5	model fluid 5
472	N	rotational speed (s^{-1})
473	p	level of statistical significance
474	ΔP_c	Pressure loss across constriction (Pa)
475	PGE 55	polyglycerol ester of fatty acid (-)
476	XG	xanthan gum (-)
477		
478	<i>Greek symbols</i>	
479	ϕ	air volume fraction (-)
480	ϕ_e	experimental air volume fraction (-)
481	ϕ_{th}^P	theoretical air volume fraction at pressure P (-)
482	$\phi_{th}^{P_{atm}}$	theoretical air volume fraction at atmospheric pressure (-)
483	$\dot{\gamma}$	shear rate (s^{-1})
484	τ	shear stress (Pa)
485	ρ	fluid density ($kg\ m^{-3}$)

486

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554

555

Table 1. Model fluids composition and properties.

Model fluid	PGE 55 (wt%)	XG (wt%)	Sugar (wt%)	ρ (kg m ⁻³)	σ_e (mN m ⁻¹)
MF1	0.2	0.50	25	1080	39
MF2	0.5	0.50	25	1080	38
MF3	1.0	0.50	25	1080	37
MF4	0.5	0.25	25	1080	38
MF5	0.5	0.35	25	1080	38

Table 2. Geometrical dimensions of continuous rotor-stator device.

Parameter	Symbol (unit)	Value
Diameter of annulus mixing space	L (mm)	5.00
Number of pins on rotor	I (-)	13.00
Number of rotor-stator pairs	h (-)	12.00
Distance between rotor-stator	s (mm)	1.00
Height of rotor/stator pin	q (mm)	2.50
Width of rotor pin	o (mm)	4.70
Rotor diameter	D (mm)	50.00
Distance between rotor pins	z (mm)	12.08

Table 3: Typical results of aeration efficiency and mean foam bubble size for different flow conditions obtained with fluid MF2 at $N = 1000$ rpm; $Q_L = 5.0$ L hr^{-1} ; $Q_G^{(Patm)} = 5.0, 7.5$ and 10.0 L hr^{-1} . Values followed by different superscript letters in the same column are significantly different ($p < 0.05$).

Sample	ΔP_c (bar)	τ (s)	$D_{32}^{(P)}$ (μm)	$D_{32}^{(Patm)}$ (μm)	$\phi_{th}^{(P)}$ (-)	$\phi_{th}^{(Patm)}$ (-)	ϕ_e (-)	$\eta = \phi_e / \phi_{th}^{(Patm)}$ (-)
G/L = 1.0	No constriction	31	–	$147^h \pm 3$	0.500	0.500	0.500	1.00
$D_o = 1.8$ mm	0.047	32	$147^a \pm 3$	$157^g \pm 5$	0.477	0.500	0.500	1.00
$D_o = 0.8$ mm	0.300	38	$147^a \pm 5$	$200^f \pm 5$	0.385	0.500	0.500	1.00
$D_o = 0.6$ mm	0.880	45	$147^a \pm 7$	$230^e \pm 10$	0.266	0.500	0.500	1.00
$D_o = 0.5$ mm	1.450	49	$147^a \pm 13$	$323^c \pm 20$	0.204	0.500	0.460	0.92
G/L = 1.5	No constriction	25	–	$130^i \pm 3$	0.600	0.600	0.600	1.00
$D_o = 1.8$ mm	0.058	27	$130^b \pm 5$	$138^h \pm 5$	0.567	0.600	0.600	1.00
$D_o = 0.8$ mm	0.357	34	$130^b \pm 5$	$227^e \pm 10$	0.442	0.600	0.600	1.00
$D_o = 0.6$ mm	0.956	43	$130^b \pm 11$	$300^c \pm 20$	0.307	0.600	0.600	1.00
$D_o = 0.5$ mm	1.680	48	$130^b \pm 13$	$447^b \pm 50$	0.224	0.600	0.560	0.93
$D_o = 0.4$ mm	2.500	56	$130^b \pm 10$	$580^a \pm 50$	0.171	0.600	0.540	0.90
G/L = 2.0	No constriction	20	–	$113^j \pm 3$	0.670	0.670	0.670	1.00
$D_o = 1.8$ mm	0.069	23	$113^c \pm 5$	$127^i \pm 5$	0.627	0.670	0.670	1.00
$D_o = 0.8$ mm	0.417	32	$113^c \pm 5$	$251^d \pm 5$	0.473	0.670	0.670	1.00
$D_o = 0.6$ mm	1.120	42	$113^c \pm 13$	$320^c \pm 20$	0.316	0.670	0.640	0.96
$D_o = 0.5$ mm	1.790	47	$113^c \pm 10$	$590^a \pm 50$	0.236	0.670	0.610	0.91

Table 4: Effects of PGE 55 surfactant concentration on aeration efficiency and mean foam bubble size for fixed flow conditions at $N = 1000$ rpm; $Q_L = 5.0$ L hr⁻¹; $Q_G^{(Patm)} = 7.5$ L hr⁻¹. Values followed by different **superscript** letters in the same column are significantly different ($p < 0.05$).

Sample	ΔP_c (bar)	τ (s)	$D_{32}^{(P)}$ (μm)	$D_{32}^{(Patm)}$ (μm)	$\phi_{th}^{(P)}$ (-)	$\phi_{th}^{(Patm)}$ (-)	ϕ_e (-)	$\eta = \phi_e/\phi_{th}^{(Patm)}$ (-)
MF1; G/L = 1.5	No constriction	25	–	143 ^d ± 10	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.327	34	143 ^a ± 10	430 ^a ± 17	0.452	0.600	0.600	1.00
MF2; G/L = 1.5	No constriction	25	–	130 ^d ± 10	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.357	34	130 ^a ± 10	227 ^b ± 8	0.442	0.600	0.600	1.00
MF3; G/L = 1.5	No constriction	25	–	110 ^e ± 5	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.362	34	110 ^a ± 10	174 ^c ± 10	0.441	0.600	0.600	1.00

Table 5: Effects of XG concentration on aeration efficiency and mean foam bubble size for fixed flow conditions at $N = 1000$ rpm; $Q_L = 5.0$ L hr⁻¹; $Q_G^{(Patm)} = 7.5$ L hr⁻¹. Values followed by different **superscript** letters in the same column are significantly different ($p < 0.05$).

Sample	ΔP_c (bar)	τ (s)	$D_{32}^{(P)}$ (μm)	$D_{32}^{(Patm)}$ (μm)	$\phi_{th}^{(P)}$ (-)	$\phi_{th}^{(Patm)}$ (-)	ϕ_e (-)	$\eta = \phi_e/\phi_{th}^{(Patm)}$ (-)
MF4; G/L = 1.5	No constriction	25	-	150 ^d ± 10	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.256	32	150 ^a ± 10	338 ^a ± 10	0.478	0.600	0.600	1.00
MF5; G/L = 1.5	No constriction	25	-	140 ^d ± 10	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.300	33	140 ^a ± 10	300 ^b ± 10	0.462	0.600	0.600	1.00
MF2; G/L = 1.5	No constriction	25	-	130 ^d ± 3	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.357	34	130 ^a ± 10	227 ^c ± 10	0.442	0.600	0.600	1.00

Table 6: Effects of rotor speed (N) on aeration efficiency and mean foam bubble size for fixed flow conditions at G/L = 1.5; $Q_L = 5.0$ L hr⁻¹; $Q_G^{(Patm)} = 7.5$ L hr⁻¹. Values followed by different **superscript** letters in the same column are significantly different ($p < 0.05$).

Sample	ΔP_c (bar)	τ (s)	$D_{32}^{(P)}$ (μm)	$D_{32}^{(Patm)}$ (μm)	$\phi_{th}^{(P)}$ (-)	$\phi_{th}^{(Patm)}$ (-)	ϕ_e (-)	$\eta = \phi_e/\phi_{th}^{(Patm)}$ (-)
$N = 500$ rpm	No constriction	25	–	230 ^b ± 6	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.330	34	230 ^a ± 10	340 ^a ± 10	0.451	0.600	0.600	1.00
$N = 1000$ rpm	No constriction	25	–	130 ^d ± 5	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.357	34	130 ^b ± 10	227 ^b ± 10	0.442	0.600	0.600	1.00
$N = 1500$ rpm	No constriction	25	–	94 ^f ± 3	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.400	35	94 ^c ± 10	195 ^c ± 10	0.429	0.600	0.600	1.00
$N = 2000$ rpm	No constriction	25	–	77 ^g ± 3	0.600	0.600	0.600	1.00
$D_o = 0.8$ mm	0.432	36	77 ^c ± 10	122 ^e ± 10	0.420	0.600	0.600	1.00

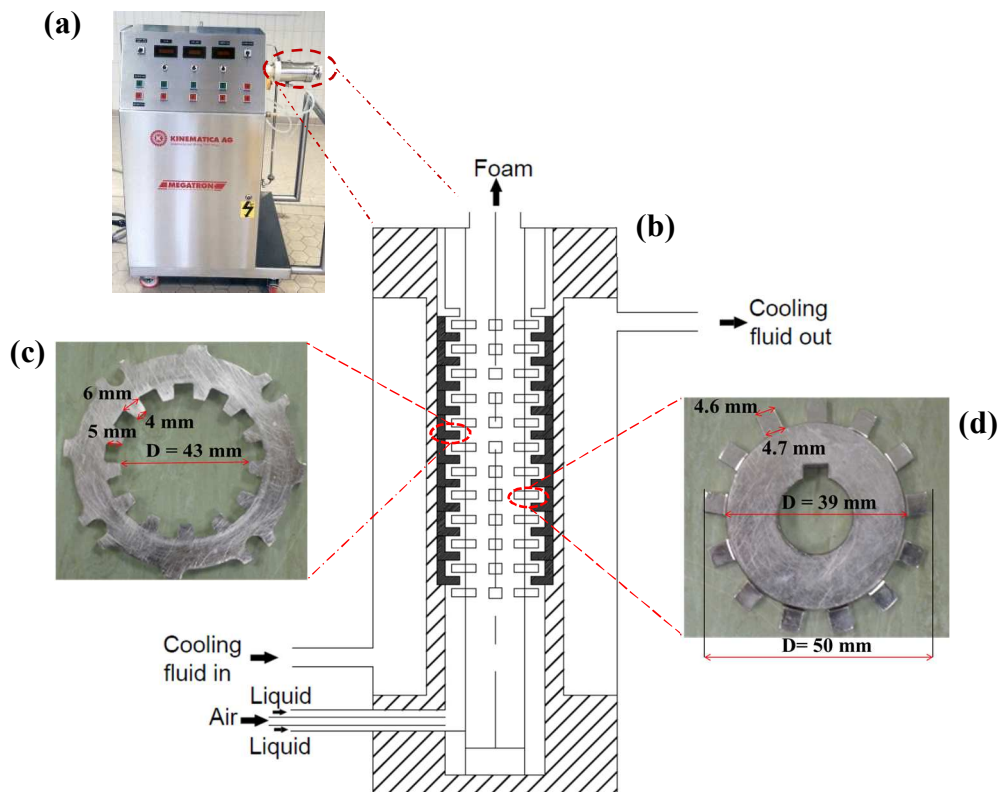


Fig. 1. Foam generator: (a) pilot-scale continuous rotor-stator unit; (b) schematic of mixing-head chamber; (c) stator; (d) rotor. The device consists of 12 rotor-stator pairs in series where, respectively, the rotor and stator have diameters of 50 and 52 mm each. Every rotor and stator has 13 pins ($4.7 \times 4.6 \times 2.5$ mm) with square ends and the gap between the rotor and stator is 1.0 mm.

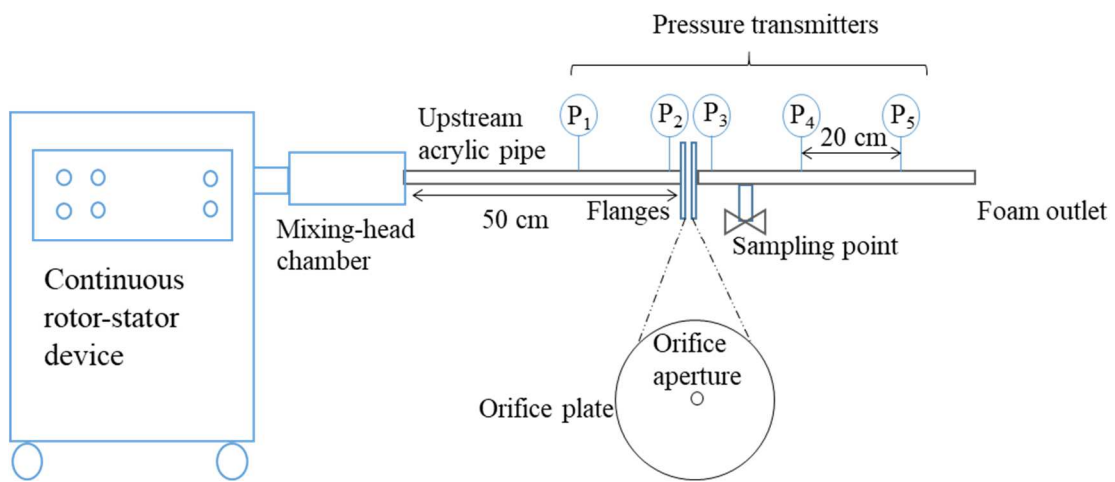


Fig. 2. Schematic of foam flow rig.

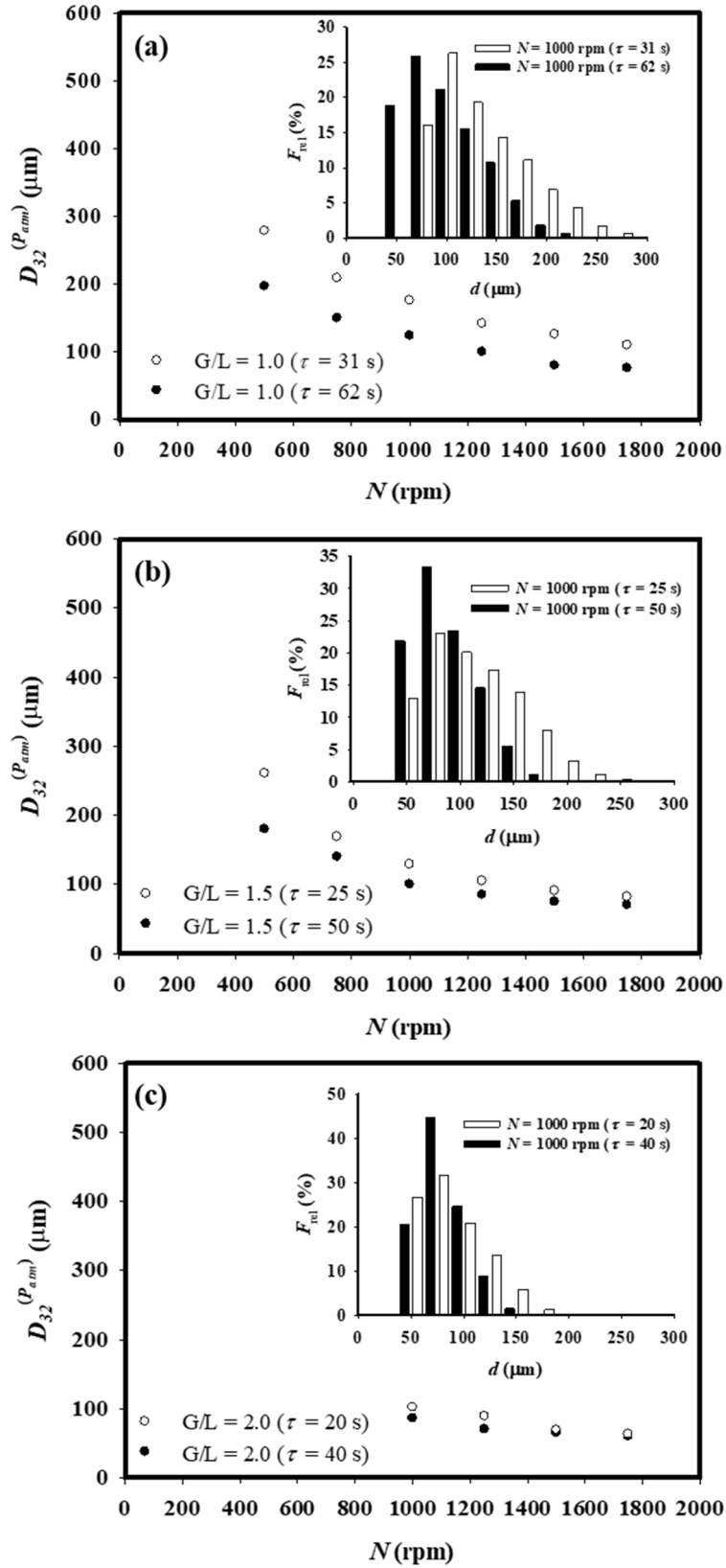


Fig. 3. Effects of residence time on bubble size of foams generated from fluid MF2: (a) $G/L = 1.0$ ($\phi_e = 0.52$); (b) $G/L = 1.5$ ($\phi_e = 0.62$); and (c) $G/L = 2.0$ ($\phi_e = 0.72$).

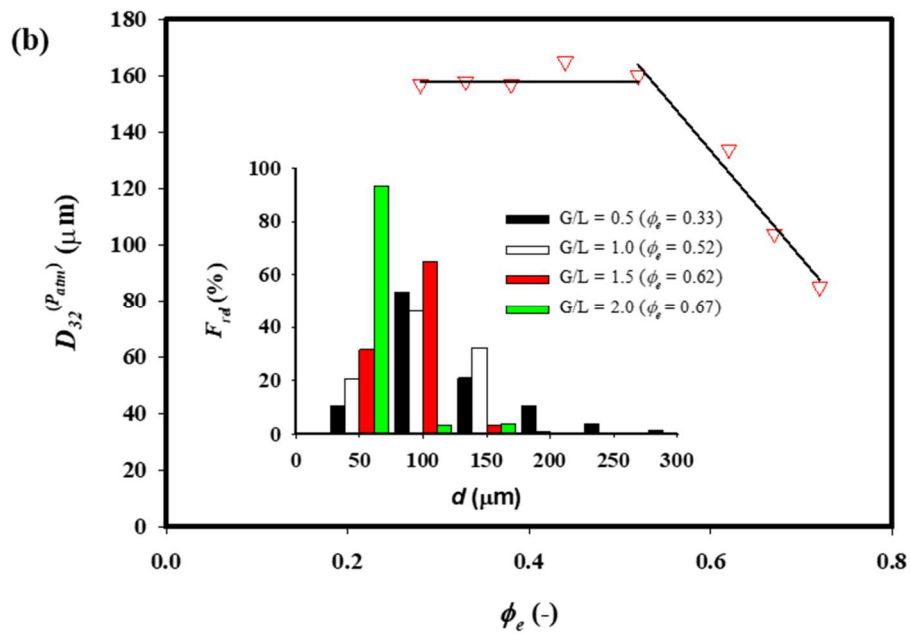
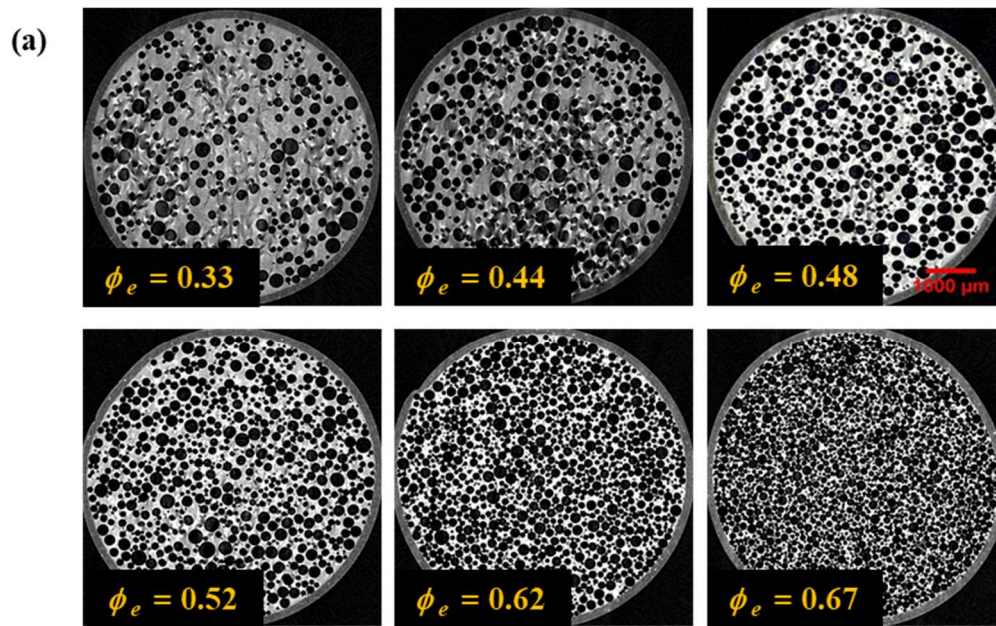


Fig. 4. Effects of air volume fraction on bubble size of foams generated from fluid MF2:
 $N = 1000$ rpm; $\tau = 40$ s.

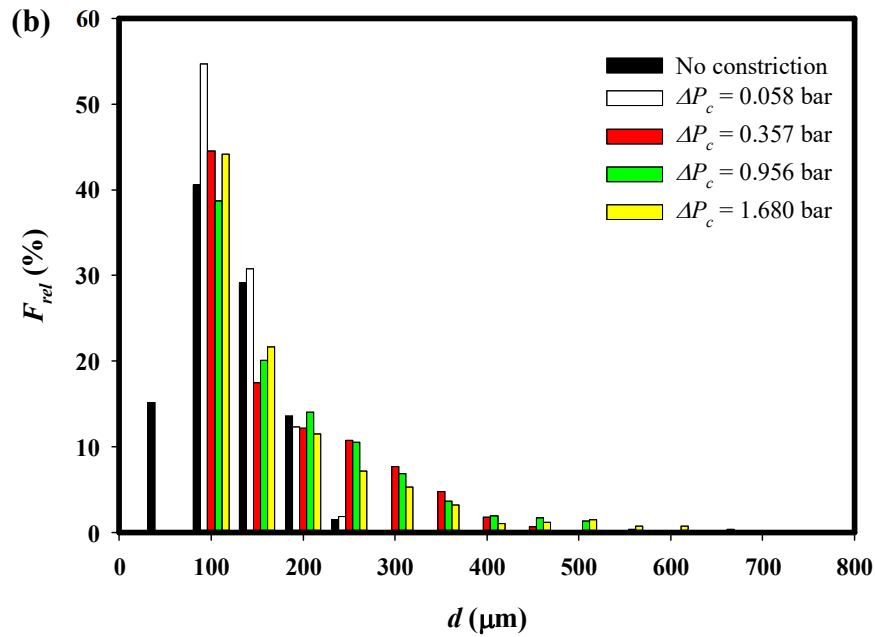
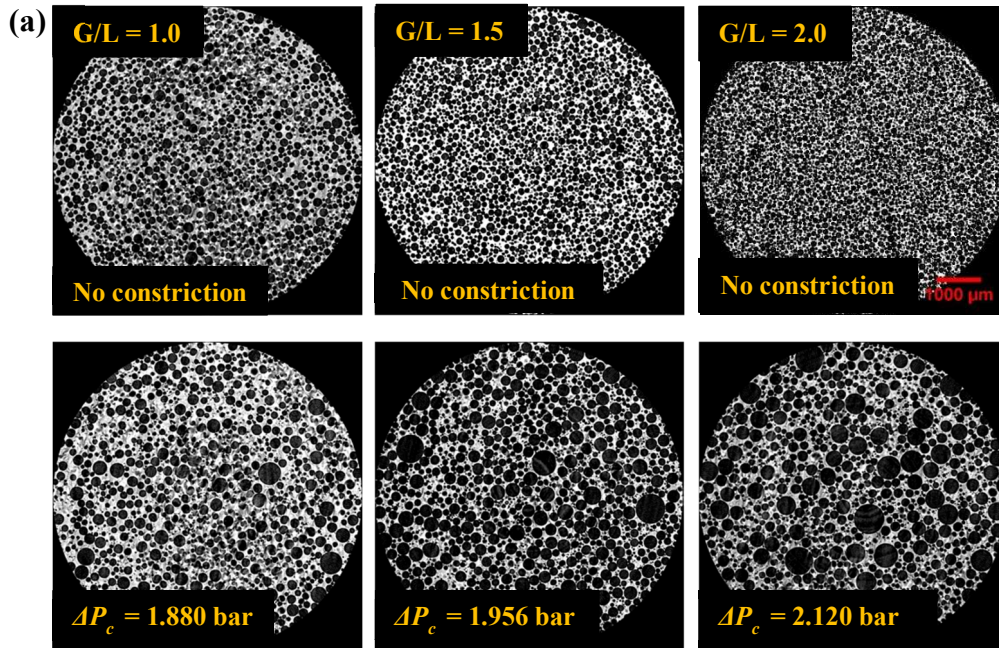


Fig. 5. Effects of pressure drop across constriction on foam microstructure generated from fluid MF2 at $N = 1000$ rpm, $G/L = 1.0$ ($\phi_{th}^{(P_{atm})} = 0.50$), $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$), $G/L = 2.0$ ($\phi_{th}^{(P_{atm})} = 0.67$): (a) Typical X-ray micro-CT foam images; and (b) bubble size distributions.

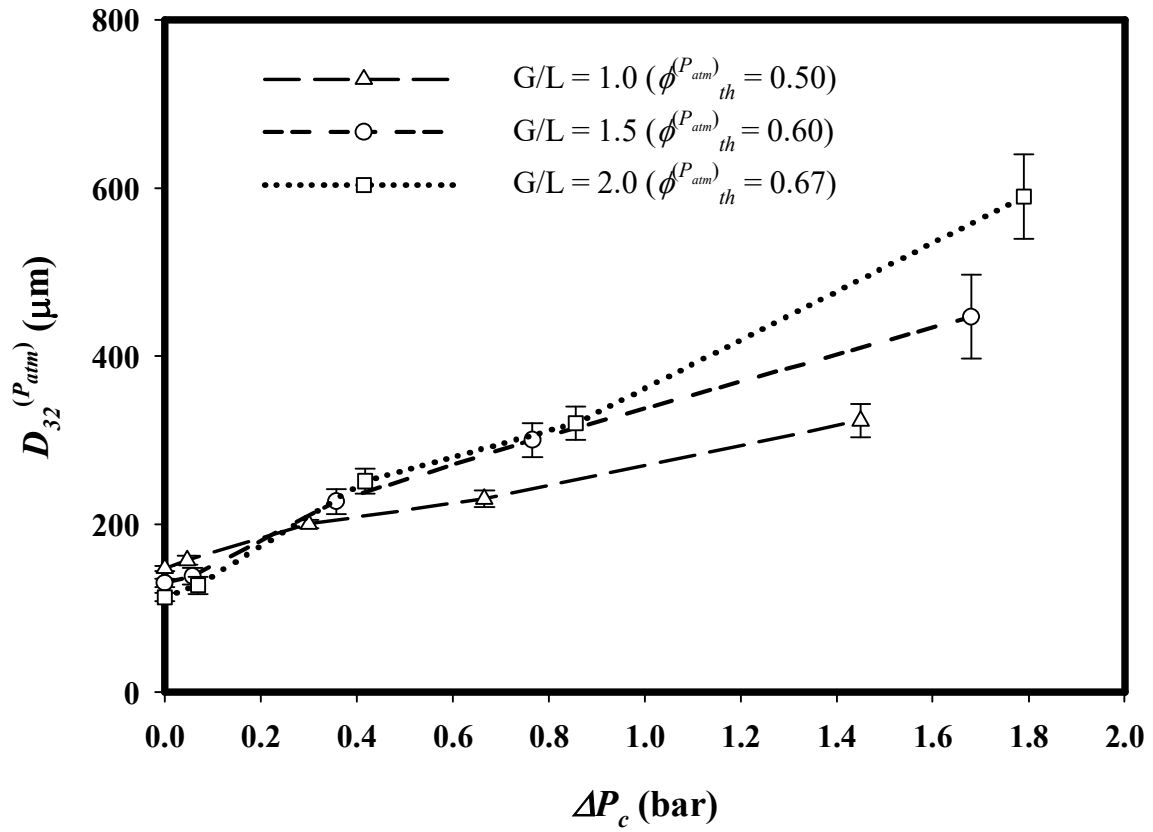


Fig. 6. Effects of pressure drop across constriction on mean bubble size of foams generated from fluid MF2 at $N = 1000$ rpm.

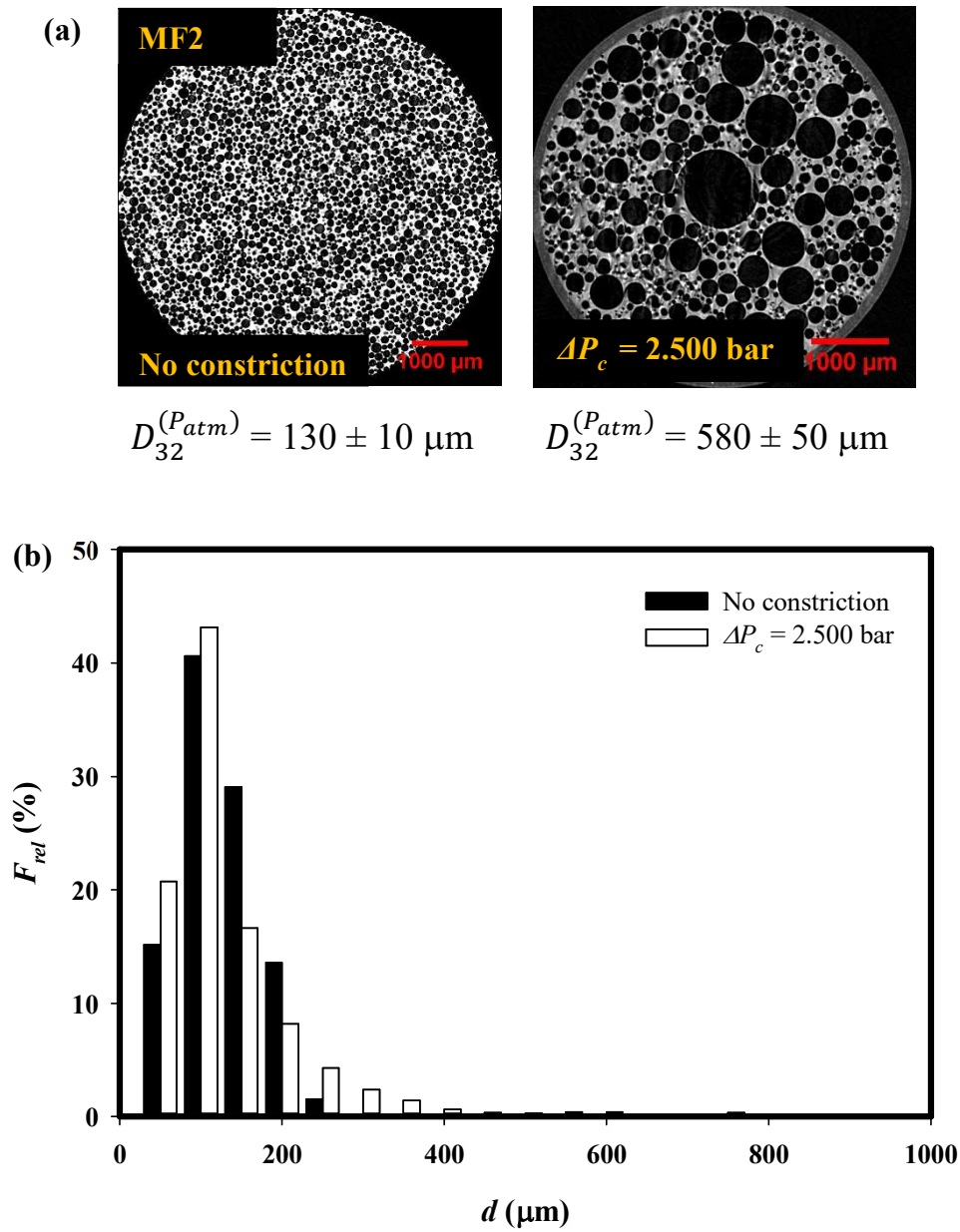


Fig. 7. Effects of pressure drop across constriction on bubble size of foams generated from MF2 at $N = 1000$ rpm, $G/L = 1.5$ ($\phi_{th}^{(Patm)} = 0.60$): (a) typical X-ray micro-CT foam images; and (b) bubble size distributions.

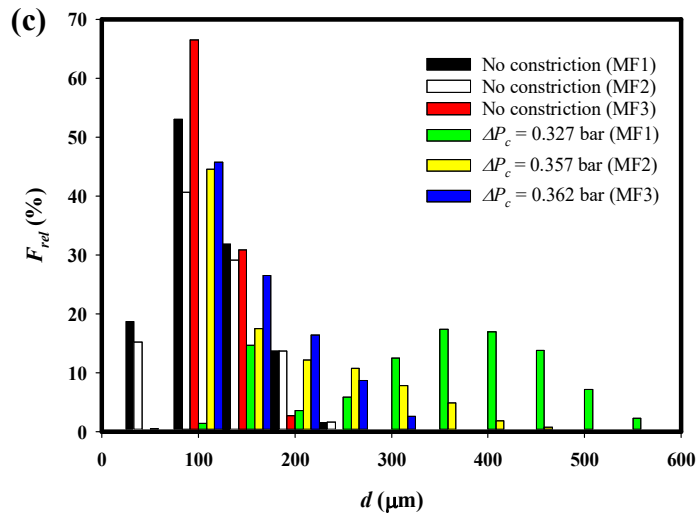
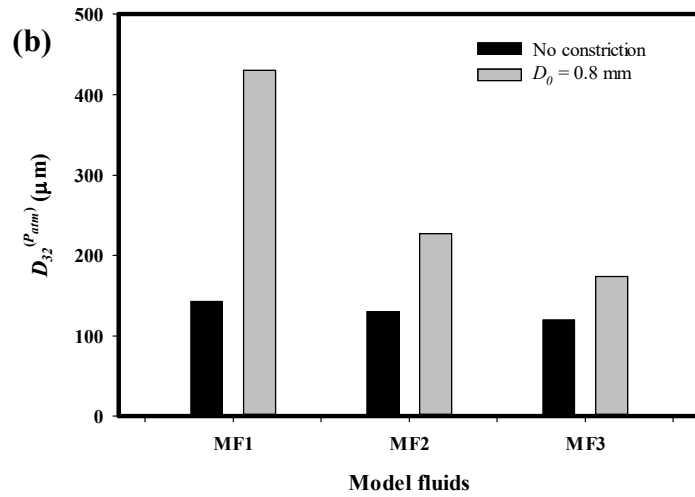
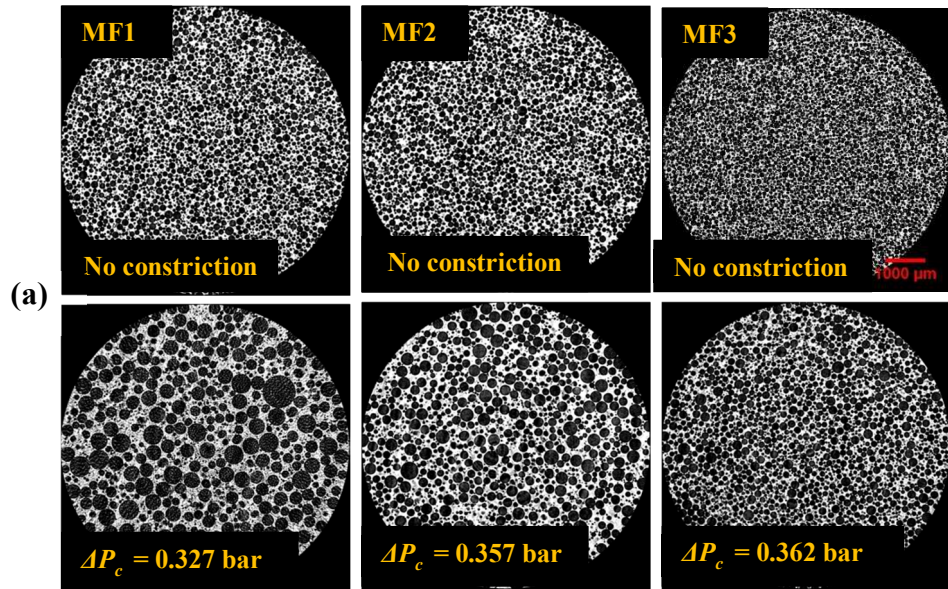


Fig. 8. Effects of PGE 55 concentration on bubble size of flowing foams generated from model fluids MF1 (0.2 wt%), MF2 (0.5 wt%) and MF3 (1.0 wt%) at $N = 1000$ rpm, $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$): (a) X-ray micro-CT foam images; (b) mean bubble size variations; and (c) bubble size distributions.

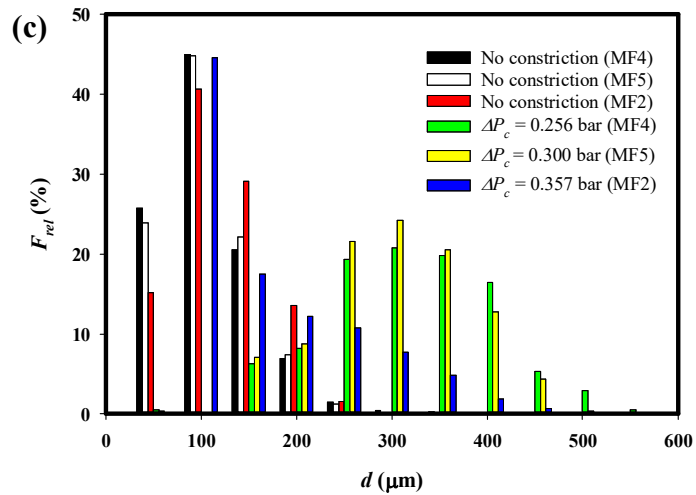
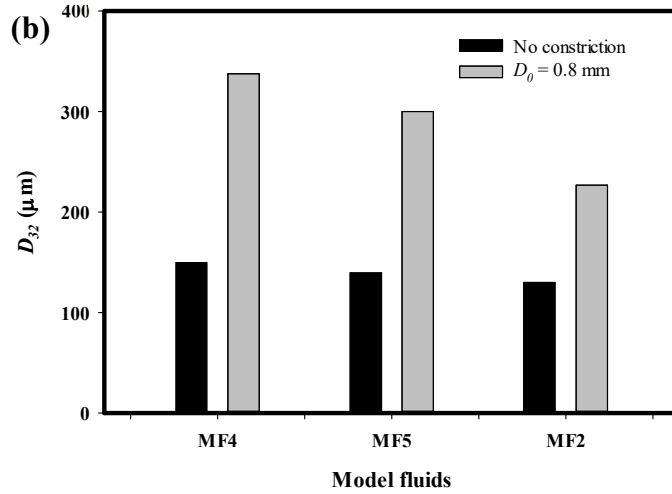
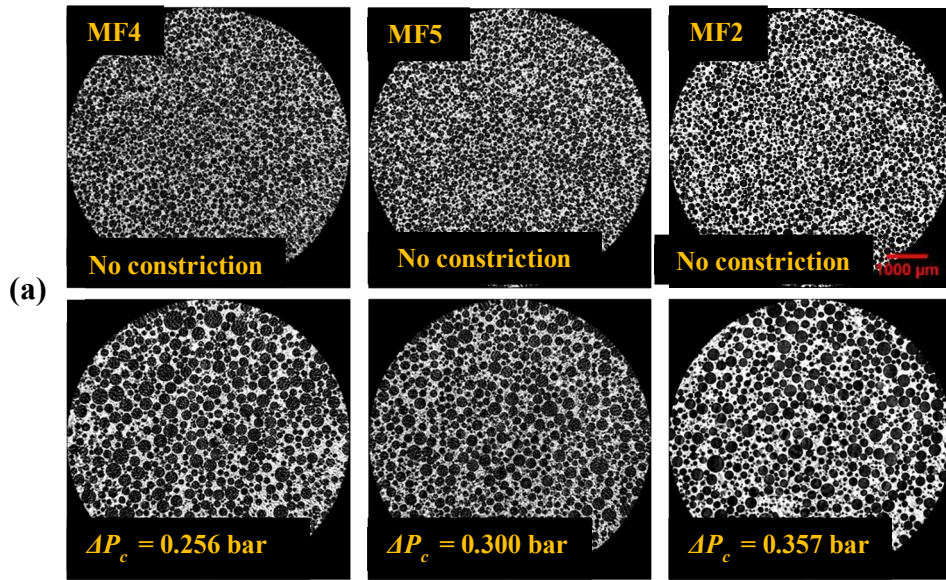


Fig. 9. Effects of xanthan gum concentration on bubble size of flowing foams generated from model fluids MF4 (0.25 wt%), MF5 (0.35 wt%) and MF2 (0.50 wt%) at $N = 1000$ rpm, $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$): (a) X-ray micro-CT foam images; (b) mean bubble size variations; (c) bubble size distributions.

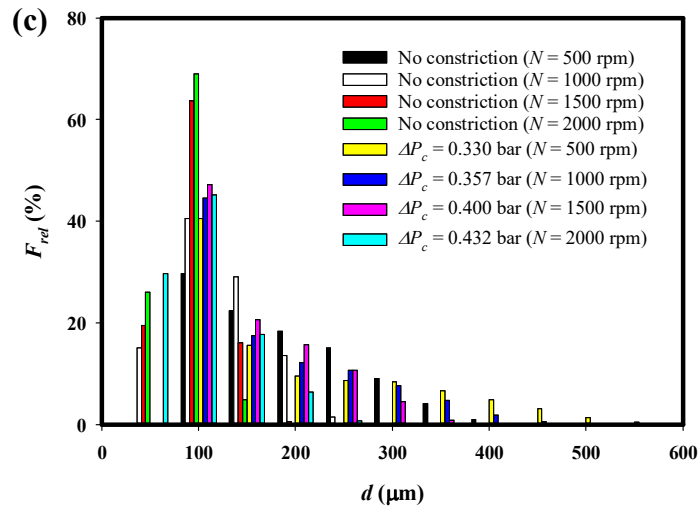
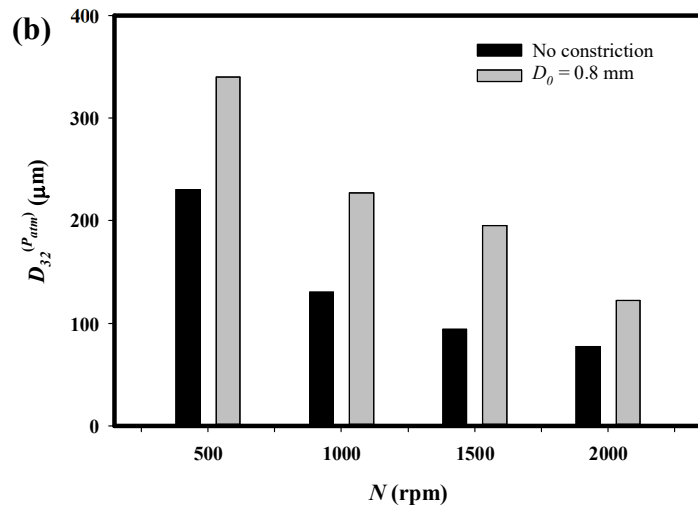
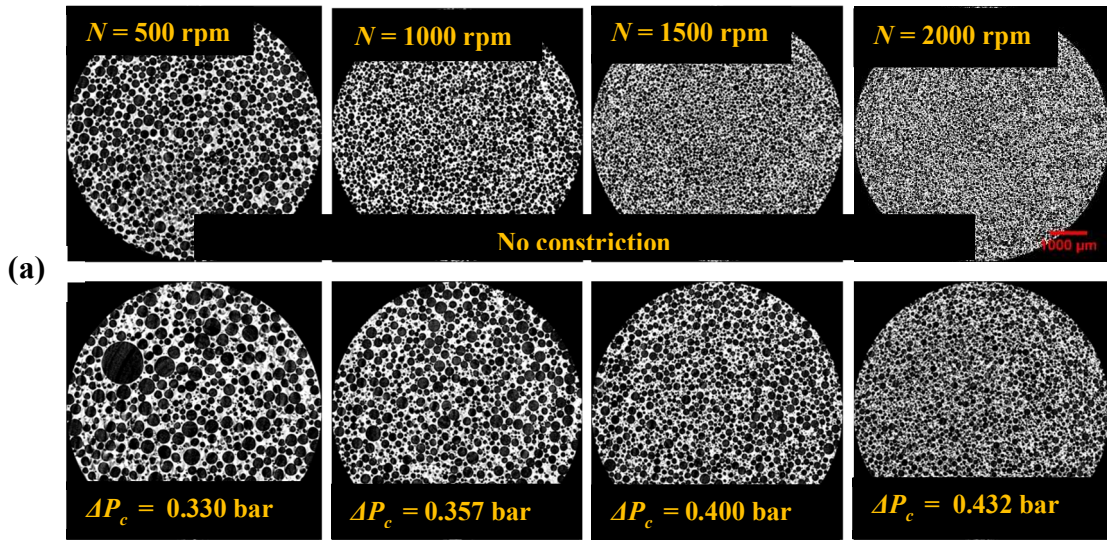


Fig. 10. Effects of rotor speed on bubble size of flowing foams generated from model fluids MF2 at $N = 500, 1000, 1500$ and 1750 rpm; $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$): (a) X-ray micro-CT foam images; (b) mean bubble size variations; (c) bubble size distributions.

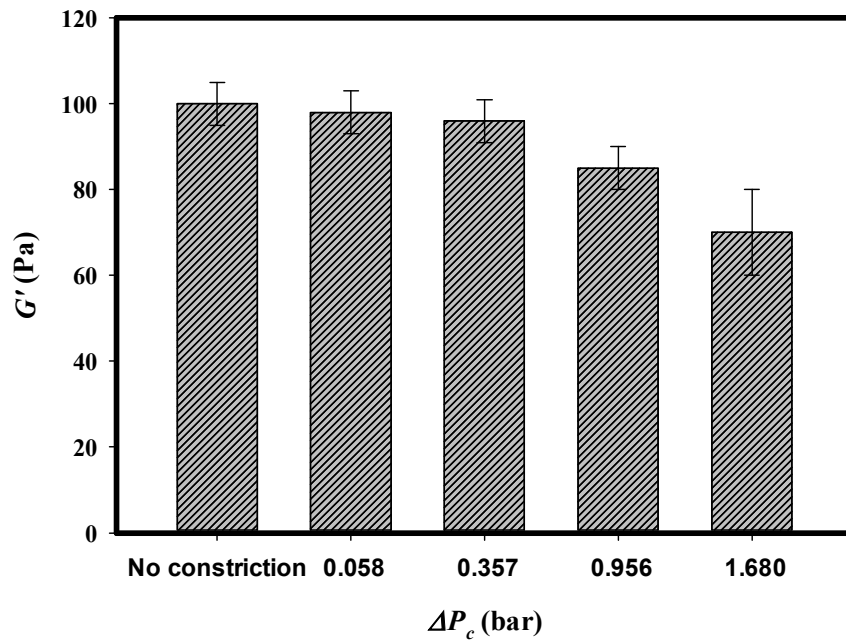


Fig. 11. Effects of pressure drop across constriction on elastic modulus of foam generated from fluid MF2:
 $N = 1000$ rpm, $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$).

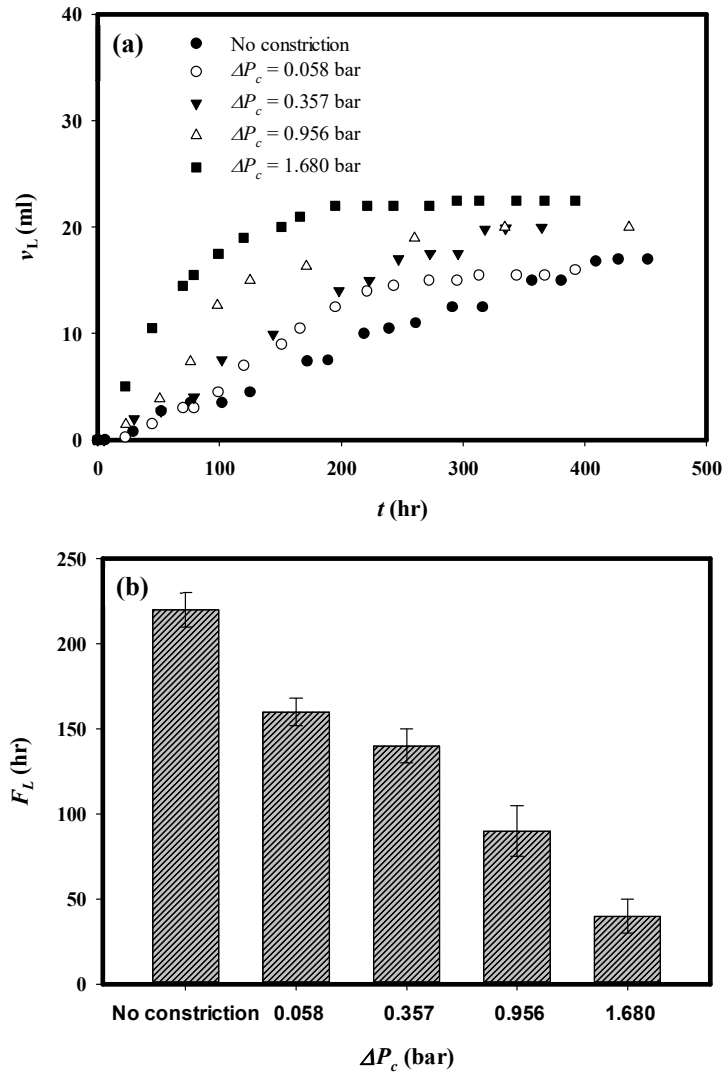


Fig. 12. Effects of pressure drop across constriction on drainage of foams generated from fluid MF2: $N = 1000$ rpm, $G/L = 1.5$ ($\phi_{th}^{(P_{atm})} = 0.60$): (a) foam drainage transient; (b) foam half-life.